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# Technical and Economic Evaluation of a Solid- Particle/Air Direct-Contact Heat Exchanger

Herbert J. Green  
Cécile M. Leboeuf  
Mark S. Bohn



# SERI

## **Solar Energy Research Institute**

A Division of Midwest Research Institute

1617 Cole Boulevard  
Golden, Colorado 80401-3393

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**Prepared under Task No. 4254.10  
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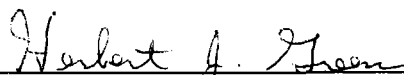
**PREFACE**

The research and development described in this document was conducted within the U.S. Department of Energy's Storage Technology Program. The Solar Energy Research Institute (SERI) is the lead laboratory for research, technology, and system analyses and assessments for thermal energy storage for solar thermal applications and for thermal energy transport.

The goal of SERI's Solar Energy Storage Program is to identify economical energy storage and transport subsystems for the industrial sector and to bring the corresponding technologies to the point where they can be transferred from research and development. The strategy to accomplish this goal is to conduct research in advanced thermal energy storage technologies for solar thermal electric power and solar thermal industrial process heat applications, and in energy transport technologies for industrial process heat applications.

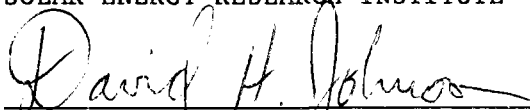
The focus of the program is to develop containment techniques and heat exchange for high temperatures and to define thermochemical transport systems. This report documents a technical and economic evaluation of a solid-particle/air direct-contact heat exchanger to heat pressurized air using solid particles heated in a solar thermal central receiver. This study was done in cooperation with Sandia National Laboratories in Livermore, California, where the development of central receivers using solid particles as the heat transfer media is currently under way for the Solar Thermal Technologies Program. This report was done for the Solar Energy Storage Program in FY 1984 under funding from the Division of Energy Storage Technologies of the U.S. Department of Energy.

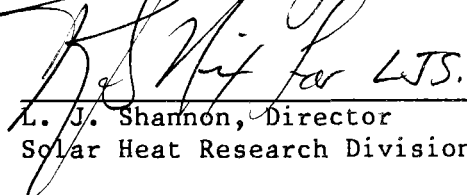
We wish to acknowledge the contributions of Elizabeth Fisher and David H. Johnson who surveyed pertinent literature and prepared a critical review of the state of the art of particle-gas heat exchange, which served as the starting point for this study. We also wish to thank Ron West of Colorado University and Jill Hruby of Sandia National Laboratories, Livermore, for their reviews of this report and their constructive comments.

  
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## SUMMARY

### Objective

The objective of this research is to determine the technical and economic feasibility of heating pressurized air in a direct-contact heat exchanger (DCHX) with hot solid particles from a solar thermal central receiver.

### Discussion

High-temperature applications (above 650°C) of solar thermal central receivers may use solid particles as the heat transfer medium. Some high-temperature applications such as Brayton-cycle electric power generation require pressurized hot air. A direct-contact heat exchanger configuration appears attractive for these applications because of the absence of heat transfer surfaces. In this report, two conceptual designs of solid-particle/air heat exchanger systems are presented including a multistage fluidized-bed heat exchanger, solid-particle feeders and defeeders, and cyclones. The first system is based on state-of-the-art technology while the second system assumes reasonable technical progress resulting from future development activities. Both systems are designed for 1000°C solid particles heating air at 10 atm at a 100 MW<sub>t</sub> heat rate. Both the technical and economic feasibilities of these systems are evaluated. As an alternative to direct contact, a shell-and-tube heat exchanger is evaluated as well.

### Conclusions

The DCHX system is technically feasible though additional development is needed in some areas. In particular, the operating temperatures for valves handling solid particles must be increased and data on particle attrition in a central receiver system is needed for accurate cyclone design. The annual levelized cost per unit of delivered energy for a DCHX system based on state-of-the-art technology is estimated to be \$6.66/GJ (\$7.04/10<sup>6</sup> Btu). If reasonable assumptions are made about the technical progress resulting from future development activities, the cost drops to \$2.30/GJ (\$2.43/10<sup>6</sup> Btu). Most of the cost is for the solids-handling equipment and not in the heat exchanger itself. The cost of a shell-and-tube heat exchanger for the same service was estimated to be \$2.91/GJ (\$3.07/10<sup>6</sup> Btu), about one-third that of the DCHX. This makes the shell-and-tube configuration competitive with the DCHX, although the applicability of this configuration at high temperatures is yet to be determined.

These costs were calculated using a cost methodology developed by the SERI Solar Energy Storage Program. In addition, a cost methodology from the Solar Thermal Technology Program was used to allow comparison to the Solar Thermal cost goals. Using the Solar Thermal methodology, the state-of-the-art configuration costs \$4.64/GJ (\$4.90/10<sup>6</sup> Btu), the configuration that assumes reasonable technical progress costs \$1.56/GJ (\$1.65/10<sup>6</sup> Btu), and the shell-and-tube configuration costs \$2.03/GJ (\$2.14/10<sup>6</sup> Btu). All these costs are high compared to the Solar Thermal cost goal of \$8.52/GJ (\$9.00/10<sup>6</sup> Btu) for thermal energy delivered from a solar central receiver.

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## NOMENCLATURE

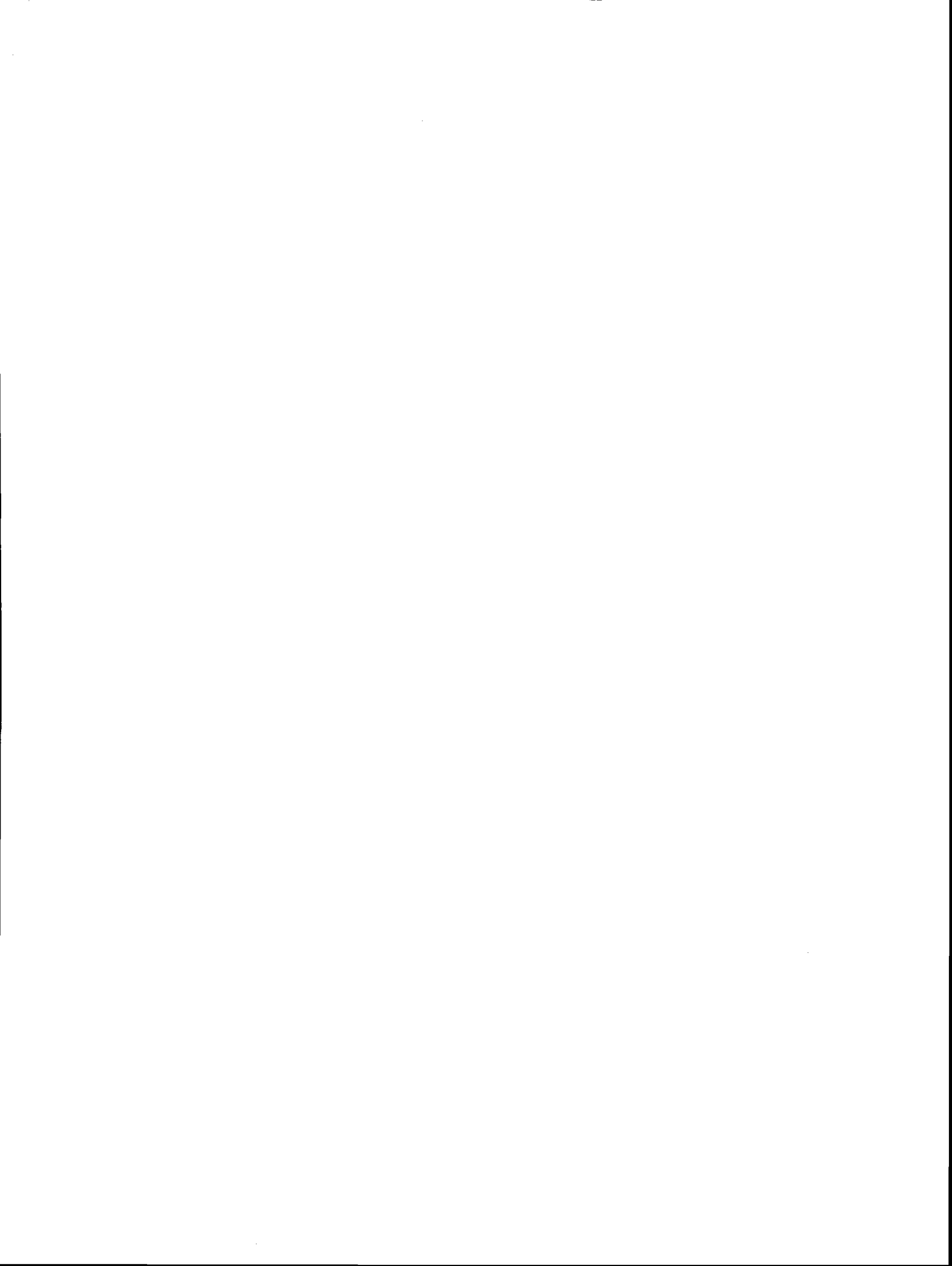
a	surface area per unit volume
$A_1$	surface area ( $m^2$ )
$c_{pa}$	specific heat of air (J/kg K)
$c_{ps}$	specific heat of solid particles (J/kg K)
$C_c$	corrosion allowance (in.)
$C_d$	drag coefficient
$C_f$	capacity factor
$C_m$	cost of electricity (\$/kWh)
$C_t$	total cost of insulation plus cost of lost heat (\$)
dp	particle diameter (m)
$d_s$	particle diameter (cm)
$d_{sh}$	inner shell diameter (in.)
D	orifice diameter (in.)
$D_h$	hydraulic diameter
$D_i$	inside diameter of the tubes
$D_o$	outside diameter of the tubes
$E_j$	joint efficiency
F	friction factor adjustment for finned tube geometry
g	$981 \text{ cm/s}^2$
h	heat transfer coefficient ( $W/m^2 \text{ K}$ )
$h_f$	operating bed depth
$h_m$	static bed depth
$h_{sh}$	total height of the heat exchanger shell (m)
H	bed height
$H_a$	air-side heat transfer coefficient ( $W/m^2 \text{ K}$ )
$H_p$	particle-side heat transfer coefficient ( $W/m^2 \text{ K}$ )
k	thermal conductivity of air ( $W/m \text{ K}$ )
$k_1$	thermal conductivity of internal insulation ( $W/m \text{ K}$ )
$k_2$	thermal conductivity of external insulation ( $W/m \text{ K}$ )
$K_a$	thermal conductivity of air
$K_s$	thermal conductivity of alumina
$K_w$	wall thermal conductivity
L	tube length

## NOMENCLATURE (Continued)

$\dot{m}_a$	mass flow rate of air (kg/s)
$\dot{m}_s$	mass flow rate of solid particles (kg/s)
$Nu_a$	air-side Nusselt number
$P$	internal pressure (psig)
$P_b$	pressure drop in the bed ( $N/m^2$ )
$Pe$	Peclet number
$Pr$	Prandtl number
$Pr_a$	air-side Prandtl number
$P_t$	pressure drop in the multistage fluidized-bed heat exchanger ( $N/m^2$ )
$q$	heat loss, heat flux ( $W/m^2$ )
$Q$	heat duty (MW)
$R_a$	air-side fouling resistance
$Re$	Reynolds number
$Re_a$	air-side Reynolds number
$Re_p$	particle-side Reynolds number
$R_p$	particle-side fouling resistance
$S$	maximum allowable stress (psi)
$t_{sh}$	thickness of the shell (in.)
$t_1$	thickness of internal insulation (m)
$T_{ai,n}$	air inlet temperature for stage n
$T_{ao,n}$	air outlet temperature for stage n
$\bar{T}_{s,n}$	average particle temperature for stage n
$u_{mf}$	minimum velocity for fluidization (cm/s)
$u_o$	operating air velocity (cm/s)
$u_s$	superficial gas velocity (m/s)
$u_t$	particle terminal velocity (cm/s)
$U$	overall heat transfer coefficient
$U_a$	volumetric heat transfer coefficient
$U_c$	air inlet velocity (m/s)
$V_a$	velocity of air
$V_c$	cyclone air inlet velocity (m/s)
$V_1$	total volume of internal insulation ( $m^3$ )
$V_{1h}$	volume of internal insulation required for an ellipsoidal head ( $m^3$ )

## NOMENCLATURE (Concluded)

$V_{1sh}$	volume of internal insulation required for the shell ( $m^3$ )
$V_o$	bed velocity
$W$	pumping power (kW)
$W_h$	weight of head (kg)
$W_s$	solids efflux rate ( $lb/s\ ft^2$ )
$W_{sh}$	weight of the shell (kg)
$W_t$	total weight of the heat exchanger vessel (lb)
$Y_w$	wall thickness
$\gamma_b$	bulk density
$\Delta_p$	pressure drop ( $N/m^2$ )
$\Delta T$	temperature difference ( $^{\circ}C$ )
$\Delta T_{1M}$	log-mean temperature difference
$\epsilon$	void fraction
$\epsilon_m$	void fraction in the static bed
$\epsilon_{mf}$	bed voidage at minimum fluidization
$\eta$	collection efficiency
$\eta_a$	heat exchanger efficiency on the air side
$\eta_c$	compressor efficiency
$\eta_m$	motor efficiency
$\eta_s$	heat exchanger efficiency on the particle side
$\mu$	air viscosity ( $Ns/m^2$ )
$\rho_a$	air density ( $g/cm^3$ )
$\rho_b$	particle bulk density ( $g/cm^3$ )
$\rho_{cs}$	density of carbon steel ( $lb/ft^3$ )
$\rho_s$	particle density ( $g/cm^3$ )
$\phi_s$	particle sphericity



## 1.0 INTRODUCTION

Solid particles have been studied as a heat transfer and storage medium for central receiver solar thermal systems (Burolla et al. 1984; Falcone et al. 1985; Martin and Vitko 1982). Figure 1-1 shows a conceptual design of a solid-particle receiver. Solid particles show potential to operate at higher temperatures by virtue of their chemical stability, essentially zero vapor pressure, and ability to withstand high incident flux levels. Applications for high-temperature central receiver systems include industrial process heat, production of fuels and chemicals, and cogeneration of steam and electricity.

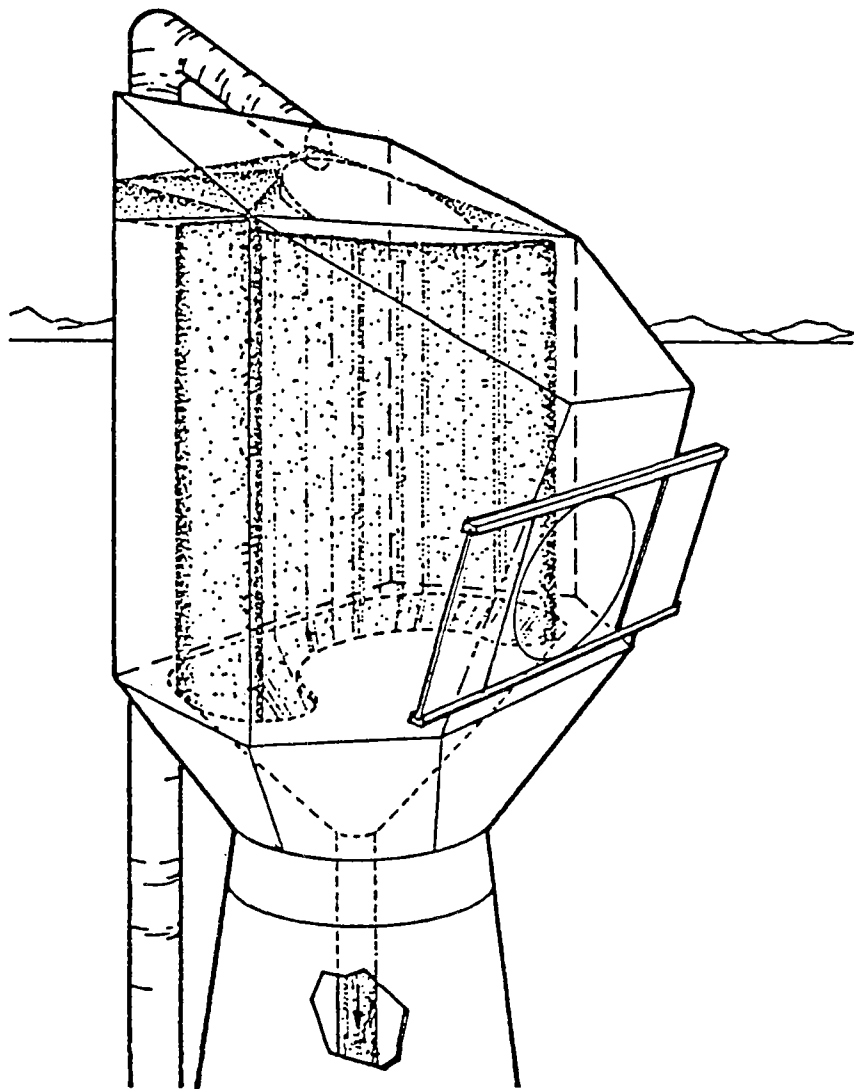


Figure 1-1. Conceptual Design of Solid-Particle Receiver (Sandia National Laboratories, Livermore)

Many of these applications require pressurized hot air. Delivering hot air from a solid-particle central receiver system requires a solid-particle-to-air heat exchanger. Figure 1-2 is a schematic of a simplified system where solid particles from high-temperature storage pass to a heat exchanger and on to low-temperature storage. A direct-contact configuration for the heat exchanger is an attractive option for such a system. Eliminating heat transfer surfaces reduces the problem of strength limitations of these surfaces at high temperature and, thus, has the potential to reduce costs. Also, there has been considerable commercial experience with solid particles as a heat transfer medium using direct contact (Martin and Vitko 1982).

The subject of this report is the conceptual design and costing of a solid-particle/air direct-contact heat exchanger (DCHX). The objective of the study was to determine the economic and technical feasibility of a solid-particle/air heat exchanger to supply pressurized hot air to an industrial process or to a Brayton-cycle gas turbine. Economic feasibility is addressed by calculating the annual levelized cost of the DCHX per unit of thermal energy delivered. The calculation will be based on a cost methodology developed by the SERI Solar Energy Storage Program. A cost methodology from the Solar Thermal Technology Program will also be used to compare the cost of the DCHX to the Solar Thermal Program cost goal of \$8.52/GJ (\$9.00/10<sup>6</sup> Btu) for thermal energy delivered by a central receiver system. Technical feasibility is determined by evaluating the heat exchanger conceptual design parameters in light of state-of-the-art technology and commercially available equipment.

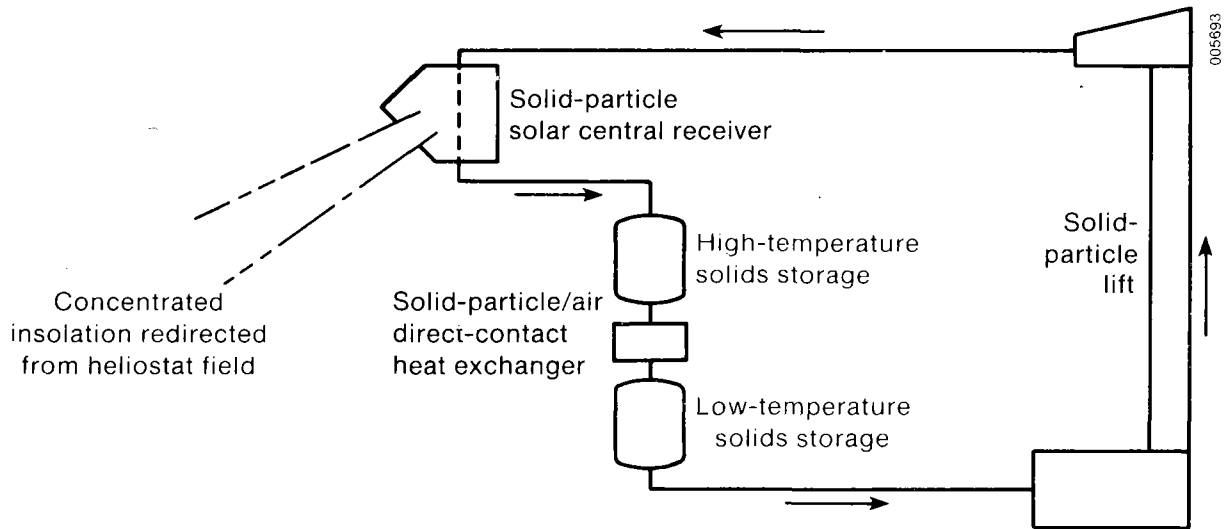


Figure 1-2. Solid-Particle Central Receiver System



We selected the following parameters for the study:

- 100-MW<sub>t</sub> capacity
- 1000°C<sub>t</sub> solid-particle inlet temperature to DCHX
- 0.5-mm particle size
- Alumina particles
- 10 atm delivered air pressure
- Delivered air quality adequate for use in a gas turbine.

The complete heat exchanger system includes the apparatus to feed the particles into and out of the heat exchanger and to clean the outlet air stream. The compressor to supply air to the heat exchanger is not included, but the portion of the compressor operating cost attributable to pressure drop in the heat exchanger and the air cleaner is included. This is reasonable since, for a gas turbine application, the compressor is an integral part of the turbine. For an industrial process requiring pressurized hot air, a compressor is required regardless of the choice of heat exchanger.

In the following chapters, we will select a conceptual design of a DCHX system and size and cost the system using the parameters listed above. This design, referred to hereafter as the original configuration, will be based on the best information available on the state of the art of each of the technologies required by the design. We will also present the size and cost of a "best case" configuration for which we will assume progress in several technologies that will result from future development activities. Finally, we will evaluate a shell-and-tube design as an alternative to direct contact.

2.0 CONCEPTUAL DESIGN

The essential components of the DCHX system include the heat exchanger itself, feeders and defeeders to get the particles into and out of the high-pressure heat exchanger, and a separator to clean residual particles out of the heated air stream. We reviewed pertinent literature concerning possible designs and performance of each of these components. The results of this review are in the notes in Appendix B.

Figure 2-1 shows the specific components recommended for the DCHX as a result of this review. For each component, we selected a baseline design that offers the best performance and for which sufficient information exists to size and cost the component. In addition, we selected optional designs that hold promise for improved performance but for which additional information is needed to predict performance and cost. The baseline design for the feeder shown in Figure 2-1 is not the same as that given in Appendix B. The switch from a piston feeder to a lockhopper feeder was made after the initial review. Additional evaluation revealed that the lockhopper is the only design that is now technically feasible at 1000°C and that lockhopper operational costs caused by vent gas losses are smaller than originally thought.

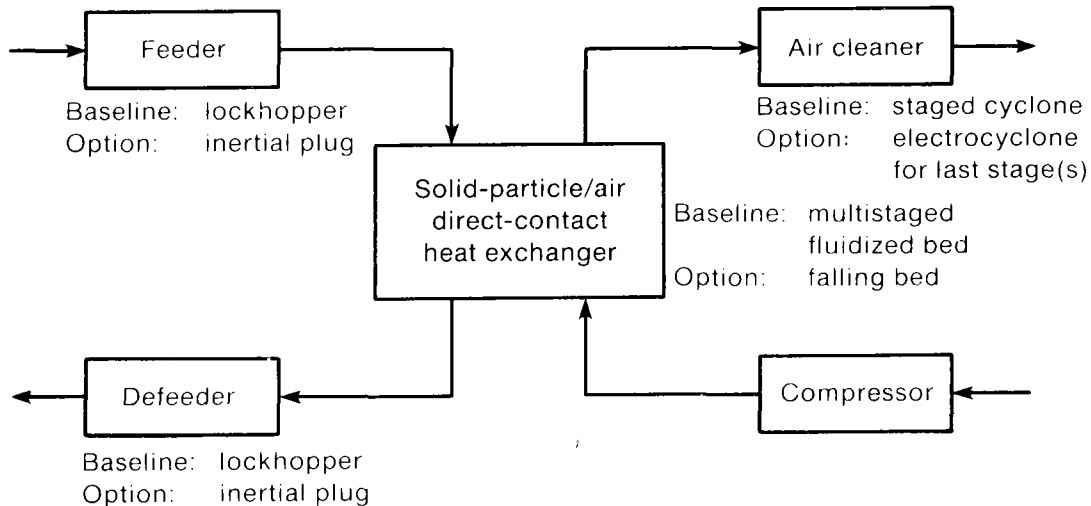


Figure 2-1. Direct-Contact Heat Exchanger Subsystems Baselines and Options to Be Explored

Once we selected the components, we completed a conceptual design of each. Figures 2-2 through 2-4 show these conceptual designs. The feeders, shown in Figure 2-2, include three lockhoppers that will be sized so that any two can deliver the required flow rate of particles. The third lockhopper can be off-line for valve repair. Isolation valves are located above and below each lockhopper for this purpose. The capability for valve repairs during operation was provided because we anticipated that frequent overhauls would be required for valves handling high-temperature solids. Buffer storage above and below the lockhoppers is provided because the flow to and from the lockhoppers is intermittent while the flows to the DCHX and from the solid-particle transport system are continuous. All of the vessels are constructed of carbon steel and have adequate internal insulation to keep the steel at 316°C as recommended in the ASME codes (Peters and Timmerhaus 1980).

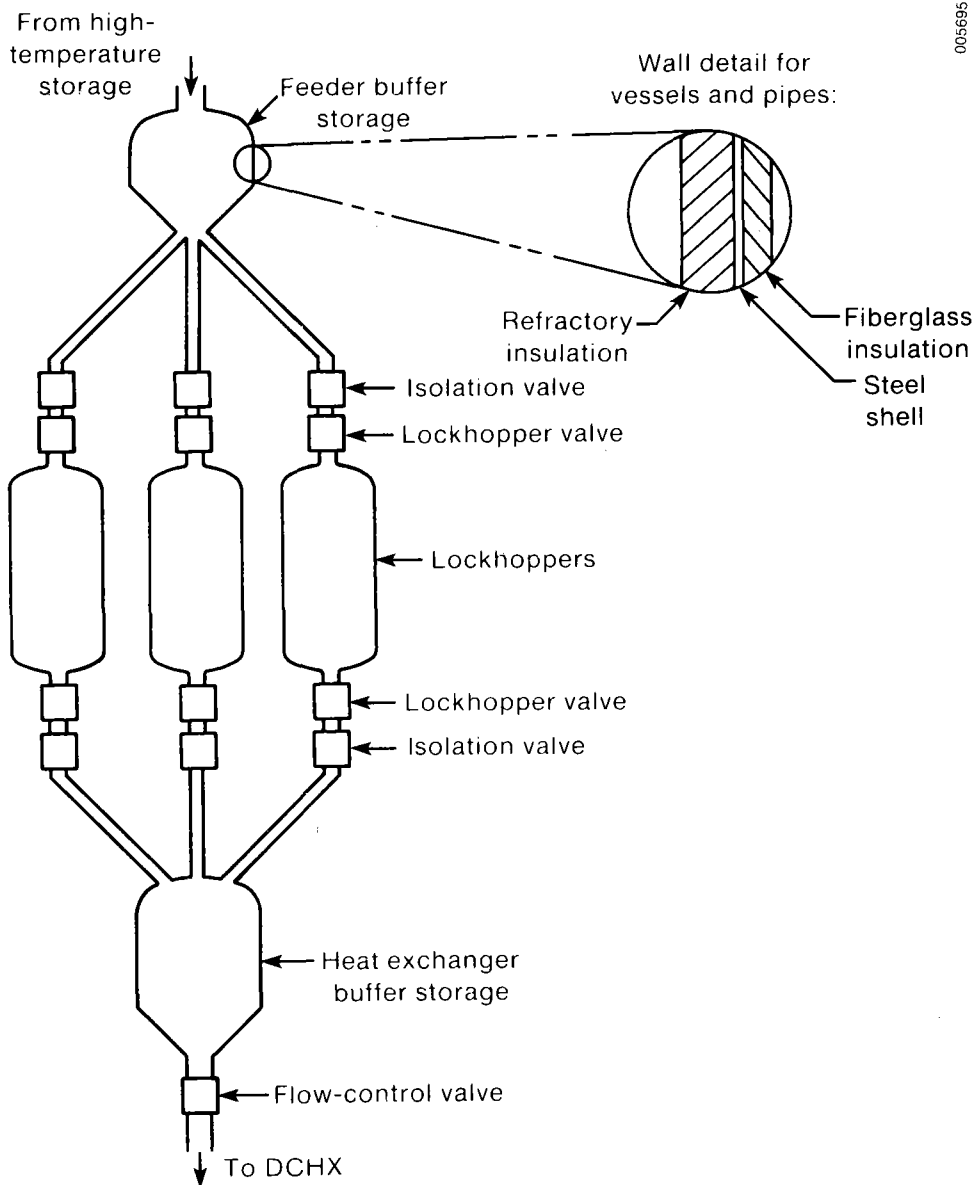
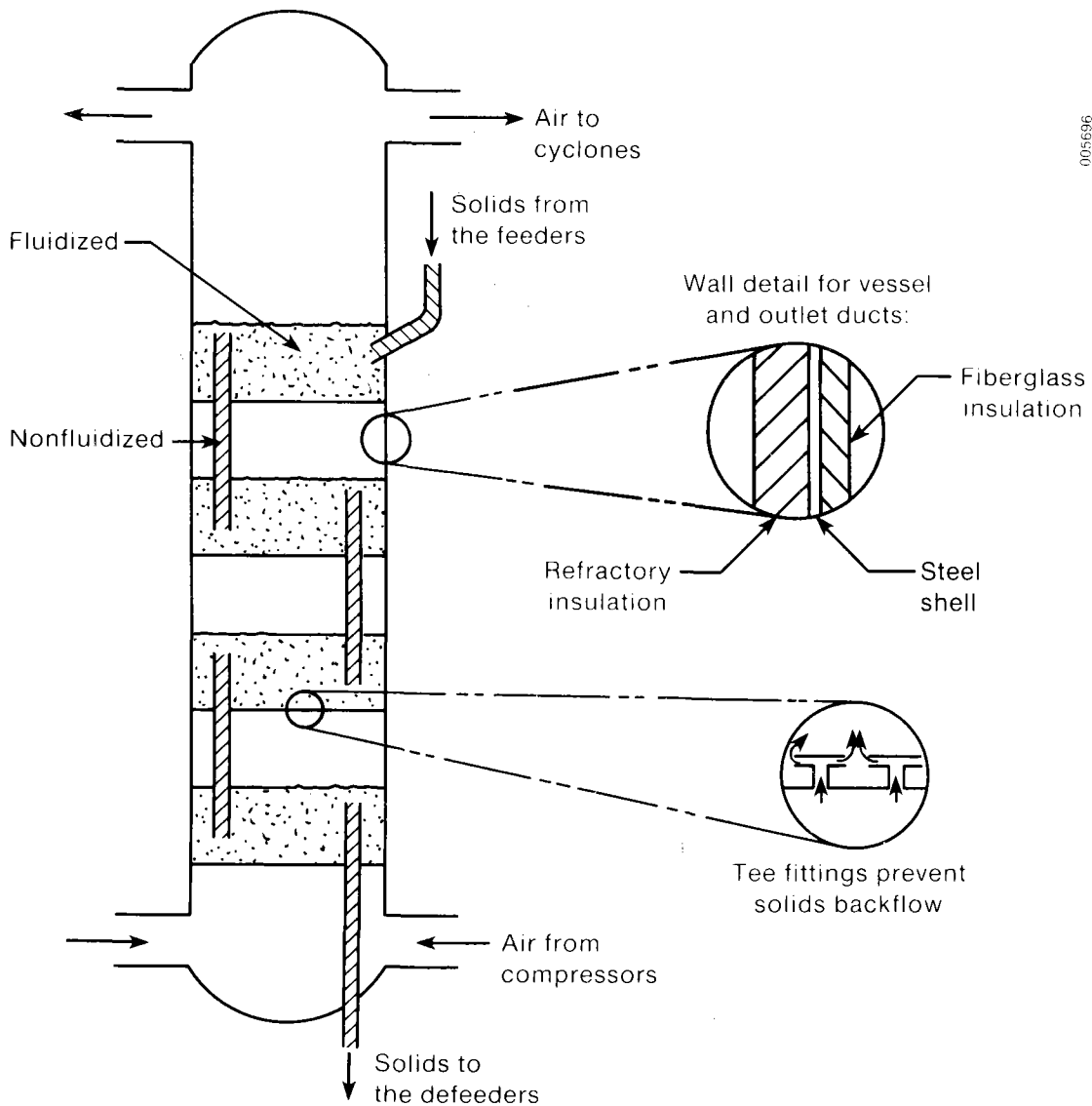


Figure 2-2. Solid-Particle Feeder Subsystem Schematic

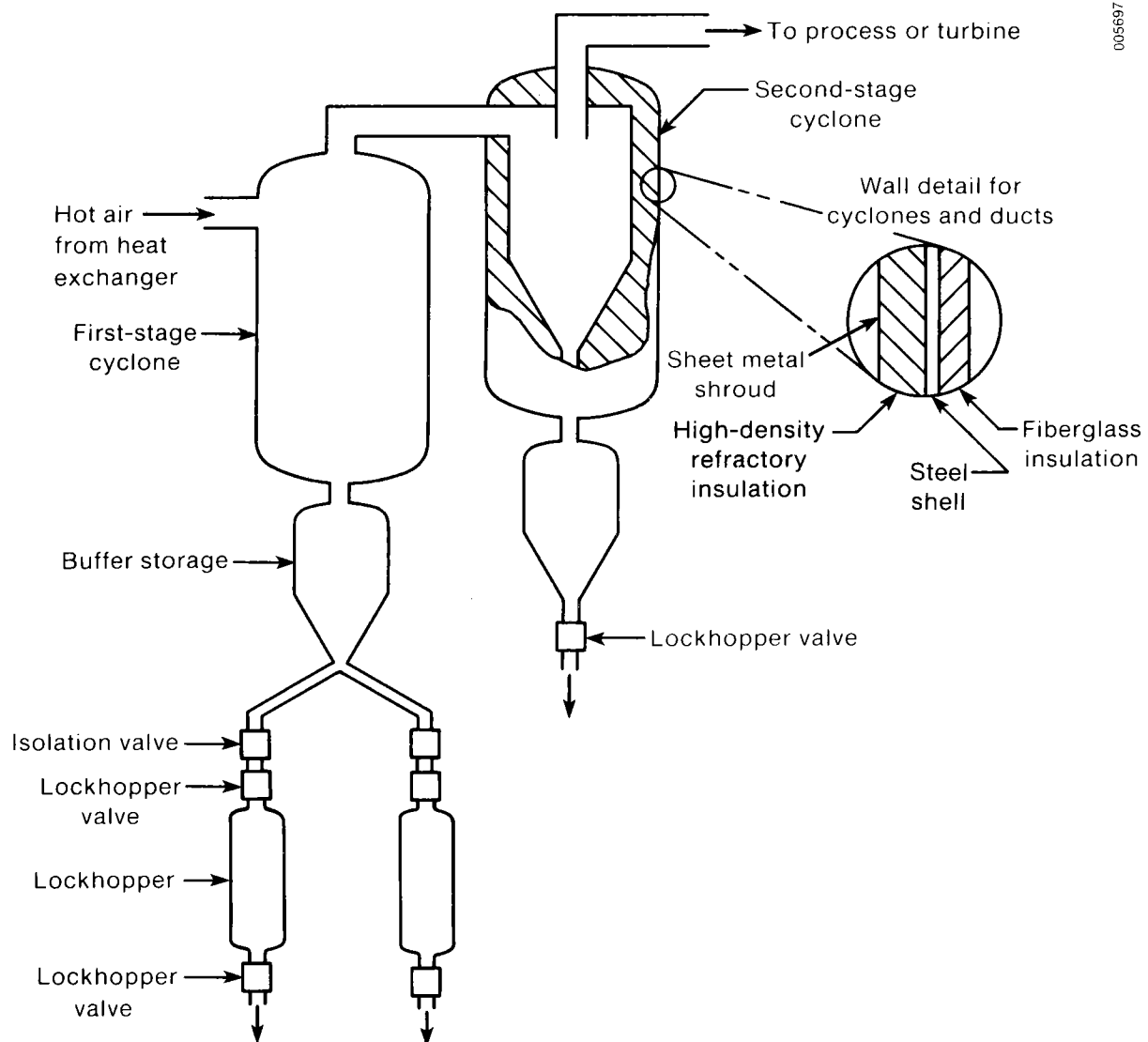


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**Figure 2-3. Direct-Contact Heat Exchanger Schematic**

The defeeders are similar to the feeders. Their internal insulation is less thick than that of the feeders because the particles being handled have a lower temperature. Isolation valves are located above the defeeder lock-hoppers, but none are required below because the adjoining buffer storage is at atmospheric pressure. Also no flow-control valve is required.

Figure 2-3 shows the conceptual design of the DCHX. Although only one down-comer is shown between each stage, more than one might be required in a final design. Each grid (the air distributor and floor of the bed) is equipped with tee fittings as shown. These fittings leave an unfluidized layer of particles on the grid providing an insulating layer between the grid and the fluidized



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**Figure 2-4. Hot Air Cleaning Subsystem Schematic**

bed. This allows a lower operating temperature for the grid, which may be important in the uppermost and hottest bed. The fittings may also be used on the lower beds to prevent drain down when the heat exchanger is not in use. The actual number of stages will be specified once we have analyzed the performance of the heat exchanger. Space is allowed below the bottom stage as a manifold for the incoming air. Similarly, a space is provided above the top stage to disengage particles entrained from that stage.

The cyclones, as shown in Figure 2-4, will be contained in a cylindrical pressure vessel. The appropriate installation of internal insulation, as shown in the figure, gives the bottom of each cyclone its familiar conical shape. We will analyze cyclone performance to determine the actual number of stages and

the number of cyclones per stage. The outlet duct is internally insulated and internally shrouded to prevent particles of insulation from contaminating the cleaned air stream. Below the first-stage cyclone, there are two lockhoppers so that valves may be serviced during plant operation as described for the feeders. For the following stage (or stages), the collection rate of solid particles is very low so that the buffer storage can be drained once per day when the system is down and not at pressure.

### 3.0 COMPONENT DESIGN AND SIZING

#### 3.1 Fluidized-Bed Heat Exchanger

##### 3.1.1 Heat Transfer

Hydrodynamic requirements, rather than heat transfer requirements, determine the depth of the fluid bed stages. To demonstrate this, we will show that, because of the very large heat transfer surface area provided by the small particles, thermal equilibrium is reached for very short stage heights. Following this, we will develop a generalized method to predict the performance of a multistage fluidized bed.

Whitaker's (1972) correlation for packed beds estimates the heat transfer between the particles and the gas. This estimate will be compared to the rate of heat transfer expected in a fluidized bed.

$$\frac{hd_p}{k} = \frac{1 - \epsilon}{\epsilon} (0.5 \text{Re}_p^{0.5} + 0.2 \text{Re}_p^{2/3}) \text{Pr}^{1/3}, \quad (3-1)$$

where

- $h$  = heat transfer coefficient ( $\text{W/m}^2 \text{K}$ )
- $d_p$  = particle diameter (m)
- $k$  = thermal conductivity of air ( $\text{W/m K}$ )
- $\epsilon$  = void fraction.

The Prandtl number is defined as:

$$\text{Pr} = \frac{\mu c_{pa}}{k}, \quad (3-2)$$

where

- $\mu$  = air viscosity ( $\text{Ns/m}^2$ )
- $c_{pa}$  = specific heat of air ( $\text{J/kg K}$ ).

The Reynolds number for the particle is:

$$\text{Re}_p = \frac{\rho_a d_p u_s}{\mu}, \quad (3-3)$$

where

- $\rho_a$  = air density ( $\text{kg/m}^3$ )
- $u_s$  = superficial gas velocity (m/s).

The superficial gas velocity  $u_s$  is approximately 0.5 m/s for an 8-m diameter tower flowing 150-kg/s air (100-MW<sub>t</sub> rating). For particle diameters of 0.5 mm and air properties of 20 atm at 1000 K, we obtain a particle Reynolds number of 37, which gives a heat transfer coefficient of 409  $\text{W/m}^2 \text{K}$ . The surface area per unit volume is:

$$a = (1 - \epsilon) \frac{6}{d_p} . \quad (3-4)$$

For a void fraction of 0.5,  $a = 6000 \text{ m}^2/\text{m}^3$ , so the volumetric heat transfer coefficient  $U_a$  is

$$\begin{aligned} U_a &= ha \\ &= 2.5 \times 10^6 \text{ W/m}^3 \text{ K} . \end{aligned} \quad (3-5)$$

The volume per meter of height  $v$  of an 8-m diameter tower is  $51.7 \text{ m}^2$ . For a 10-stage heat exchanger with inlet temperatures of  $300^\circ\text{C}$  (air) and  $1000^\circ\text{C}$  (particles), a log mean temperature difference per stage will be approximately  $\Delta T_{LM} = 35^\circ\text{C}$ . For a  $10\text{-MW}_t$  per stage heat duty  $Q$ , the bed height  $H$  required for thermal equilibrium is:

$$\begin{aligned} H &= 10^8 Q / U_a v \Delta T_{LM} \\ &= 0.2 \text{ cm} . \end{aligned} \quad (3-6)$$

Thus, very little bed height is required for the air entering the bottom of a stage to equilibrate with the particle temperature in the stage. The requirement for good fluidization and bubbling action in the bed, not heat transfer requirements, will determine the bed height.

Since the air rapidly equilibrates with the particle temperature, we equate the air outlet temperature for stage  $n$ ,  $T_{ao,n}$ , with the average particle temperature for stage  $n$  (see Figure 3-1):

$$T_{ao,n} = \bar{T}_{s,n} . \quad (3-7)$$

Neglecting radiative heat transfer and wall losses, a thermal balance on stage  $n$  gives:

$$\dot{m}_s c_{ps} (\bar{T}_{s,n+1} - \bar{T}_{s,n}) = \dot{m}_a c_{pa} (T_{ao,n} - T_{ai,n}) , \quad (3-8)$$

where

$\dot{m}_s$  = mass flow rate of solid particles (kg/s)

$\dot{m}_a$  = mass flow rate of air (kg/s)

$c_{ps}$  = specific heat of solid particles (J/kg K)

$T_{ai,n}$  = air inlet temperature for stage  $n$  (K).

Since  $T_{ai,n} = T_{ao,n-1} = \bar{T}_{s,n-1}$  and  $\gamma = \dot{m}_a c_{pa} / \dot{m}_s c_{ps}$ ,

$$\bar{T}_{s,n+1} - \bar{T}_{s,n} = \gamma (\bar{T}_{s,n} - \bar{T}_{s,n-1}) , \quad (3-9)$$



or

$$\bar{T}_{s,n-1} = \frac{(1 + \gamma)\bar{T}_{s,n} - \bar{T}_{s,n+1}}{\gamma} . \tag{3-10}$$

The stage-to-stage drop in particle temperature is:

$$\Delta T_{s,n} \equiv \bar{T}_{s,n+1} - \bar{T}_{s,n} = \gamma(\bar{T}_{s,n} - \bar{T}_{s,n-1}) . \tag{3-11}$$

This temperature drop decreases by a factor of  $\gamma$  for each stage. At the top of a heat exchanger with  $N$  stages (see Figure 3-2),

$$\Delta T_{s,N-1} \equiv \bar{T}_{s,N} - \bar{T}_{s,N-1} , \tag{3-12}$$

but  $\bar{T}_{s,N} = T_{ao}$ . So from Equation 3-10,

$$\bar{T}_{s,N-1} = \frac{(1 + \gamma)\bar{T}_{s,N} - \bar{T}_{s,N+1}}{\gamma} = \frac{(1 + \gamma)T_{ao} - T_{si}}{\gamma} , \tag{3-13}$$

and

$$\begin{aligned} \Delta T_{s,N-1} &= T_{ao} - \frac{(1 + \gamma)T_{ao} - T_{si}}{\gamma} \\ &= \frac{T_{si} - T_{ao}}{\gamma} . \end{aligned} \tag{3-14}$$

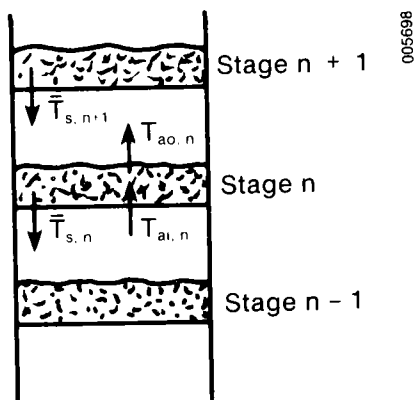


Figure 3-1. Notation for Solid-Particle and Air Temperatures in a Multistage Fluidized Bed

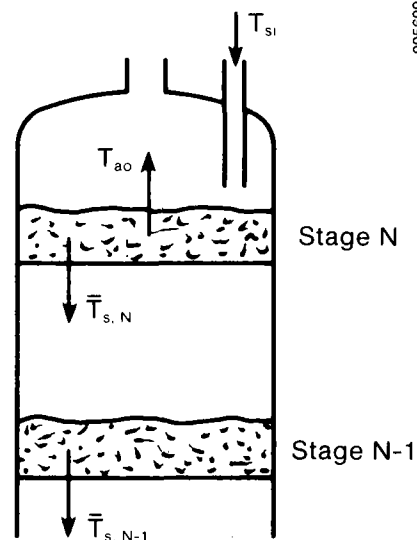


Figure 3-2. Notation for Solid-Particle and Air Temperatures at the Top of a Multistage Fluidized Bed

From Eq. 3-14,  $\Delta T_{s,N} = (T_{si} - T_{ao})$ , therefore

$$\Delta T_{sn} = \frac{T_{si} - T_{ao}}{\gamma^{N-n}} . \quad (3-15)$$

The overall swing in particle temperature is:

$$T_{si} - T_{so} = \sum \Delta T_{sn} = (T_{si} - T_{ao}) \sum_{n=1}^N \gamma^{n-N} . \quad (3-16)$$

Define  $x$  as:

$$x = \sum_{n=1}^N \gamma^{n-N} , \quad (3-17)$$

which expands into:

$$x = \frac{\gamma(\gamma^{-N} - 1)}{(1 - \gamma)} ,$$

so

$$T_{si} - T_{so} = x(T_{si} - T_{ao}) = \gamma(T_{ao} - T_{ai}) . \quad (3-18)$$

Finally, the outlet temperatures are:

$$T_{ao} = \frac{xT_{si} + \gamma T_{ai}}{\gamma + x} \quad (3-19)$$

$$T_{so} = \frac{T_{si}(\gamma + x - \gamma x) + \gamma x T_{ai}}{\gamma + x} . \quad (3-20)$$

Defining the heat exchanger efficiencies on the air and particle sides:

$$\eta_a = \frac{T_{ao} - T_{ai}}{T_{si} - T_{ai}} = \frac{x}{\gamma + x} \quad (3-21)$$

$$\eta_s = \frac{T_{si} - T_{so}}{T_{si} - T_{ai}} = \frac{\gamma x}{\gamma + x} . \quad (3-22)$$

The efficiency therefore depends only on  $\gamma$  and the number of stages. Figure 3-3 plots values of  $\eta_a$  for five values of  $\gamma$  versus the number of stages. Figure 3-4 is a similar plot for  $\eta_s$ .

This analysis does not account for two possible modes of heat transfer between stages. The first is radiation heat transfer between stages. The second is carryover of particles from a given stage into the stage above due to entrainment in the air stream. These modes of heat transfer are, in effect, thermal back mixing between adjacent stages. This back mixing will affect heat exchanger performance only to the extent that it reduces the temperature of the top stage and, thus, reduces  $T_{ao}$ . We will show later that the temperature difference between the top two stages is small. Thus, the radiant back mixing

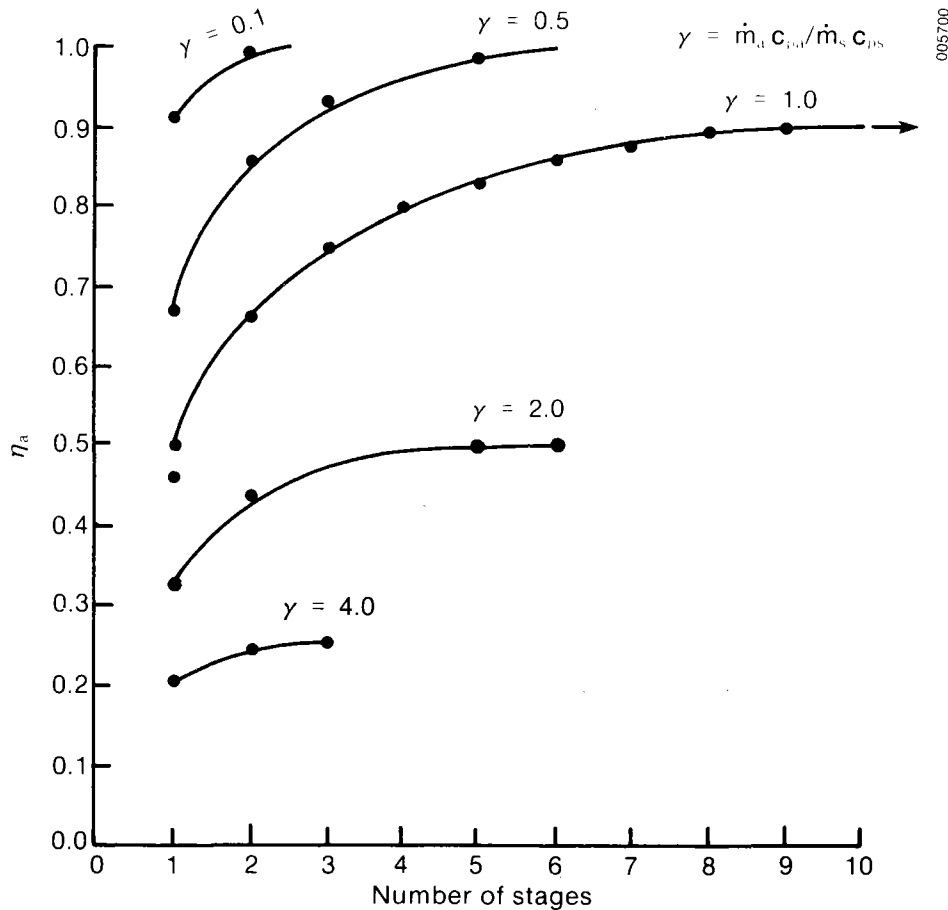


Figure 3-3. Heat Exchanger Air-Side Efficiency versus Number of Stages

is small and can be ignored. As for the entrained particles, only those few that hit the holes in the grid above pass through to the stage above while the rest strike the grid itself and fall back. Because so few particles are carried over, the thermal back mixing is small.

For this study, we selected a four-stage heat exchanger with an outlet air temperature of  $970^{\circ}\text{C}$ . Table 3-1 summarizes the operating conditions for this heat exchanger. Because  $C_{pa}$  very nearly equals  $C_{ps}$ ,  $\gamma$  can be expressed as the ratio of mass flow rates,  $\dot{m}_a/\dot{m}_s$ . The height and diameter of the heat exchanger and the pressure drop will be determined in the following section based on the design of the fluidized beds.

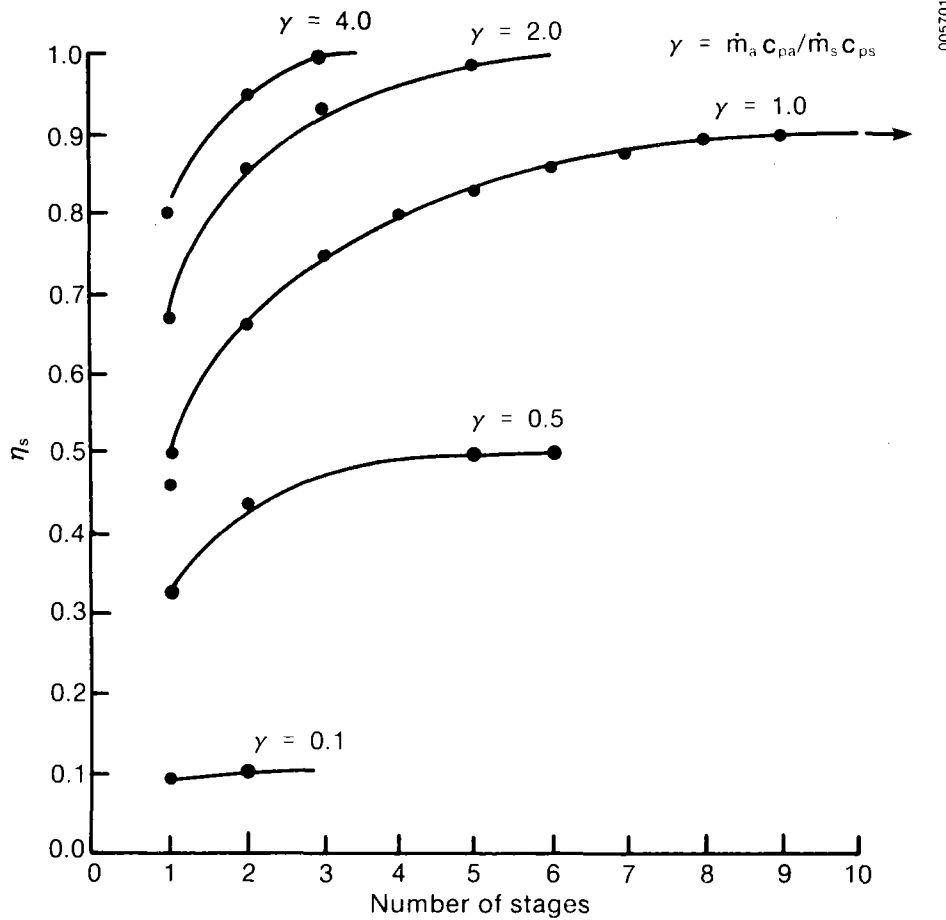


Figure 3-4. Heat Exchanger Particle-Side Efficiency versus Number of Stages

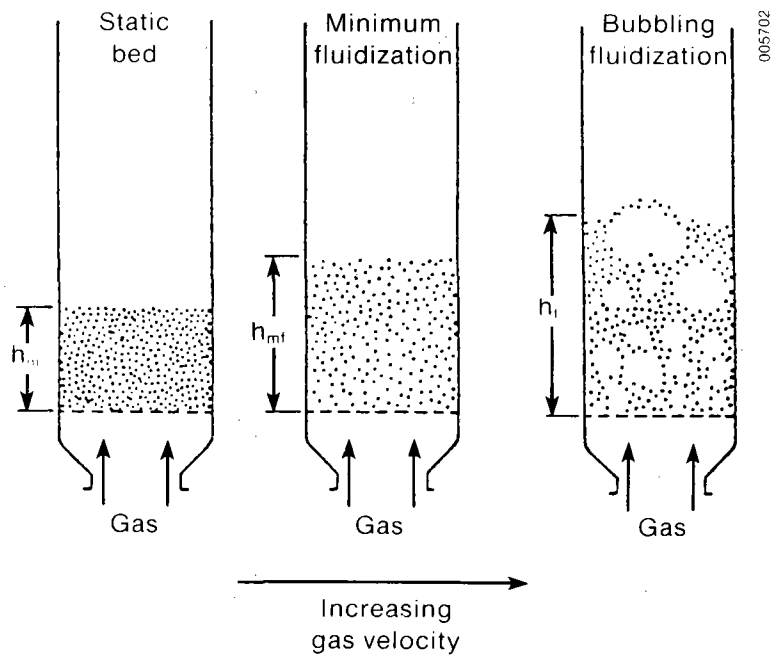
3.1.2 Fluidized-Bed Design

When the velocity of a gas passing upward through a bed of particles is gradually increased, the bed is first fluidized and then begins to bubble (see Figure 3-5). The minimum velocity for fluidization,  $u_{mf}$ (cm/s), given by Kunii and Levenspiel (1977), is:

$$\frac{1.75}{\phi_s \epsilon_{mf}^3} \left( \frac{d_s u_{mf} \rho_a}{\mu} \right)^2 + \frac{150(1 - \epsilon_{mf})}{\phi_s^2 \epsilon_{mf}^3} \left( \frac{d_s u_{mf} \rho_a}{\mu} \right) = \frac{d_s^3 \rho_a (\rho_s - \rho_a) g}{\mu^2}, \quad (3-23)$$

**Table 3-1. Operating Parameters of a Four-Stage Fluidized-Bed Heat Exchanger**

	Outlet pressure = 10 atm		
	Heat rate = 100 MW <sub>t</sub>		
	$\gamma = \dot{m}_a / \dot{m}_s = 0.51$		
	$\dot{m}_a = 111 \text{ kg/s}$		
	$\dot{m}_s = 217 \text{ kg/s}$		
	$d_{sh} = 7.15 \text{ m}$		
	<u>T<sub>s</sub> (°C)</u>	<u>T<sub>a</sub> (°C)</u>	<u>u<sub>o</sub> (cm/s)</u>
Inlet	1000	150	--
First stage (top stage)	581	581	67.2
Second stage	801	801	84.5
Third stage	914	914	93.4
Fourth stage (bottom stage)	971	971	97.9
Outlet	581	971	--



**Figure 3-5. Minimum and Bubbling Fluidization**

where

- $\phi_s$  = particle sphericity
- $\epsilon_{mf}$  = bed voidage at minimum fluidization
- $d_s$  = particle diameter (cm)
- $\rho_s$  = particle density (g/cm<sup>3</sup>)
- $\rho_a$  = air density (g/cm<sup>3</sup>)
- $\mu$  = air viscosity (g/cm s)
- $g$  = 981 cm/s<sup>2</sup>.

We assumed values of  $\epsilon_{mf} = 0.5$  and  $\phi_s = 0.9$ . (Particle sphericity is defined as the volume of the particle divided by the volume of a sphere having the same surface area as the particle.) From Section 1.0,  $d_s = 0.5$  mm and  $\rho_s = 4$  g/cm<sup>3</sup> for alumina. For a vigorously bubbling bed, Kunii and Levenspiel recommend that the operating air velocity  $u_o$  be at least twice the minimum fluidization velocity. Vigorous bubbling ensures good mixing and, thus, a uniform temperature in the bed. Kunii and Levenspiel also note that, for stable operation,  $u_o$  should be less than one-third of the particle terminal velocity  $u_t$  (cm/s):

$$u_t = \left[ \frac{4gd_s(\rho_s - \rho_a)}{3\rho_a C_d} \right]^{1/2}, \quad (3-24)$$

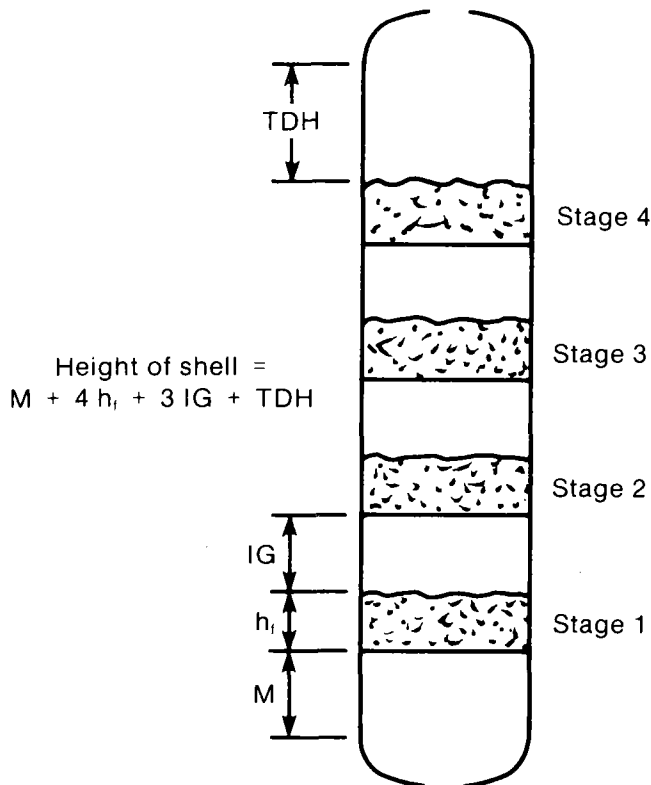
where the drag coefficient  $C_d = 10/Re^{1/2}$  and:

$$Re = \frac{d_s \rho_a u_t}{\mu}. \quad (3-25)$$

We determined velocities in the heat exchanger by setting the velocity at the top stage to  $1/3 u_t$  and checking the lower stages to verify that the bubbling criteria  $u_o = 2u_{mf}$  was met for each stage. The cross-sectional area of the heat exchanger was held constant for all stages. We then calculated the heat exchanger diameter of 7.15 m given the mass flow rate of air and the air velocity and density for the first stage.

Figure 3-6 is a schematic of the four-stage fluidized bed heat exchanger. The height of the heat exchanger is the sum of the transport disengaging height (TDH), the heights of the beds, the interstage gaps (IG), and the air inlet manifold (M). The TDH is an empty space above the uppermost bed of the heat exchanger. This height allows particles that have been thrown out of the bed by bubbles bursting at the surface to disengage from the air stream and fall back into the bed. The TDH is defined as the height at which the rate of decrease of entrainment of particles in the air stream approaches zero. Placing the outlets to the cyclones above TDH ensures that the air entering the cyclones has the least possible particle loading.

Bed height should be kept small since it does not affect the heat transfer but does influence the size of the heat exchanger. Ideally, experiments with the particles in question would determine the minimum stable operating height of the bed as well as the bed expansion during fluidization. The literature offers little guidance as to these quantities and none for the pressures and particles under consideration. A static bed depth  $h_m = 0.305$  m (1 ft) and an



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operating bed depth  $h_f = 0.61$  m (2 ft) were assumed. This operating height should be adequate to provide stable operation of the beds without making the heat exchanger excessively tall.

We assumed that the interstage gap was equal to the operating bed depth, which allows clearance between the bed and the grid above as the bed height fluctuates during operation. We allowed a height of 1 m for the air inlet manifold. Zenz (1983) correlates TDH with superficial velocity  $u_s = u_o - u_{mf}$  and bubble diameter. Assuming a bubble diameter of 15.24 cm (6 in.) and given a superficial velocity of 74 cm/s, the TDH is 1.52 m. Using the equation in Figure 3-6, total height of the heat exchanger shell  $h_{sh}$  (m) is:

$$h_{sh} = 1 + (4 \times 0.61) + (3 \times 0.61) + 1.52 = 6.8 \text{ m} \quad (3-26)$$

**Figure 3-6. Schematic Layout of Multistage Fluidized-Bed Heat Exchanger**

The pressure drop in a fluidized bed must include the drop in the bed and the drop through the grid. The

pressure drop in the bed  $P_b$  ( $N/m^2$ ) is simply the weight per unit area of particles in the bed:

$$P_b = h_m(1 - \epsilon_m)\rho_s g/10 ,$$

where  $\epsilon_m$  is the void fraction in the static bed. A pressure drop in each grid of at least 30% of the drop in the bed is recommended for air distribution to all parts of the grid (Zenz 1982). Thus, the pressure drop in the multistage fluidized-bed heat exchanger  $P_t$  is:

$$P_t = 1.3 \times 4 \times P_b = 37,340 \text{ N/m}^2 .$$

Entrance and exit losses to and from the heat exchanger have not been included.

### 3.1.3 Vessel Design

The heat exchanger is essentially an internally insulated pressure vessel with 2:1 ellipsoidal heads. Given the required height and diameter of the heat exchanger from the previous sections, we now can size the vessel.

To determine the required inner diameter of the shell, we must first calculate the thickness of the internal insulation. Ceramic firebrick was chosen for the internal insulation because it provides a rigid, durable inner wall for the vessel. The ceramic firebrick has a thermal conductivity,  $k_1$  of 0.17 W/m K and a cost of \$809/m<sup>3</sup> (Bohn 1983). The heat lost through 1 m<sup>2</sup> of this insulation is:

$$q = k_1 \Delta T / t_1, \quad (3-27)$$

where

$q$  = heat loss (W/m<sup>2</sup>)

$\Delta T$  = temperature difference (K)

$t_1$  = thickness of internal insulation (m).

The temperature difference is 684 K, which is the particle inlet temperature, 1000°C, minus the shell temperature 316 K. Assuming a cost of \$9/GJ for thermal energy, the value of the heat lost at a rate of 1 kW over a year (350 days of operation) is \$272. Over a 30-year life, the value of this heat loss will be \$272 times the present worth factor 9.427 (30 years, 10% interest), or \$2566/kW. Thus, the total cost of the insulation plus the cost of the lost heat  $C_t$  is:

$$C_t = t_1 \$809/m + \$2566/kW. \quad (3-28)$$

This equation was differentiated and set to zero,  $dC_t/dt_1 = 0$ , and solved for  $t_1$  giving a thickness of 0.6 m. Thus, the required shell diameter  $d_{sh}$  is the heat exchanger diameter plus twice the insulation thickness, or 8.35 m.

Peters and Timmerhaus (1980) give the required thickness of the shell  $t_{sh}$  (cm) of a pressure vessel.

$$t_{sh} = 2.54 \left[ Pd_{sh} / (2 SE_j - 1.2 P) + C_c \right], \quad (3-29)$$

where

$P$  = internal pressure (psig)

$d_{sh}$  = diameter of shell (in.)

$S$  = maximum allowable stress (13,700 psi at 650°F)

$E_j$  = joint efficiency = 1

$C_c$  = corrosion allowance = 0.125 in.

We assumed the same thickness for the heads, a reasonable approximation when  $P$  is much less than  $S$ . The weight of the shell is given by:

$$W_{sh} = \rho_{cs} \pi h_{sh} \left[ (t_{sh} d_{sh} / 100) + (t_{sh}^2 / 10,000) \right], \quad (3-30)$$

where

$W_{sh}$  = weight of the shell (kg)

$\rho_{cs}$  = density of carbon steel (7833 kg/m<sup>3</sup>)



$h_{sh}$  = height of shell (m)

$d_{sh}$  = inner diameter of shell (m).

The weight of an ellipsoidal head is given by:

$$W_h = \rho_{cs} \pi t_{sh} (1.23 d_{sh} + t_{sh}/100)^2 / 4 , \quad (3-31)$$

where

$W_h$  = weight of head (kg).

The total weight of the heat exchanger vessel  $W_t$  (kg), including an additional 20% for nozzles, manholes, etc., is:

$$W_t = 1.2(W_{sh} + 2 W_h) . \quad (3-32)$$

The capital cost of the vessel is based on this total weight plus the cost of insulation, both internal and external, and the cost of the grids for the fluidized beds. In the following section on costs, the grids will be treated as bubble cap trays using the cost method given by Peters and Timmerhaus (1980).

The cost of the insulation is based on the volume required. Equations for calculating these volumes are taken from Peters and Timmerhaus (1980). The volume of internal insulation required for the shell  $V_{lsh}$  ( $m^3$ ) will be:

$$V_{lsh} = \pi h_{sh} (t_1 d_{sh} + t_1^2) . \quad (3-33)$$

The volume required for an ellipsoidal head  $V_{lsh}$  ( $m^3$ ) is:

$$V_{lh} = \pi t_1 (1.23 d_{sh} + t_1)^2 / 4 . \quad (3-34)$$

The total volume of internal insulation  $V_l$  ( $m^3$ ) is:

$$V_l = V_{lsh} + 2 V_{lh} . \quad (3-35)$$

To find the thickness of external insulation, the heat flux through the wall of the vessel is calculated:

$$q = k_1 \Delta T / t_1 , \quad (3-36)$$

where

$q$  = heat flux ( $W/m^2$ )

$\Delta T$  = temperature difference ( $684^\circ C$ ).

We then use this flux to calculate the required thickness of the external fiberglass insulation  $t_2$  (m):

$$t_2 = k_2 \Delta T / q . \quad (3-37)$$

The temperature difference,  $\Delta T$ , for this calculation was the shell temperature,  $316^\circ C$ , minus the ambient temperature,  $30^\circ C$ . The thermal conductivity of the fiberglass insulation  $k_1$  was assumed to be  $0.4 W/m K$ . We calculated a

value of 0.05 m for  $t_2$ . We calculated the total volume of the external insulation using the same equations as for the internal insulation.

For the aluminum lagging, we calculated the required surface area  $A_1$  ( $m^2$ ) as follows:

$$A_1 = \pi h_{gh} d + 2.17 d^2, \tag{3-38}$$

where  $d = d_{sh} + 2(t_2 + t_{sh}/100)$ .

Figure 3-7 shows the major dimensions and the stage temperatures for the heat exchanger.

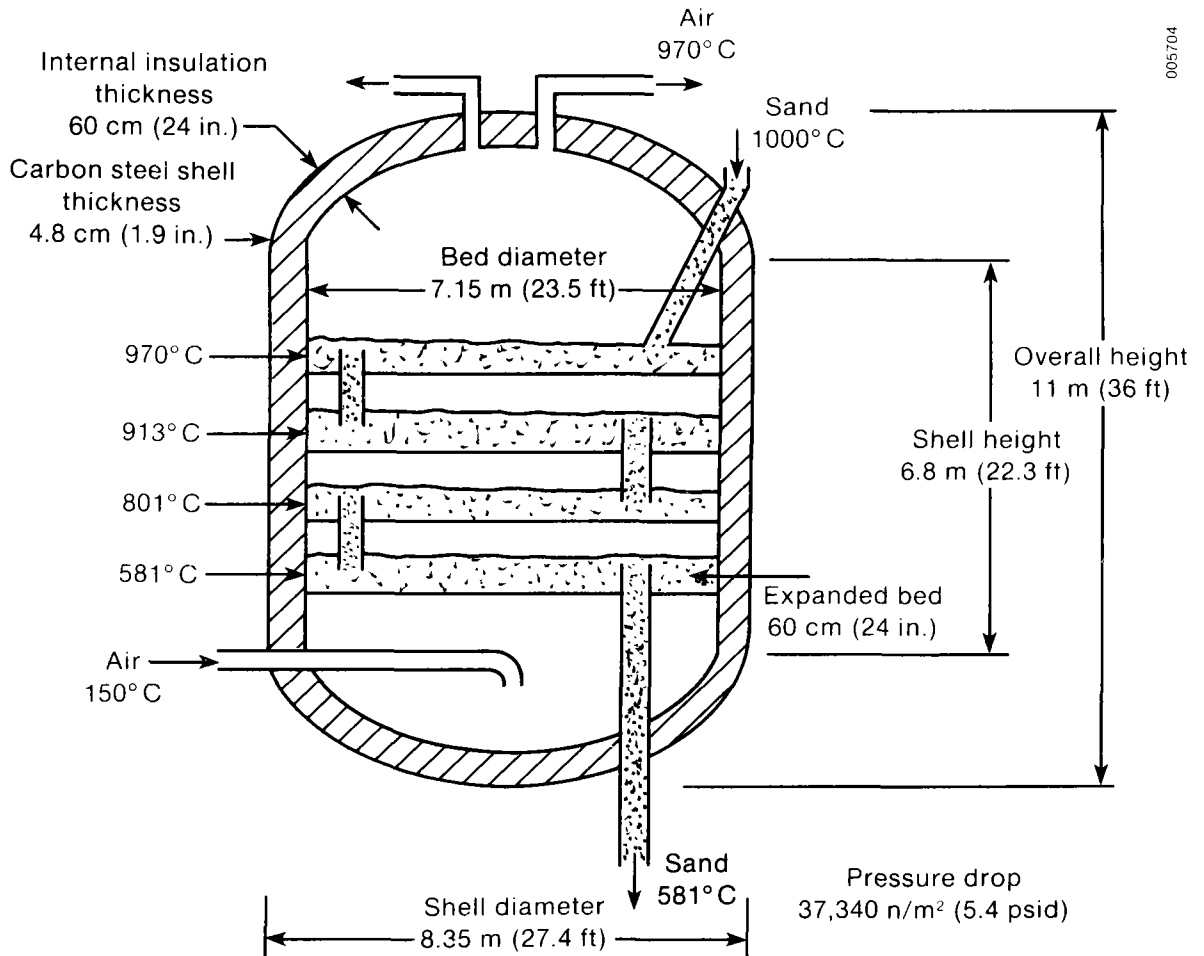


Figure 3-7. Schematic of Four-Stage Fluidized Bed

### 3.2 Feeders and Defeeder

The lockhoppers and buffer storage vessels are pressure vessels with internal insulation. They each have a shell with an aspect ratio of 2:1, height to diameter, and the heads are 2:1 ellipsoidal heads. The feeder lockhoppers go through a four-stage cycle. First, the upper valve is opened and the lockhopper is filled with hot particles. Next, the upper valve is closed and the lockhopper is pressurized. Third, the bottom valve is opened and the particles are discharged. And fourth, the bottom valve is closed and the lockhopper is depressurized. The defeeder lockhopper cycle is similar except the discharge step is at ambient pressure.

There is a trade-off between lockhopper size and the number of cycles required per unit time. We prefer that a low cycle rate be used to reduce wear on the lockhopper valves. We chose a 15-minute cycle time to determine the required lockhopper volume, which results in 4 valve cycles per hour and 40 cycles for a 10-hour day. We further assumed that 45% of the cycle time was for charging, 45% was for discharging, and the remaining 10% was for cycling of valves and pressurization or depressurization. As mentioned in Section 2.0, two lockhoppers handle the required particle flow in both the feeder and defeeder; the spare lockhoppers are available for valve maintenance or simply held in reserve.

Using these assumptions and the particle volumetric flow rate, we determined the valve size and lockhopper volume. The mass flow rate of 217.4 kg/s was given in the previous section. Alumina particles have a particle density of 4 g/cm<sup>3</sup>. Assuming a void fraction  $\epsilon_m$  of 0.4, the particle bulk density is 2.4 g/cm<sup>3</sup> and the volumetric flow rate is 0.09 m<sup>3</sup>/s. The lockhopper valves must be oversized by 10% to pass one-half the required flow rate while open only 45% of the time. The lockhopper volume must be sufficient to accept this flow rate of particles for 45% of 15 minutes, or 6.75 minutes. The feeder and defeeder buffer storage vessels are sized for twice the volume needed to contain the 0.14 m<sup>3</sup>/s flow for 1.5 minutes (10% of 15 minutes).

We applied similar assumptions to the cyclone defeeders. The particle flow rate from the first-stage cyclone was assumed to be 1% of the heat exchanger flow rate. For the second-stage cyclone, a particle flow rate of 0.025% of the heat exchanger flow rate was assumed. These flow rates are generous and will lead to adequate defeeder capacity regardless of cyclone performance. Only one of the first-stage cyclone lockhoppers is used at any time. The second is held in reserve. Thus, these lockhoppers are the same size as the first-stage buffer storage vessel. The second-stage buffer storage vessel must be sized so that it need only be emptied once per 10-hour day. We found a vessel identical in size to the first-stage vessels to be adequate.

We assumed that the required volume for all of these vessels was contained within the shell alone. The heads add less than 20% additional volume, which will be allowed as ullage. We used the same methods as in the previous section on the heat exchanger to determine the thickness and volume of insulation

and the size and weight of the various vessels required for the feeders and defeeders. The only difference is that less insulation is required in the defeeders because of their lower operating temperature of 580°C. Using the same method described previously to calculate the most economical thickness of insulation, the internal insulation thickness for the defeeders is 37 cm and the thickness of external insulation is 12 cm. Table 3-2 gives the major dimensions and weight of each of the vessels.

In some lockhopper applications, vent gas losses are a significant operating cost. For the DCHX, the volume of gas lost in the operation of the feeders and defeeders is approximately the same as the volumetric flow rate of solids. The volumetric flow rate of air through the heat exchanger is over 100 times larger than the volumetric flow rate of solids. Thus, the vent gas losses are small and no accounting of them is made in this analysis.

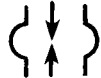


### 3.3 Lockhopper Valves

Table 3-3 summarizes the service conditions for the lockhopper valves required for the DCHX. These valves must handle high-temperature abrasive solids while providing a pneumatic seal for the lockhoppers. Table 3-4 shows the relative hardness of various solids media and valve materials. The hardness of alumina relative to that of the alloys indicates the problem of abrasion in this type of valve. The ceramic materials that have the required hardness are not commonly used in commercially available valves. The capability of a valve in this type of service can be expressed as some combination of the three inter-related parameters of temperature, pressure, and life time (number of cycles before service is required to maintain acceptable leak rates).

**Table 3-2. Dimensions and Weights of the Feeder and Defeeder Vessels**

Vessel	Operating Pressure (atm)	Quantity	Shell Diameter (m)	Overall Height (m)	Weight (kg)
Feeder buffer storage	1	1	3.4	6.0	6,280
Feeder lockhoppers	10	3	4.2	8.0	28,800
DCHX buffer storage	10	1	3.4	6.0	14,920
Defeeder buffer storage	10	1	2.9	5.8	10,820
Defeeder lockhoppers	10	3	3.7	7.8	22,240
Cyclone lockhoppers and buffer storage	10	4	1.8	2.2	1,930

Table 3-3. Lockhopper Valve Service Conditions

Application	Configuration	Temperature of Solid Particles (°C [°F])	Pressure (atm)
Feeders to DCHX	solids flow  pressure	1000 (1830)	10
Defeeders from DCHX	pressure solids flow  pressure	600 (1100)	10
Defeeders from cyclones	pressure solids flow 	1000 (1830)	10

The DOE Morgantown Energy Technology Center began a program in 1976 to test state-of-the-art lockhopper valves and to develop prototype valves capable of operating under more severe conditions than the state-of-the-art valves. Their assessment of the capabilities of state-of-the-art valves as of 1982 was 15,000 cycles at  $1.38 \times 10^6 \text{ N/m}^2$  (200 psi) and  $540^\circ\text{C}$  ( $1000^\circ\text{F}$ ) (DOE 1983). Prototype valves were tested at much higher pressures and temperatures with materials such as silicon carbide and alumina. The final report on those tests is due in 1985.

Discussions with representatives of valve companies reveal similar assessments of the state of the art (personal communications with Kamy-Neles Inc., Mogas Industries Inc., and Everlasting Valve Co.). Temperature limits of  $650^\circ$  to  $760^\circ\text{C}$  ( $1200^\circ$  to  $1400^\circ\text{F}$ ) are considered reasonable for solids-handling valves. Valve seat materials are commonly noted as a limiting factor. Valves have been supplied to the petroleum industry for handling alumina-based catalysts at high temperature and pressure. Costs in the range of \$35,000 to \$65,000 for 6-in. valves were suggested as typical for this type of application.

The valves required for the DCHX defeeder lockhoppers can be considered state of the art. Valves for the feeders and cyclone defeeders will require development but appear to be feasible. The valves are sized according to the equation given by Zenz (1962) for the flow of solids into an orifice:

$$W_s = 1.2 \rho_s D^{1/2} , \tag{3-39}$$

where

$$\rho_s = \text{solids bulk density (lb/ft}^3\text{)}$$

Table 3-4. Relative Hardness of Solids Media and Hard-Facing Materials

Material	Equivalent Vickers Hardness Number (VHN)
<b>Solids media</b>	
Coal <sup>a</sup>	<40
Limestone	110 - 130
Dolomite	130 - 150
Fused ash	800 - 2000
Aluminum oxide	1800 - 2100
<b>Hard-facing alloys</b>	
316 Stainless steel	160 - 290
Stellite No. 6	400
Stellite No. 1	580
Haynes No. 40	630
Tribaloy T-800	650
METCO 19-E	600 - 700
<b>Cermet and ceramic materials</b>	
Silicon nitride	1400
Tungsten carbide	1600 - 1750
Silicon carbide	1900 - 3300
Boron carbide	3000
Tungsten titanium diboride over tungsten carbide (TMT-745)	≈5000

<sup>a</sup>This is for carbonaceous material and is not representative of siliceous and other common mineral inclusions. The hardness on these ranges from 100 to over 1000.

Source: DOE 1983.

D = orifice diameter (in.)

$W_s$  = solids efflux rate (lb/s ft<sup>2</sup>).

Valve sizes have all been rounded to the next largest even size in inches according to standard industry practice. Based on the particle flow rates determined above, the feeder and defeeder lockhopper valves and the flow control valve are all 12-in. valves while 2-in. valves are needed for the cyclone defeeder.

### 3.4 Cyclones

This section describes the method used to calculate the performance of the cyclones that remove small particles from the fluidized-bed heat exchanger outlet air before the air passes to a turbine or an industrial process.

First, we must describe the particles leaving the fluidized bed. As a baseline, we have chosen a nominal particle size of 500  $\mu\text{m}$  in the bed itself. We assume that through attrition, these particles will be ground down producing a distribution of smaller particles. The largest of these particles will remain in the fluidized bed because the operating gas velocity is chosen somewhat below the terminal velocity of 500  $\mu\text{m}$  particles. Smaller particles will be carried over into the exhaust stream and must be removed before leaving the system. For example, if the bed operates at 10 atm, the terminal velocity for the 500- $\mu\text{m}$  particles is 269 cm/s (assuming a particle density of 4 g/cm<sup>3</sup>). Under these conditions the minimum fluidization velocity is 36 cm/s, and if we choose an operating velocity three times the minimum fluidization velocity we get 108 cm/s. The particle diameter for which 108 cm/s is a terminal velocity is approximately 200  $\mu\text{m}$ ; that is, particles smaller than about 200  $\mu\text{m}$  will be carried out of the fluidized bed at an operating velocity of 108 cm/s. Larger particles will remain in the fluidized bed.

There is no sure way of predicting the loading and size distribution of fines that might be generated in a central receiver plant. Clearly the probability of a particle existing should increase with the particle diameter since we assume that the small particles result from grinding of larger particles. A simple particle-size distribution that satisfies this criterion is the Gates-Gaudin-Schumann distribution, which is:

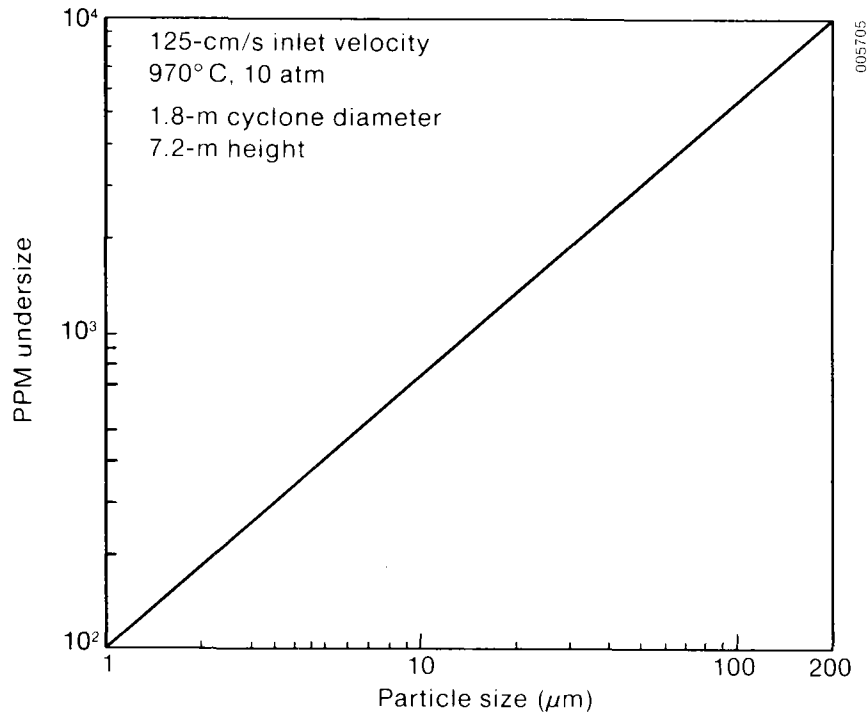
$$\log L = b + a \log d , \quad (3-40)$$

where L is the quantity of particles with diameters less than d in parts per million (ppm) of mass. We can determine the constants a and b from the largest diameter in the sample and, for example, the diameter below which 1% of the mass exists. In the overall system analysis, we will let the largest particle diameter entering the cyclone be determined by the fluidized bed operating velocity, as calculated above. We will arbitrarily set the 1% point at 1  $\mu\text{m}$ .

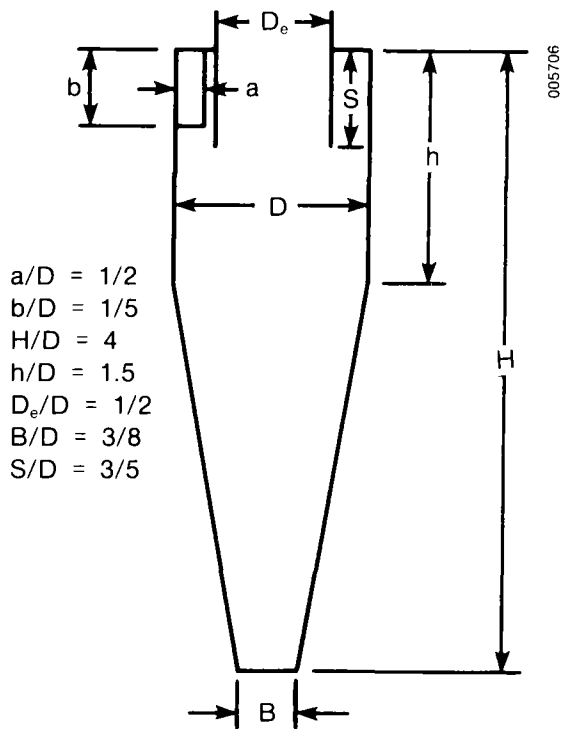
Lastly, we must choose the total loading of particles elutriated from the fluidized bed. For the study, we assume that 1% (10,000 ppm) of the total particle flow is carried over into the cyclones. This is surely a worst case since in 100 passes through the DCHX, a mass of particles equivalent to the entire plant inventory would be carried into the cyclones. The assumed distribution of elutriated particles is a straight line on a log-log plot, as shown in Figure 3-8.

Next, we must prescribe the desired exit air quality in terms of particle loading. The best analysis of the state of the art of turbine technology is that of Boericke et al. (1980) based on turbine tests with various dusty gases. They recommend keeping the total loading below 100 ppm (based on the mass of the air flow) with 98% of the particles smaller than 10  $\mu\text{m}$ .

A cyclone removes particles from gas streams by centrifugal force. The particle-laden gas stream enters a cylindrical vessel tangentially and the particles are thrown to the outer wall by centrifugal force, slide down the wall, and are collected by a conical bottom. The gas exits through a central opening in the top of the cyclone. Figure 3-9 shows a cyclone with typical dimensional ratios. Since centrifugal force is the separation mechanism, larger particles are more efficiently removed from the gas stream than are



**Figure 3-8. Size Distribution of Particles Carried over from the DCHX Expressed as ppm of the Total Mass Flow Rate of Solids**



**Figure 3-9. Cyclone with Typical Dimensional Ratios**

smaller particles. Other mechanisms are apparently at work at the high pressure and temperature at which these cyclones operate. As shown by Parker et al. (1981), classical cyclone efficiency correlations fail at high pressure and temperature. Typically, high pressure increases cyclone efficiency and high temperature reduces cyclone efficiency. Parker has developed a correlation based on high-pressure and high-temperature data (pressure up to 20 atm and temperature up to 693°C) in a 15-cm diameter cyclone, and it is upon this correlation that we will base our cyclone efficiency. Some of the data presented by Parker suggest that cyclone efficiency is reduced by increasing the cyclone size, but at the present time there is no way to estimate this effect. This presents one source of uncertainty in using Parker's correlation.

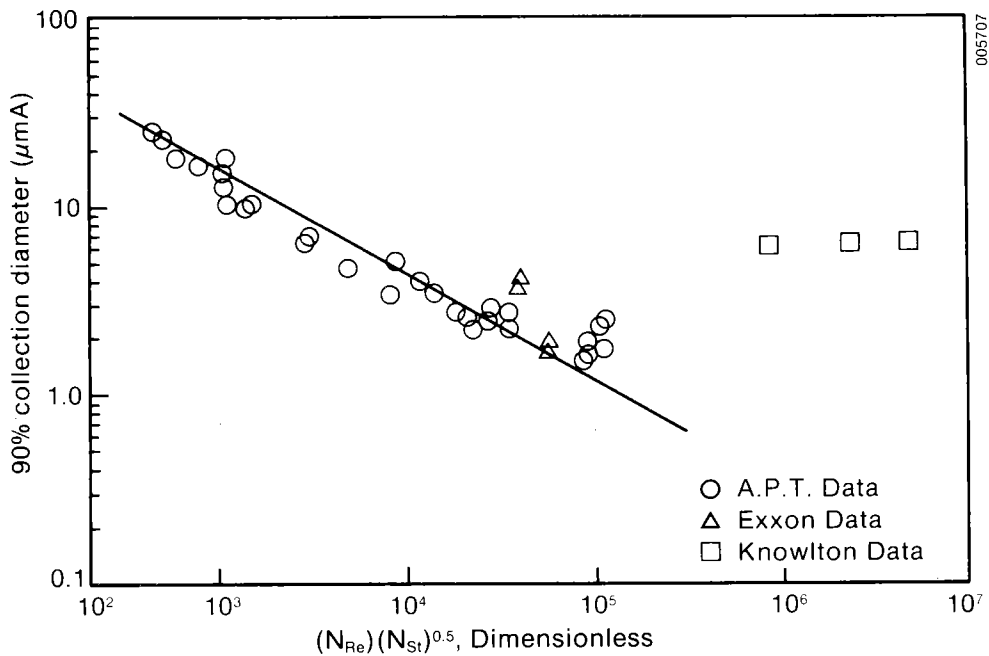


The Parker correlation, Figure 3-10, presents a 90% collection diameter versus a dimensionless parameter constructed from the cyclone Reynolds number and the Stokes number:

$$d_{90\%} = f(\text{Re} \times \text{Stk}^{1/2}) . \quad (3-41)$$

The data follow a straight line on a log-log plot decreasing from 30 to 2 μm as the abscissa increases from 300 to 100,000. The only data beyond that value of the abscissa are the data of Knowlton and Backhorchin (1978), which give a constant 90% diameter of 6.4 μm for abscissa values greater than 10<sup>6</sup>. The jump in 90% diameter near abscissa values of 100,000 has not been explained in the literature according to one of the authors of the Parker paper, but the jump may be caused by Knowlton and Backhorchin's larger cyclone (100 mm versus 50 mm for Parker) or because Knowlton and Backhorchin only ran at ambient temperatures. At any rate, the discrepancy occurs near our operating point and thus creates an uncertainty in collection efficiency. Because of this uncertainty, we will evaluate two cases. The liberal case will be based on the straight line shown in Figure 3-10. The conservative case will assume a constant 90% diameter of 6.4 μm.

The 90% collection diameter must be related to an efficiency-versus-diameter curve so that we may specify the cyclone inlet particle-loading distribution and predict the outlet distribution. To do this we refer to Parker's data for combined high pressure and temperature. We will fit a straight line from the 90% diameter efficiency to the 0,0 point:



Source: Parker, Jain, and Calvert 1981.

Figure 3-10. Cyclone Performance at High Temperature and Pressure

$$\eta = (d/d_{90})^{0.9} \quad d < d_{90} , \quad (3-42)$$

where  $\eta$  = collection efficiency.

The efficiency curves level out for diameters greater than the 90% diameter, and from Parker's data it is difficult to prescribe a curve shape. The shape of the curve beyond the 90% diameter is very important because a substantial fraction of the inlet particles will be in this range, and the choice of curve shape beyond the 90% diameter strongly affects effluent distribution. The best data available for this purpose are from the commissioning test of the pressurized fluidized-bed coal combustion facility at Grimethorpe, England (National Coal Board 1983). That operation ran at a pressure and temperature similar to our operation, and the particle distribution and loading were also close (mass mean particle diameter was approximately 100  $\mu\text{m}$  and loading was approximately 18,000 ppm). The data shown in Figure 3-11 give efficiency versus diameter and go well beyond the 90% diameter that was 5.62  $\mu\text{m}$ . The data go out to the 99+% diameter and with slight extrapolation, one can project the 99.9% diameter to be 31.6  $\mu\text{m}$ . A good representation of the Grimethorpe data beyond the 90% diameter is:

$$\begin{aligned} \eta &= 1 - 10^{-[1+2.666 \log(d/d_{90})]} \\ &= 1 - 0.1(d/d_{90})^{-2.666} . \end{aligned} \quad (3-43)$$

Equations 3-41 and 3-42 will be used to generate efficiency-versus-diameter curves given the 90% diameter.

Figures 3-12a and b show the predicted cyclone performance based on the preceding assumptions. Results for both the liberal and conservative assumptions for 90% collection efficiency diameter are given. With the liberal assumption, one stage is more than adequate to meet the goal of 100-ppm total loading. Using the conservative assumption, two stages are needed to reach that goal.

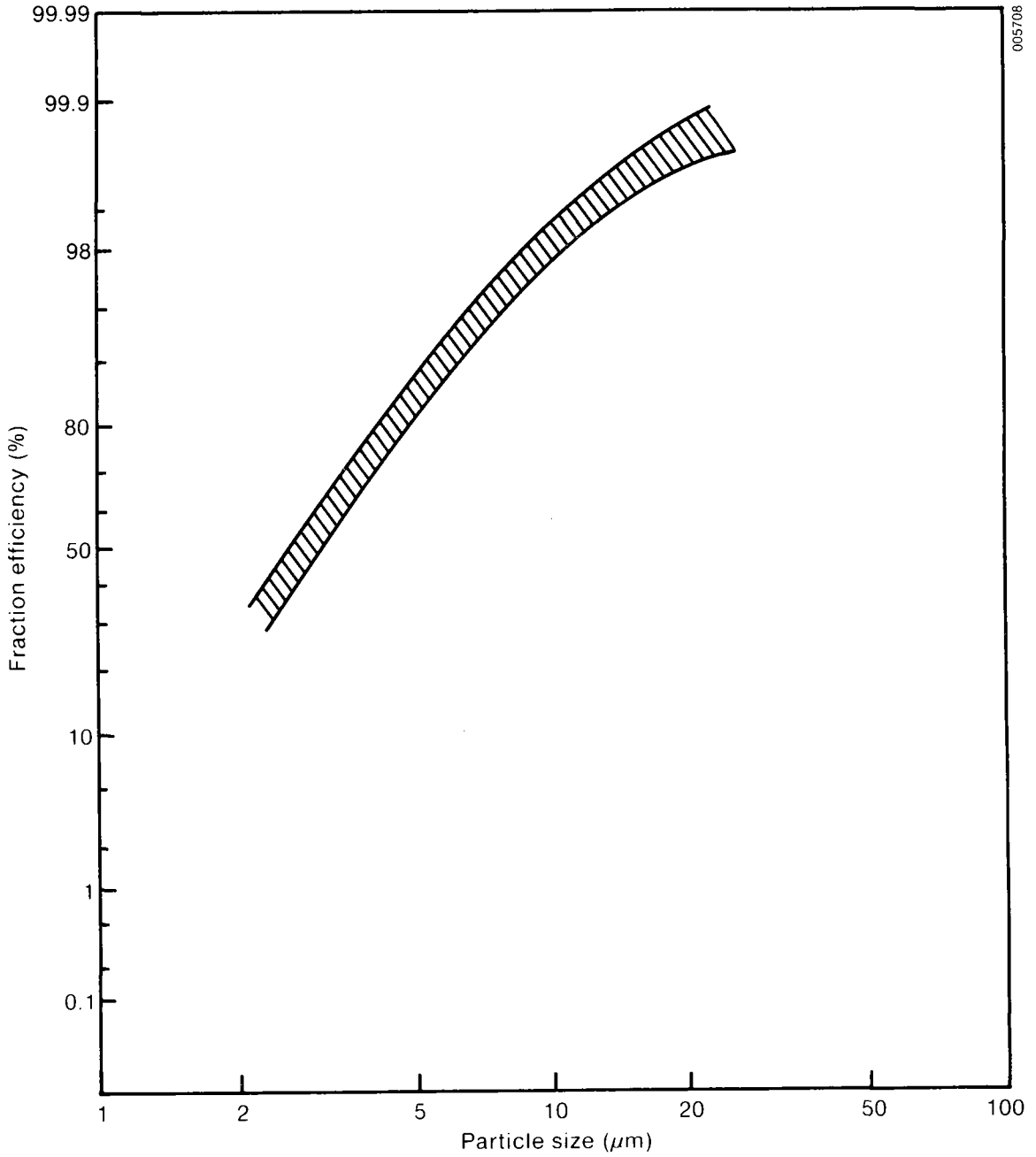
The cyclone pressure drop may be estimated from an equation recommended by Leith and Mehta (1973):

$$\Delta p = \frac{U_c^2 \Delta H}{2} \rho_a , \quad (3-44)$$

where

$$\begin{aligned} \Delta p &= \text{pressure drop (N/m}^2\text{)} \\ U_c &= \text{air inlet velocity (m/s)} \\ \Delta H &= 16 ab/D_e^2 \text{ (refer to Figure 3-9)} \\ \rho_a &= \text{air density (kg/m}^3\text{)}. \end{aligned}$$

For the design and cost of the DCHX system, we obtained a vendor quote for cyclones operating at 970°C and 10 atm from Aerodyne Development Corp. The quote called for 5 units per stage with a capacity of 9.4 m<sup>3</sup>/s (20,000 cfm) each and a pressure drop of 1.5 kPa (0.217 psi). The cyclones were internally insulated and lined. Assuming that two stages of cyclones are required, 10 units total will be included in the DCHX system.



Source: National Coal Board 1983.

**Figure 3-11. Cyclone Fraction Efficiency**

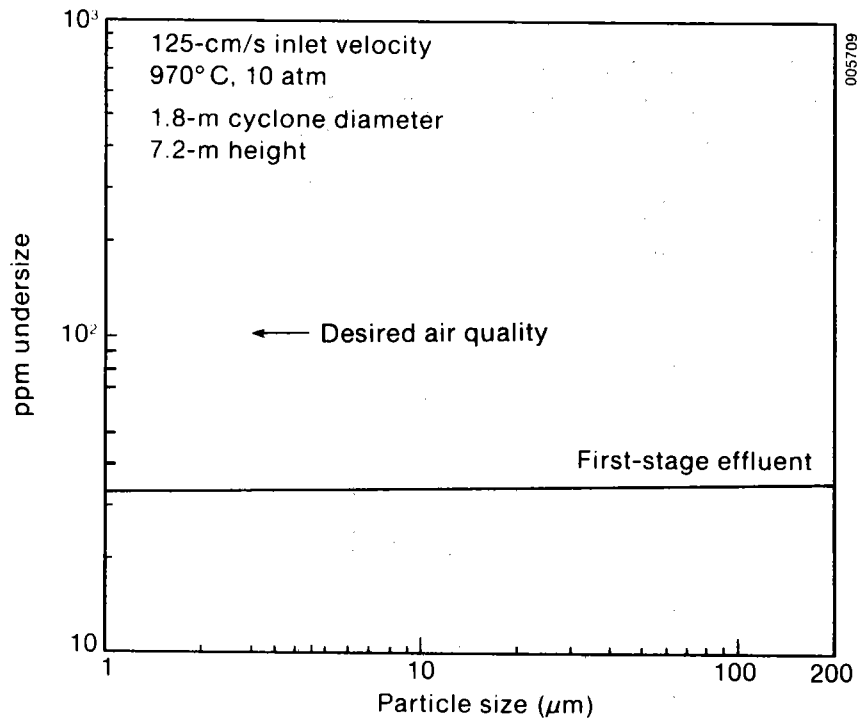


Figure 3-12a. Cyclone Performance Based on the Liberal Assumption for the 90% Collection Efficiency Diameter

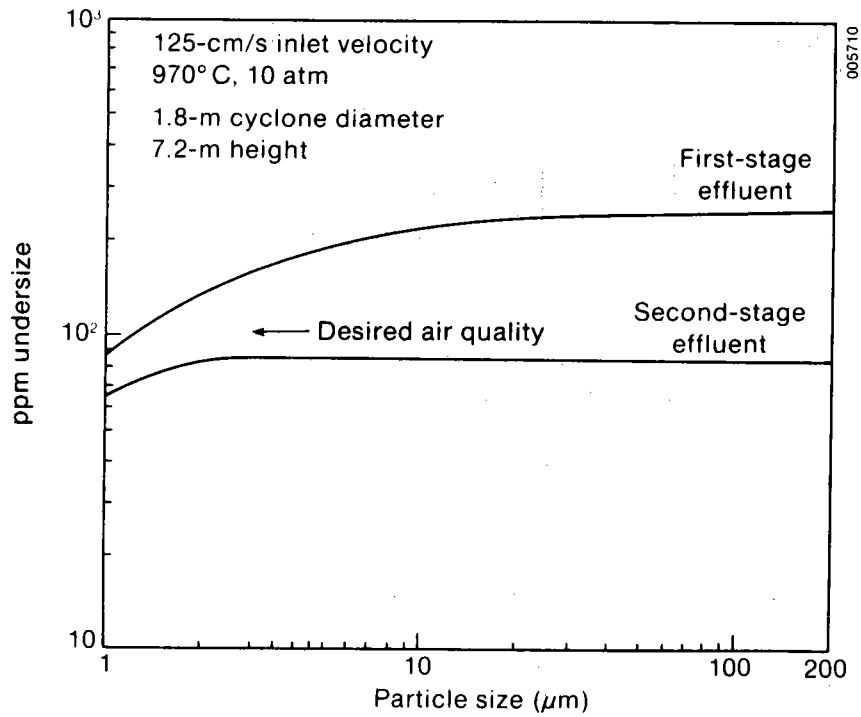


Figure 3-12b. Cyclone Performance Based on the Conservative Assumption for the 90% Collection Efficiency Diameter

### 3.5 Ducting and Piping

The ducting from the outlets of the heat exchanger and the cyclones will be internally insulated and internally shrouded. The internal insulation maintains a temperature that keeps the walls of the ducts structurally sound, and the internal shroud prevents contamination of the air stream that is caused by spalling of the refractory insulation. We evaluated the cost and performance of this type of ducting for the pressurized fluidized-bed combustion of coal (General Electric 1978). Researchers successfully tested a section of ducting up to 1000°C (1850°F) with transients as high as 400°C/h (700°F/h). Although the tests were performed at ambient pressure, the ducting is designed to deliver hot pressurized gases to gas turbines. Ducting with a 36 in. inside diameter was priced at \$2300/ft in 1978 dollars. Tees and elbows in the same size were priced at \$33,000 apiece. For this study, the cost of the ducting was assumed to vary linearly with diameter; the diameter was sized for 100-ft/s air velocities.

The balance of piping and ducting for the heat exchanger was costed at 4% of the total installed capital cost (Peters and Timmerhaus 1980, p. 171). This is a typical value for a solids-processing plant.

## 4.0 ECONOMIC ANALYSIS

### 4.1 Methodology

The cost of the DCHX system is expressed as an annual levelized cost (ALC). This is the constant annual cost (in fixed dollars) that, if paid over the lifetime of the heat exchanger, would have a present value equal to the present value of the actual costs incurred over the lifetime of the heat exchanger. The actual costs include both capital costs and annually recurring operating and maintenance costs. The costing methodology for SERI's Solar Energy Storage Program detailed in Appendix A is used to calculate the ALC from the capital and annual costs. Parameters used in the calculation include:

Discount rate--10%  
Lifetime--30 yr  
Corporate tax rate--50%  
First year of operation--1990  
General inflation--6%  
Escalation rate for capital costs--6%  
Escalation rate for annual costs--6%.

Only one capital cost (CC) is considered, the cost of the original purchase and installation. The annually recurring costs (AC) include both an operating and maintenance (O&M) cost and the cost of the pumping power to overcome the pressure drop in the heat exchanger and cyclones. Given these assumptions and the method in Appendix A, the ALC is expressed as:

$$ALC = 0.2228 CC + 1.886 AC . \quad (4-1)$$

All costs are in 1981 dollars. The DCHX cost is also expressed as the cost per unit of energy transferred  $ALC/Q$  where  $Q, MWh$  is:

$$Q = 8760 C_f (100 MW_t) = 350,400 MWh_t , \quad (4-2)$$

where 8760 is the number of hours per year and the capacity factor  $C_f$  is assumed to be 0.4, which implies 10 hours of operation per day.

A costing methodology used in the Solar Thermal Technology Program will also be used to facilitate comparison to the Solar Thermal cost goal of \$8.52/GJ (\$9.00/10<sup>6</sup> Btu) for thermal energy delivered from a solar central receiver (Williams 1985). For this method, the ALC is expressed as:

$$ALC = 0.1766 CC + 1.0 AC .$$

In the following text, the Solar Thermal cost methodology will be specifically noted wherever it is used. In all other cases, the Storage Program methodology is used.

## 4.2 Capital Costs

The valve costs suggested by vendors (Section 3.3) were \$35,000-\$65,000 for 6-in. valves or \$6,000-\$11,000 per inch of inner diameter. These state-of-the-art valves are suitable for the DCHX defeeder valves, and a cost of \$10,000 per inch is assumed. A higher cost of \$15,000 per inch is used for the feeder and cyclone defeeder valves.

For the lockhopper and buffer storage vessels, we use a method given by Peters and Timmerhaus (1980) to calculate the cost of a pressure vessel based on the weight  $W$  (lb) of the vessel. The cost in 1979 dollars is given as:

$$$/lb = 50 W^{-0.34} \quad (4-3)$$

This equation is applicable to vessels up to 100,000 lb, which is heavier than any of the lockhopper or buffer storage vessels. These costs are increased by a factor of 4, the Lang Factor, to account for delivery and installation (Peters and Timmerhaus 1980). Added to the cost of the vessel is the cost of insulation, both internal and external. The installed costs are (Bohn 1983):

Ceramic firebrick--\$809/m<sup>3</sup>  
 Fiberglass--\$265/m<sup>3</sup>  
 Aluminum lagging--\$25/m<sup>2</sup>.

The total cost, vessel and insulation, was converted to 1981 dollars assuming 6% inflation.

The DCHX vessel was costed in the same manner with two exceptions. First, the vessel weighs over 100,000 lb. At 100,000 lb, the equation gives a cost of \$1/lb (\$2.203/kg). This was the base cost used for the vessel. Second, the cost of the grids for the fluidized beds was added to the vessel cost:

$$\text{cost of grids} = (\$431/m^2)4 \left( \frac{\pi d_{sh}^2}{4} \right) \quad (4-4)$$

Peters and Timmerhaus (1980) recommend this equation for the cost of bubble cap trays.

The vendor quote on the cyclones was \$300,000 per unit in 1981 dollars. With 2 stages of cyclones and 5 cyclones per stage, the total cost with the Lang Factor is  $\$12 \times 10^6$ . In 1978 dollars, General Electric (1978) gives costs of \$2300/ft for the internally insulated and shrouded ducting at the outlet of the DCHX and the cyclones and \$33,000 a piece for tee and elbow fittings, all with 36-in. inner diameter. These costs are equivalent to \$82.50/cm of inner diameter (ID) per meter for ducting and \$361/cm of ID for the fittings (tees and elbows), both in 1978 dollars (see also Section 3.5). The balance of piping in the system was taken as 4% of the total capital cost. As before, all costs not in 1981 dollars were converted using an inflation rate of 6%.

## 4.3 Annual Costs

The annually recurring costs for the DCHX are O&M costs and auxiliary power costs. Battleson (1981) estimates the O&M cost of a solar central receiver power plant as 2% to 3% of the capital costs. This agrees with the EPRI

Technical Assessment Guide (1978), which gives the O&M cost for atmospheric fluidized-bed combustion of coal. Excluding the consumables (limestone for desulfurization), the cost was 3% of the total capital cost. We expect the DCHX to have higher maintenance costs because of its high operating temperature and because the particles are very abrasive. The lockhopper valves, in particular, will be more costly to maintain than conventional valves. In chemical processing plants, maintenance costs alone are usually above 3% with 5%-9% considered average and 10% or more possible under severe operating conditions (Peters and Timmerhaus 1980). For the annual O&M cost, a value of 6% of the total capital cost is assumed.

The auxiliary power cost is based on the pumping power required to overcome the pressure drop in the heat exchanger and the cyclone. The power required to bring the air to the delivery pressure of 10 atm is not included. Given the total pressure drop in the system,  $P_d$  in  $N/m^2$ , the pumping power is given by:

$$W = \frac{P_d m_a}{\rho_a \eta_c \eta_m 10^3}, \quad (4-5)$$

where

$W$  = pumping power (kW)

$m_a$  = mass flow rate of air (kg/s)

$\rho_a$  = density of air ( $kg/m^3$ )

$\eta_c$  = compressor efficiency = 0.7

$\eta_m$  = motor efficiency = 0.96 .

Assuming a cost of electricity  $C_m$  in 1990 of \$0.0464/kWh (in 1981 dollars) as recommended in Appendix A, the annual cost of the auxiliary power  $AC_m$  is:

$$AC_m = W C_f C_m 8760 . \quad (4-6)$$

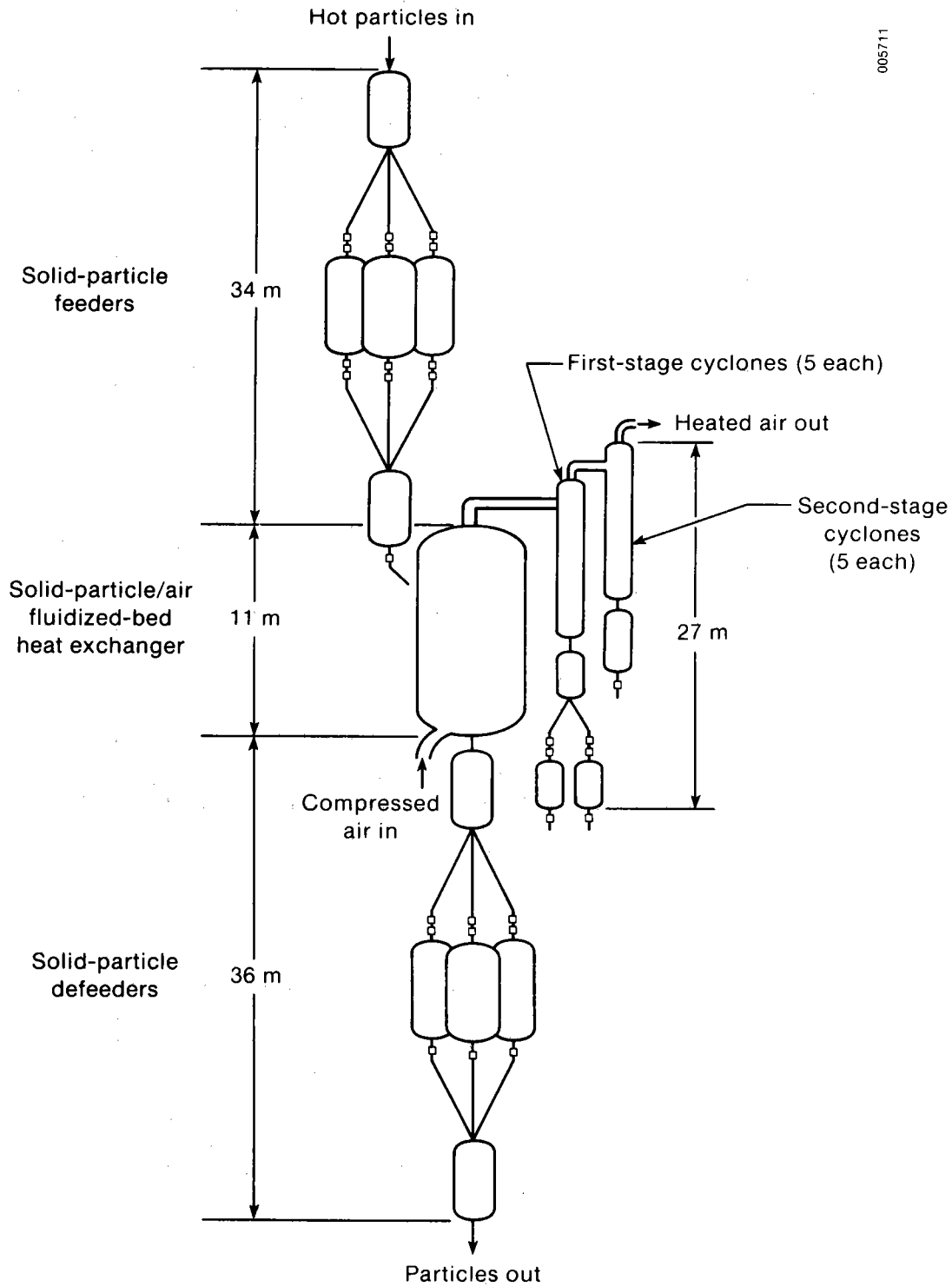
#### 4.4 Results

Figure 4-1 shows the complete DCHX system. It has an overall height of 81 m, only 11 m of which is the DCHX. Most of the height is made up of the numerous feeder and defeeder vessels. There are, altogether, 24 pressure vessels in addition to the DCHX. The height of the system presents a construction problem in itself. The system should be installed as part of the receiver tower, if possible, to avoid the additional cost of a superstructure to support the various vessels.

Table 4-1 summarizes the system costs and shows a cost per unit of delivered energy of \$6.66/GJ. Most of the system cost is in the solids-handling equipment and not in the heat exchanger itself. The feeders and defeeders alone have a capital cost more than three times that of the DCHX. The cyclones cost



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**Figure 4-1. Solid-Particle/Air Direct-Contact Heat Exchanger System Schematic**

Table 4-1. Direct-Contact Heat Exchanger Costs in 1981 Dollars

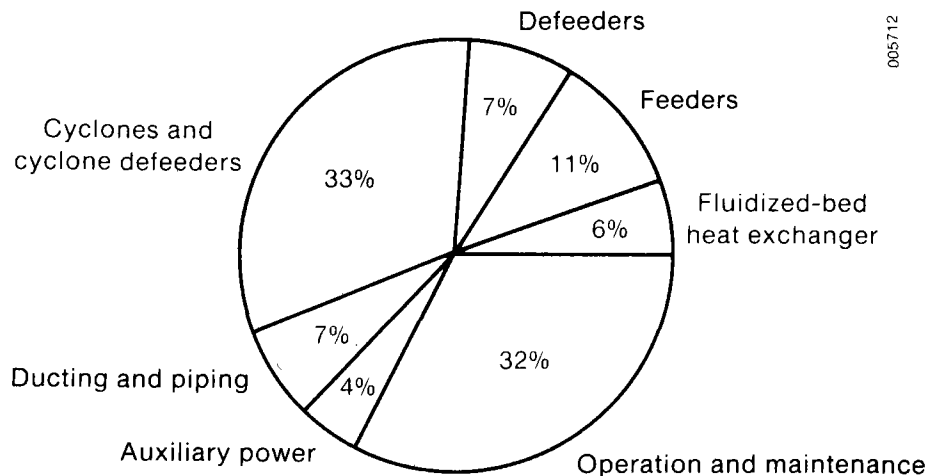
	Total (10 <sup>6</sup> \$)	Annual Levelized (10 <sup>6</sup> \$)
Capital investment		
Fluidized-bed heat exchanger	2.16	0.48
Feeders	4.29	0.96
Defeeders	2.55	0.57
Cyclones	12.0	2.67
Cyclone defeeders	0.48	0.11
Ducting	1.59	0.35
Piping	0.92	0.21
Total capital investment	<u>24.00</u>	<u>5.35</u>
Annual costs		
Heat exchanger auxiliary power	0.17	0.32
Cyclone auxiliary power	0.01	0.02
Operation & maintenance	1.44	2.72
Total annual costs	<u>1.62</u>	<u>3.06</u>
Total annual levelized cost		8.41
Annual levelized cost per unit of energy transferred		0.024 \$/kWh 6.66 \$/GJ 7.04 \$/10 <sup>6</sup> Btu

nearly six times as much as the DCHX. The pie chart in Figure 4-2 more clearly shows how the capital and annual costs contribute to the ALC. The cost of the valves is 61% of the feeder total cost, 48% of the defeeder cost, and 49% of the cyclone defeeder cost.

Using the Solar Thermal Technology Program's cost methodology, the DCHX cost is \$4.64/GJ. This cost is high compared to a cost goal of \$8.52/GJ (\$9.00/10<sup>6</sup> Btu) for thermal energy delivered from a solar central receiver.

#### 4.5 Best Case Configuration

Because of the high cost of the original configuration of the DCHX, we costed a second configuration as well. While the original configuration was based on state-of-the-art technology, the best case configuration assumes progress in several key technologies that have a significant impact on system cost. The assumed progress was limited to technologies that have a reasonable opportunity for progress as a result of future development. Whereas continuing research in these technologies may also create opportunities for cost reduction, these opportunities and their impact are more difficult to project. We have limited our best case assumptions to the development and resulting maturity of existing technologies.



**Figure 4-2. Breakdown of Annual Levelized Cost for Direct-Contact Heat Exchanger**

For the best case configuration the heat exchanger is unchanged, but we made new assumptions that will lower the cost of the solids-handling equipment. These new assumptions are:

- o High-reliability valves--With valves of sufficient reliability, we would not have to allow for maintenance of valves while the plant is on-line. This eliminates the need for the third lockhopper and the isolation valves. Assuming 6 months between plant shutdowns, the system would require valves with lifetimes of about 10,000 cycles between overhauls.
- o No buffer storage--The lockhopper cycles are timed to have one feeder and one defeeder lockhopper available to service the heat exchanger at all times.
- o No flow control valve--The lockhopper valves alone can adequately control flow rate.
- o One stage of cyclones--This is feasible if the particle loading into the cyclones is lower than estimated in Section 3.4 or if adequate performance can, in fact, be gained from one stage.

For this configuration, the cost of the heat exchanger remains the same. The feeders, defeeders, and valves are sized and costed using the same methods as before. Instead of vendor quotes, cyclones were sized and costed using the methods previously described for costing pressure vessels. The cyclones were treated as pressure vessels with height-to-diameter ratios of 4 to 1. The calculation of cyclone pressure drop is given in Section 3.4. Cyclone size was reduced by increasing the inlet air velocity. A trade-off study of cyclone size versus pressure drop resulted in a least cost configuration consisting of four cyclones 6.5 m in height and 1.6 m in diameter with inlet velocities of 30 m/s.

These assumptions had a significant impact on the size and the cost of the system. Figure 4-3 shows a schematic of the configuration. The overall height is 41 m compared to 81 m for the original configuration. Table 4-2 gives costs for the best case configuration. The delivered energy cost is \$2.30/GJ. Within the feeder and defeeder totals, 24% is the cost of valves and 76% is the cost of the lockhopper pressure vessels. Figure 4-4 gives a breakdown of the system cost. This breakdown shows that O&M costs are the single largest contributor to the annual levelized cost. If O&M costs were lower than we assumed, the total cost would be significantly reduced. If the O&M costs were 3% instead of the assumed 6% of total capital costs, the delivered energy would cost \$1.96/GJ.

Using the Solar Thermal Technology Program's cost methodology, the cost of the best case configuration is \$1.56/GJ. This cost, too, is high compared to the \$8.52/GJ (\$9.00/10<sup>6</sup> Btu) cost goal.

This configuration costs about one-third as much as the original configuration and indicates what might be possible with additional progress in the development of solids-handling valves, additional information on O&M costs, and information on the adequacy of a single stage of cyclones. In Section 1.0, we surmised that a direct-contact configuration would be economically attractive because of the elimination of heat transfer surfaces. This is true in that the fluidized-bed heat exchanger itself is not high in cost. However, the cost of the solids-handling equipment required by a direct-contact configuration--feeders, defeeders, and cyclones--results in a DCHX system cost that is high as shown by the comparison to the Solar Thermal cost goal.

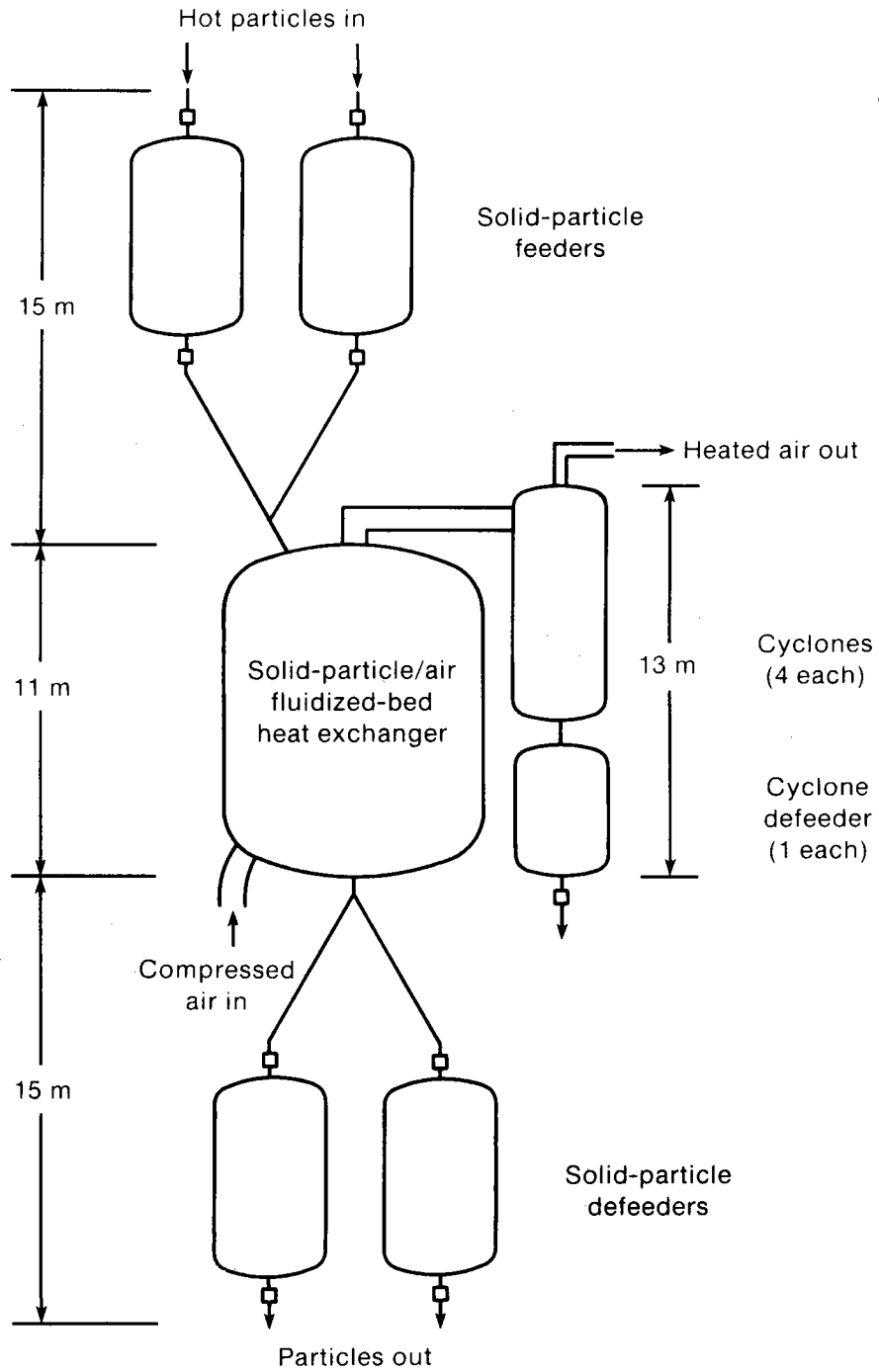
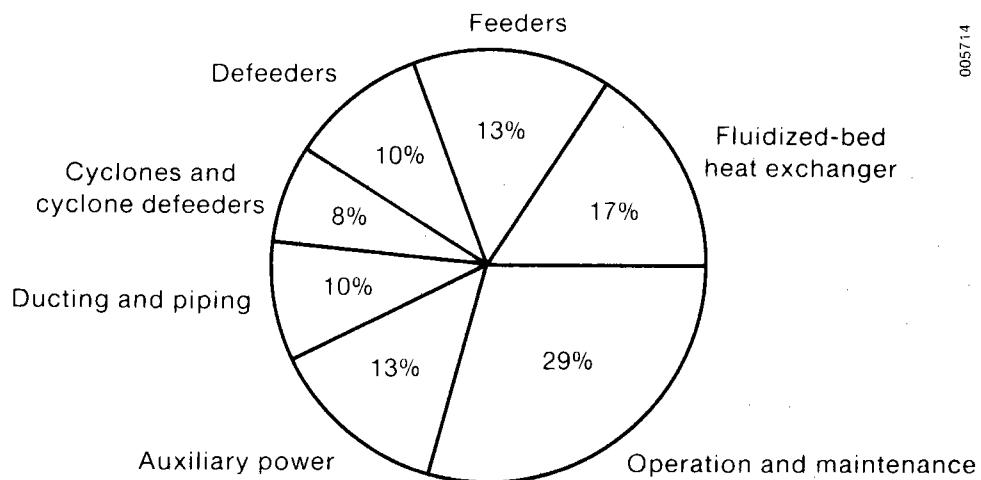


Figure 4-3. Solid-Particle/Air Direct-Contact Heat Exchanger System, Best Case Configuration

**Table 4-2. Direct-Contact Heat Exchanger Costs, Best Case Configuration, in 1981 Dollars**

	Total (10 <sup>6</sup> \$)	Annual Levelized (10 <sup>6</sup> \$)
<b>Capital investment</b>		
Fluidized-bed heat exchanger	2.16	0.48
Feeders	1.67	0.37
Defeeders	1.23	0.27
Cyclones	0.93	0.21
Cyclone defeeders	0.16	0.04
Ducting	1.02	0.23
Piping	0.29	0.06
<b>Total capital investment</b>	<b>7.46</b>	<b>1.66</b>
<b>Annual costs</b>		
Heat exchanger auxiliary power	0.17	0.32
Cyclone auxiliary power	0.04	0.07
Operation & maintenance	0.45	0.85
<b>Total annual costs</b>	<b>0.66</b>	<b>1.24</b>
<b>Total annual levelized cost</b>		<b>2.90</b>
<b>Annual levelized cost per unit of energy transferred</b>		<b>0.0083 \$/kWh<sub>t</sub></b> <b>2.30 \$/GJ</b> <b>2.43 \$/10<sup>6</sup> Btu</b>



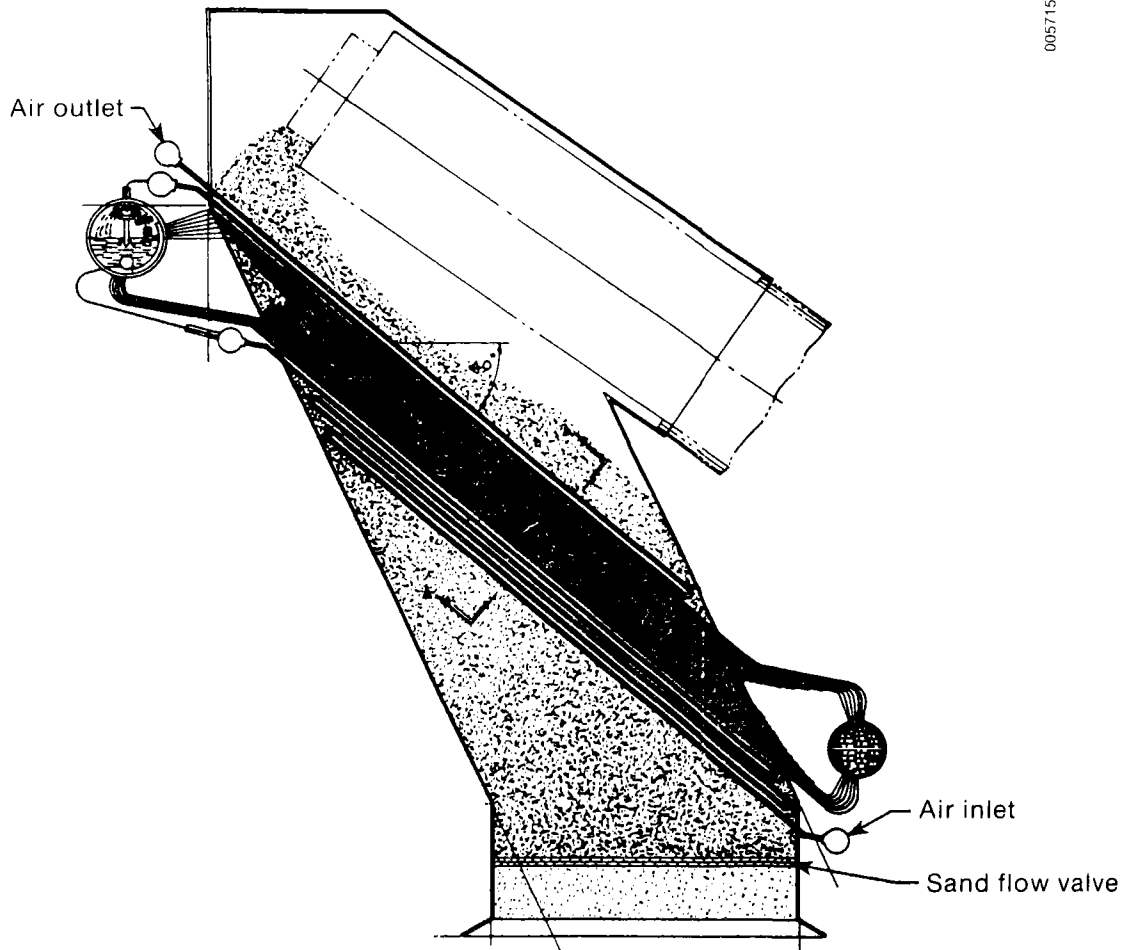
**Figure 4-4. Breakdown of Annual levelized Cost for Direct-Contact Heat Exchanger, Best Case Configuration**

## 5.0 SHELL-AND-TUBE CONFIGURATION

Given the high costs estimated for the DCHX, we decided to evaluate a shell-and-tube heat exchanger configuration as well. In a shell-and-tube configuration, the solid particles are always at ambient pressure, eliminating the need for feeders and defeeders. The air is never in contact with the particles so that cyclones are not required. Because a shell-and-tube heat exchanger does not require such solids-handling equipment, it may be an attractive alternative. This section presents a parametric analysis of shell-and-tube heat exchanger requirements for this application. We assess heat transfer coefficients, required area, flow rates, pressure drops, and cost.

Although a prototype of a moving bed shell-and-tube heat exchanger has not yet been built, several investigators have performed significant research. In a study aimed at the 10-MW solar thermal central receiver pilot plant, Wright et al. (1981) of Babcock and Wilcox investigated the feasibility of several storage concepts for solar thermal application. The most promising alternative to the plant's oil-and-rock storage system was the moving-bed thermal energy storage system (MBTESS), which included discharging heat exchangers that transferred heat from sand (the storage medium), on the shell side of the exchanger, to tubes containing water or steam (see Figure 5-1). The MBTESS design employed gravity-induced sand flow, at low velocity, over the tube bundles to be heated. The tubes were arranged in a staggered pattern and inclined at an angle between the angle of repose and the vertical. The shell was also inclined, parallel to the tubes. This configuration reduces flow resistance, minimizes stagnant regions at the top of each tube, and reduces the appearance of voids underneath the tubes. A recommended bed velocity of 0.15-0.30 m/s provides good heat transfer without appreciable tube wear or particle attrition. A flow restrictor below the tube bank keeps the heat exchanger shell full of moving-bed material. The Babcock and Wilcox study predicted an overall heat transfer coefficient of 931 to 1162 W/m<sup>2</sup> K from the sand moving bed to steam, based on the work of Denloye and Botterill (1977). Dubberly et al. (1983) also investigated the sand moving-bed heat exchanger and predicted performance comparable to the Babcock and Wilcox results (Wright et al. 1981).

A shell-and-tube design has the disadvantage of being limited in operating temperature by the strength of the tube materials. The temperature limit depends on many factors including operating pressure, tube-wall thickness, and tube material. Because no steam is produced in a solid-particle/air heat exchanger, the operating pressures will be inherently lower than in the MBTESS heat exchanger. In this section, no attempt is made to evaluate candidate tube materials and their associated temperature limits. The analysis of the solid particle/air heat exchanger is limited to aspects of performance such as heat transfer and pressure drop.



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Source: Wright et al. 1981.

Figure 5-1. Configuration of the Moving-Bed Heat Exchanger

### 5.1 Sizing the Heat Exchanger

To make a fair comparison with the DCHX, the inlet and outlet temperature conditions for the particles and air sides were identical for the shell-and-tube exchanger, with:

$$T_{ai} = 150^{\circ}\text{C}$$

$$T_{ao} = 970^{\circ}\text{C}$$



$$T_{si} = 1000^{\circ}\text{C}$$

$$T_{so} = 581^{\circ}\text{C} .$$

The desired rate of heat transfer from the alumina particles to the air in the exchanger  $Q$  was  $100 \text{ MW}_t$ . Characteristics of the alumina particles were given as:

particle diameter  $d = 0.5 \text{ mm}$

specific gravity = 4.0

specific heat,  $c_{ps} = 837.2 \text{ J/kg K}$

thermal conductivity =  $8 \text{ W/m K}$  (on average).

The foregoing analysis is based on the configuration studied by Babcock and Wilcox, which has the alumina particles on the shell side and air on the tube side. Brinn et al. (1948) analyzed heat transfer from granular materials moving downward inside vertical tubes. They observed rodlike flow behavior for Ottawa sand in 0.022-m inside diameter tubes. Extending their correlations to our materials, properties, and conditions, the tube-side heat transfer coefficient for a nominal 0.0254-m diameter tube is only about  $8 \text{ W/m}^2 \text{ K}$ . Because the Babcock and Wilcox study predicted much higher overall heat transfer coefficients for particles on the shell side, we chose to follow their work. For purposes of this study, the materials we considered to fabricate the tubes were Incoloy 825 for the first few rows experiencing the highest temperatures, and stainless steel for the remaining tubes. Sensitivities examined in the foregoing analysis include:

- o Effect of outlet air temperature requirement on heat exchanger area and pressure drop
- o Effect of internally finned tubes on required heat exchanger area and pressure drop
- o Effect of particle-side heat transfer coefficient on overall heat transfer coefficient and hence on required heat transfer area
- o Effect of air-side Reynolds number on required heat exchanger area and pressure drop.

## 5.2 Thermal Analysis

Counterflow heat transfer in a shell-and-tube heat exchanger may be expressed by:

$$Q = UA\Delta T_{lm} , \quad (5-1)$$

where  $A$  is the surface area of the heat exchanger,  $U$  is the overall heat transfer coefficient, and  $\Delta T_{lm}$  is the log-mean temperature difference between the two streams. The log-mean temperature difference is known and may be found from:

$$\Delta T_{lm} = \frac{(T_s - T_a)_B - (T_s - T_a)_A}{\ln \left[ \frac{(T_s - T_a)_B}{(T_s - T_a)_A} \right]} \quad (5-2)$$

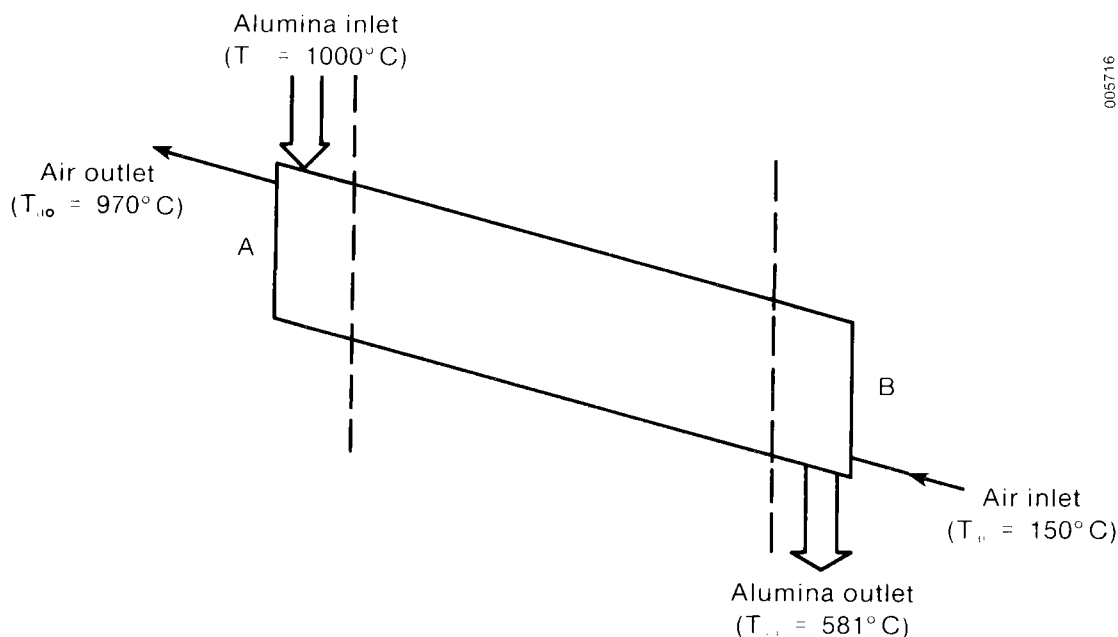
In the preceding equation, and henceforth in this section, the subscript s refers to the alumina solid particles, the subscript a refers to air, and A and B refer to opposite ends of a counterflow heat exchanger configured as in Figure 5-2.

To solve for the required heat transfer area, we must compute the overall heat transfer coefficient U from:

$$U = \frac{1}{\frac{1}{H_p} + R_p + \left( \frac{1}{H_a} + R_a \right) \frac{D_o}{D_i} + \frac{Y_w D_o}{K_w D_w}} \quad (5-3)$$

where

$$D_w = \frac{D_o - D_i}{\ln(D_o/D_i)} \quad (5-4)$$



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Figure 5-2. Schematic of Moving-Bed Shell-and-Tube Heat Exchanger

In the previous equations,  $H_p$  is the heat transfer coefficient on the particle or shell side,  $H_a$  is the air-side (tube-side) heat transfer coefficient,  $R_p$  and  $R_a$  are fouling resistances,  $D_o$  and  $D_i$  are the outside and inside diameters of the tubes,  $Y_w$  is the wall thickness, and  $K_w$  is the wall thermal conductivity.

The expression describing the tube-side heat transfer coefficient  $H_a$  is (Carnavos 1979):

$$Nu_a = 0.023 Re_a^{0.8} Pr_a^{0.4} F, \quad (5-5)$$

where  $F$  is a heat transfer adjustment factor for fin-tube geometry ( $F = 1$  for smooth tubes),  $Nu_a$  is the air-side Nusselt number,  $Re_a$  is the air-side Reynolds number, and  $Pr_a$  is the air-side Prandtl number. The air heat transfer coefficient  $H_a$  is then found from the definition of  $Nu_a$ :

$$H_a = \frac{Nu_a K_a}{D_h}, \quad (5-6)$$

where  $D_h$  is the hydraulic diameter of the tube and  $K_a$  is the thermal conductivity of air. Table 5-1 gives characteristics for a smooth tube and a finned tube used in the following analysis.

The alumina-side (shell-side) heat transfer coefficient is found from (Kurochkin 1966):

$$Nu_s = 0.0214 Pe^{0.21} \frac{D_o}{d_s}, \quad (5-7)$$

where

$$Pe = \frac{V_o c_{ps} \gamma_b D_o}{K_s}.$$

In the above equations,  $d_s$  is the mean particle diameter,  $V_o$  is the bed velocity,  $c_{ps}$  is the specific heat of the alumina,  $\gamma_b$  is the bulk density,  $K_s$  is the thermal conductivity of the alumina particles, and  $Pe$  is the Peclet number. The bed velocity was 0.15 m/s, based on the design developed by Babcock

**Table 5-1. Tube Dimensions and Adjustment Factors**

	Smooth Tube	Finned Tube
$D_i$	22.2 mm	23.7 mm
$D_o$	27.2 mm	25.4 mm
$D_h$	22.2 mm	12.2 mm
$F$	1.0	1.13
$F^*$	1.0	1.07

and Wilcox. Sample calculations for the heat transfer coefficients may be found in Appendix C. For those conditions, the value of  $H_s$  is  $1468 \text{ W/m}^2 \text{ K}$ , and  $H_a$  is  $146 \text{ W/m}^2 \text{ K}$ , so that the air side controls the heat transfer.  $U$  is  $103 \text{ W/m}^2 \text{ K}$  for the case shown in Appendix C.

### 5.3 Pressure Drop

The pressure drop on the air side (tube side) was a major consideration in the operating cost of the heat exchanger. However, because the air side controls heat transfer (as was seen in our calculations in Appendix C), we wished to have a relatively high velocity in the tubes to enhance heat transfer. In addition to smooth tubes, we investigated internally finned tubes that are designed to improve heat transfer. Carnavos (1979) gives the friction factor for both smooth and finned tubes as:

$$f = \frac{0.046}{\text{Re}^{0.2} F^*}, \quad (5-8)$$

where  $F^*$  is a friction factor adjustment for finned-tube geometry. Pressure drop across the tubes in the heat exchanger core may then be found from:

$$\Delta P = \frac{2fV_a^2 L \rho_a}{D_h}, \quad (5-9)$$

where  $V_a$  is the velocity of the air,  $L$  is the tube length, and  $D_h$  is the hydraulic diameter. This expression does not account for entrance or exit effects, which we assume are negligible compared to the core friction. Sample calculations appear in Appendix D.

### 5.4 Parametric Analysis

Because the greatest unknown is the thermal performance of the moving bed on the shell side of the heat exchanger, we first examined the influence of  $H_p$ , the particle-side heat transfer coefficient, on the required area. The model presented by Kurochkin (1966) results in a value of  $H_p = 1468 \text{ W/m}^2 \text{ K}$ , which is reasonable compared to values of overall heat transfer coefficient for sand to steam predicted by the Denloye and Botterill model by Wright et al. From Figure 5-3, we see that beyond  $H_p$  approximately equal to  $800 \text{ W/m}^2 \text{ K}$ , there is little impact on the heat transfer surface required because the air side controls heat transfer. This result indicates that our value for  $H_p$  is a reasonable choice for this analysis, as predictions of the area requirement do not significantly change for  $H_p$  between  $800$  and  $1700 \text{ W/m}^2 \text{ K}$ .

We next examined the effect of changing the conditions on the air side to improve heat transfer. Figure 5-4 shows the effect of increasing the Reynolds number on the tube side from  $10,000$  to  $50,000$ . Figure 5-5 illustrates the impact on pressure drop. Another way of improving heat transfer is through the use of finned tubes. Using the characteristics of the internally finned tube described in Table 5-1, we compared the performance of smooth tubes to

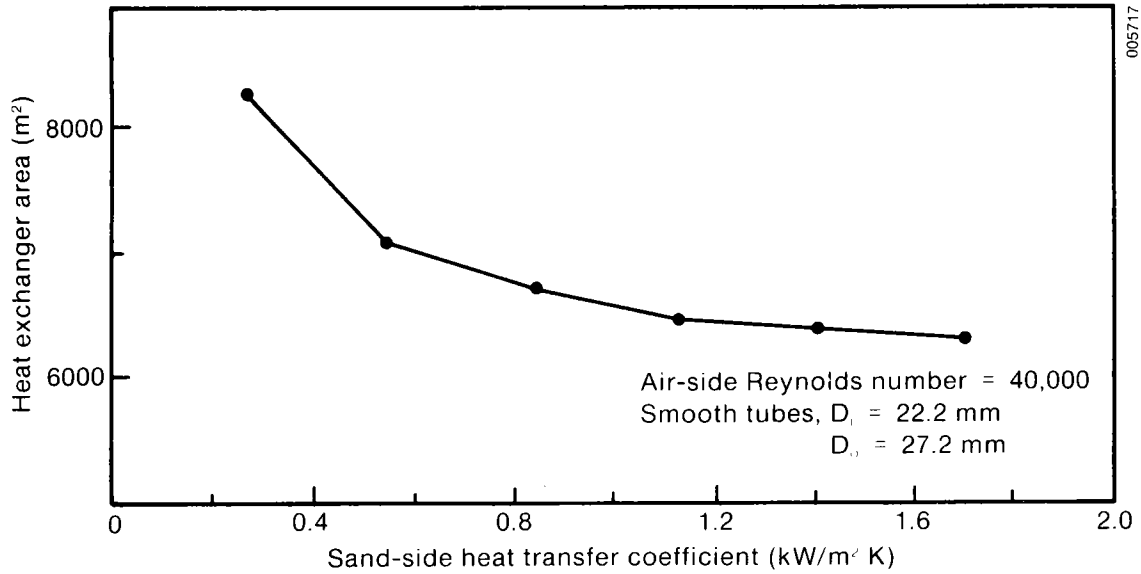


Figure 5-3. Effect of Improving Sand-Side Heat Transfer Coefficient on Total Area Requirement

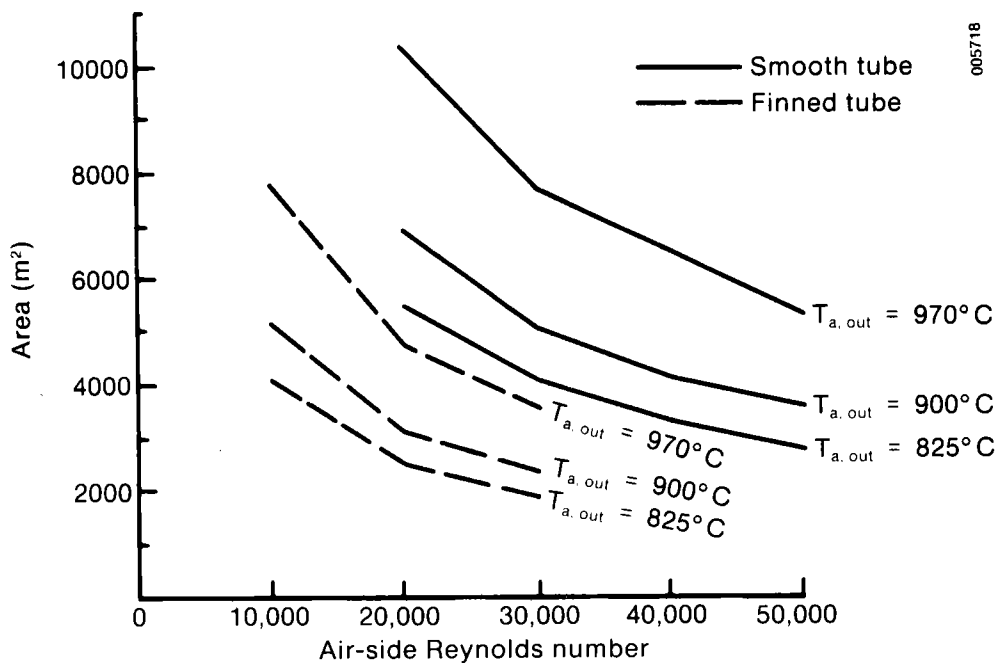


Figure 5-4. Effect of Air-Side Flow Rate on Required Heat Transfer Area

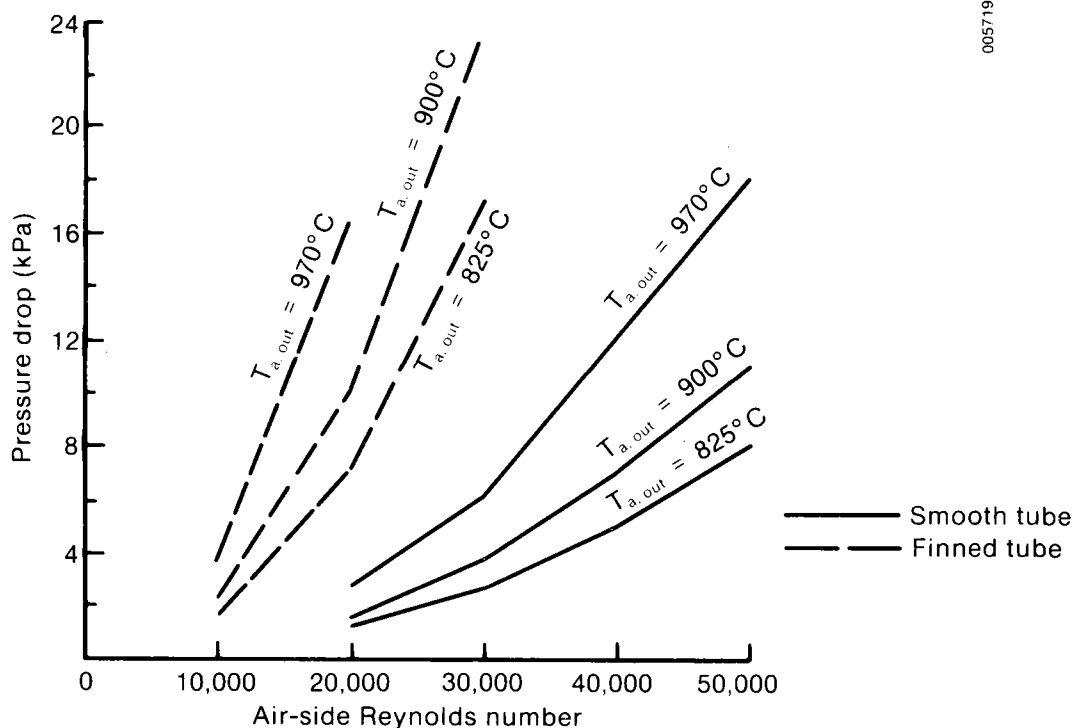


Figure 5-5. Effect of Air-Side Flow Rate on Pressure Drop

finned tubes as a function of Reynolds number (also in Figures 5-4 and 5-5). Finally, we looked at the effect that relaxing the outlet air temperature requirement has on the required heat transfer area. The DCHX easily attained the outlet temperature of  $970^\circ\text{C}$  because of the heat transfer characteristics of fluidized beds. With the shell-and-tube configuration, such a high outlet temperature is not as easily attained and affects the required area and the pressure drop. These results appear as well in Figures 5-4 and 5-5.

### 5.5 Cost Estimates

We estimated capital costs for the heat exchangers discussed in the previous section based on techniques described in Peters and Timmerhaus (1980). The cost of a U-tube heat exchanger with 2.54-cm (1-in.) stainless steel tubes operating at 1034 kPa (150 psi) is given as  $\$280/\text{m}^2$  ( $\$26/\text{ft}^2$ ) in 1981 dollars. This is for a heat exchanger area of  $409 \text{ m}^2$  ( $4400 \text{ ft}^2$ ), the largest for which data are given (Peters and Timmerhaus 1980, p. 670). The same heat exchanger constructed with Incoloy 825 tubing would cost  $\$463/\text{m}^2$  ( $\$43/\text{ft}^2$ ) (Peters and Timmerhaus 1980, p. 677). For our cost estimate, we assumed a capital cost of  $\$540/\text{m}^2$  ( $\$50/\text{ft}^2$ ) in 1981 dollars. This cost was increased by a Lang factor of 3.5 to account for delivery and installation. We used the methods described in Section 4.0 to determine O&M costs and auxiliary power costs, and to calculate the annual levelized costs.

For comparison to the DCHX, we chose a baseline case for the shell-and-tube heat exchanger that included smooth tubes,  $T_{a,o}$  at  $970^\circ\text{C}$ ,  $Re_a$  of 50,000, requiring a heat exchanger area of  $5300 \text{ m}^2$ . Table 5-2 gives the costs for this baseline configuration. This configuration has an energy cost of  $\$2.91/\text{GJ}$ , less than one-half the cost of the original DCHX configuration. Figure 5-6 shows heat exchanger costs for other outlet temperatures, other

values of  $Re_a$ , and for both smooth and finned tubes. For both types of tubes, we assumed the same cost of  $\$540/m^2$ .

Using the Solar Thermal Technology Program's cost methodology, the shell-and-tube configuration has a cost of  $\$2.03/GJ$ .

**Table 5-2. Cost Estimate for Baseline Shell-and-Tube Configuration in 1981 Dollars**

	Total ( $10^6$ \$)	Annual Levelized ( $10^6$ \$)
<b>Capital investment</b>		
Heat exchanger	10.06	2.24
Piping	0.40	0.09
Total capital investment	<u>10.46</u>	<u>2.33</u>
<b>Annual costs</b>		
Heat exchanger auxiliary power	0.08	0.15
Operation & maintenance	0.63	1.19
Total annual costs	<u>0.71</u>	<u>1.34</u>
Total annual levelized cost		3.67
Total annualized cost per unit of energy transferred		0.0105 $\$/kWh_t$ 2.91 $\$/GJ$ 3.07 $\$/10^6$ Btu

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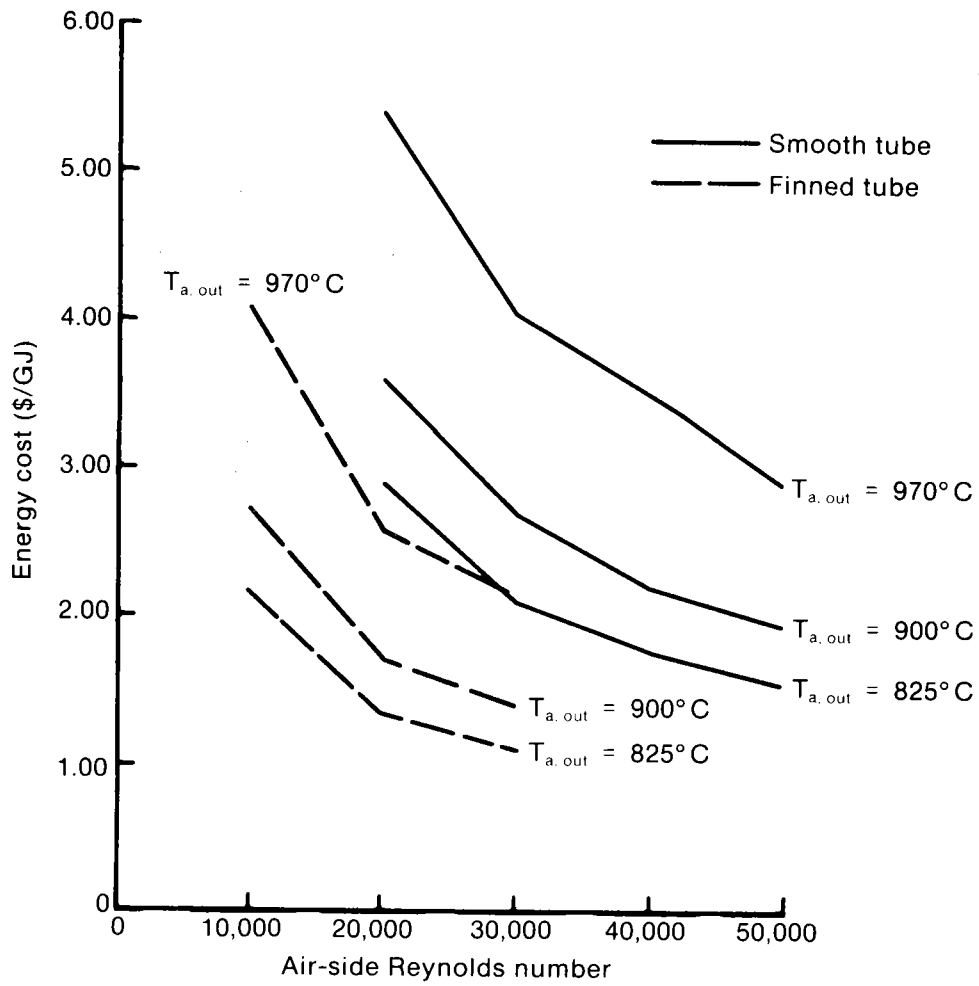


Figure 5-6. Effect of Air-Side Flow Rate on Heat Exchanger Cost



## 6.0 CONCLUSIONS AND RECOMMENDATIONS

A direct-contact heat exchanger system was designed to transfer heat at a rate of 100 MW<sub>t</sub> from 1000°C solid particles to air at 10 atm pressure. The annual levelized cost of thermal energy delivered from the system was estimated for two direct-contact configurations. The original configuration was based on the best information available on the state of the art of the various technologies involved and has an annual levelized cost per unit of delivered energy of \$6.66/GJ. The best case configuration allowed for reasonable progress resulting from future development activities in several technologies and has a cost of \$2.30/GJ. Much of the cost of the direct-contact configurations is in the solids-handling equipment--particle feeders and defeeders and the cyclones--and not in the heat exchanger itself. As an alternative to direct contact, a shell-and-tube heat exchanger was designed for the same service. The cost of this heat exchanger per unit of delivered energy is estimated to be \$2.91/GJ.

These costs were calculated using a cost methodology developed by the SERI Solar Energy Storage Program. In addition, a cost methodology from the Solar Thermal Technology Program was used to allow comparison to the Solar Thermal cost goals. Using this methodology, the original configuration cost \$4.64/GJ, the best case configuration cost \$1.56/GJ, and the shell-and-tube configuration cost \$2.03/GJ. All these costs are high compared to the Solar Thermal cost goal of \$8.52/GJ (\$9.00/10<sup>6</sup> Btu) for thermal energy delivered from a solar central receiver.

The direct-contact heat exchanger (DCHX) is a technically feasible option, though development is needed in several areas. Fluidized-bed behavior is well characterized, but data on fluidized-bed behavior with the particles that will actually be used in the system would greatly increase the confidence of design. We must resolve design details such as grid design for good air distribution, minimum stable bed depth, and the number of downcomers needed between stages to maintain uniform temperatures in the beds. Because of the high temperatures in the uppermost beds in the heat exchanger, materials for grid construction need to be examined.

Development of lockhopper valves to handle abrasive solids is needed to extend the temperature range of state-of-the-art valves beyond the current 650°C at 10 atm for 2000 cycles. Valves are needed that will operate at 1000°C at 10 atm pressure for 10,000 cycles. In particular, development of improved valve seat materials is needed. Confirmation of valve reliability is important because providing the capability for on-line valve maintenance significantly increased system cost.

For cyclone design, data are required on the extent of particle attrition in the receiver, in storage, and in transport. These attrition rates will determine the loading of fines into the cyclones, which in turn will dictate the number of cyclone stages needed and perhaps the pressure drop. Another important need is the confirmation of cyclone performance at high temperature and pressure. Advances in turbine technology allowing higher particle loadings would also be a benefit.

The DCHX can be economically competitive with shell-and-tube configurations if the valves noted above become available and if future developments indicate that only one stage, or perhaps no stages, of cyclones are needed. These assumptions were made for the best case configuration for which a DCHX system with one stage of cyclones is estimated to cost \$2.30/GJ. This cost will be reduced if O&M costs are found to be less than the 6% of total capital cost assumed in this study. More information is needed on O&M costs for this type of system.

The shell-and-tube heat exchanger, unlike the direct-contact configuration, does not require extensive solids-handling equipment. Therefore the shell-and-tube heat exchanger has a lower cost that could be reduced even further by reducing the outlet air temperature or possibly by using tubes with heat transfer enhancement on the air side. In this study, we have not evaluated tube design or tube materials for the high-temperature regions of the heat exchanger. These issues appear to be the major technical uncertainties of the shell-and-tube configuration and may limit the operating temperature. Also, there seems to be less commercial experience with this type of heat exchanger than there is with equipment such as cyclones and fluidized beds.

This study is an evaluation of a particular subsystem, not a full system study. The specific values of many parameters used in the course of the study will significantly affect the cost and performance of the balance of the central receiver system. These parameters include solids mass flow rate, solids outlet temperature, and air outlet temperature. System studies will be needed to evaluate the impact of these parameters and to determine what portion of system cost should be allocated to the heat exchanger.

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**APPENDIX A. COSTING METHODOLOGY FOR SERI'S SOLAR ENERGY STORAGE PROGRAM**

To ensure comparable cost projections, a consistent methodology and constant financial and economic parameters should be used both by SERI in-house researchers as well as by subcontractors.

The cost methodology adapted is the one developed by the Jet Propulsion Laboratory [1].

The basic approach of the methodology is to devise an estimate of the costs incurred by the owner/operator of the system as a result of purchasing, installing, and operating the solar energy system under consideration. These costs, aggregated over the system lifetime and converted to an annual basis, are divided by the expected yearly system output. The result is an estimate of the levelized annual cost per unit of output. This levelized cost is the price that must be charged per unit of output so that the resultant revenues would exactly recover the full cost of the system over its expected life. If the levelized annual cost per unit is less than the levelized cost of the same output provided by other means, the system is cost-effective.

The nomenclature and symbols used in this section are explained in Table A-1.

The basic equation for the levelized cost is

$$LOC = AC/O \quad (A-1)$$

The levelized annual system cost in  $Y_b$  dollars is computed from the capital expenditures and their timing, as well as the operating and maintenance cost stream. Note that replacement item capital costs are treated as capital expenditures.

The levelized annual system cost is given by:\*

$$AC = (1 + g)^{-d} [FCR \cdot CI_{pv} + CRF_{K,N} (O\&M_{pv} + FL_{pv})] \quad (A-2)$$

The annualized fixed charge rate (FCR) is the factor by which  $CI_{pv}$  must be multiplied to obtain the contribution of capital investment to the levelized annual system cost.

The capital recovery factor (CRF) represents the uniform annual amount (payment) that must be made to fully amortize the capital investment (loan) over  $N$  years at the interest rate of  $K$ .

$$FCR^{**} = \frac{1}{1 - T} \left( CRF_{K,N} - \frac{T}{N} \right) + b \quad (A-3)$$

---

\*Present value refers to the first year of commercial operation,  $Y_{CO}$ .

\*\*Disregarding investment tax credit. With investment tax credit FCR is given in Eq. A-4.

Table A-1. Nomenclature

Symbol	Description
a	Investment tax credit fraction
AC	Levelized annual system cost in $Y_b$ dollars
ACRS	Accelerated cost recovery system
b	Annual insurance and "other tax" fraction
CI	Capital expenditures
CRF	Capital recovery factor
d	Time difference
DPF	Depreciation factor for sum-of-the-years-digits depreciation
FCR	Annualized fixed charge rate
FL	Fuel cost
g	Annual rate of general inflation
$g_c$	Annual escalation rate for capital costs
$g_f$	Annual escalation rate for fuel costs
$g_o$	Annual escalation rate for operation and maintenance costs
j	Time difference
K	Cost of capital (rate of return on capital, discount rate)
LOC	Levelized annual cost per unit of output
n	Accounting lifetime (depreciation life or tax life)
N	System operating lifetime
O&M	Operating and maintenance costs
p	Time difference
Q	Annual system output as measured in MJ
SDF	Depreciation factor for statutory accelerated depreciation
T	Effective corporate income tax rate
V	Levelized annual value of system output
$V_o$	Value of system output in year $Y_{co}$ expressed in $Y_b$ dollars
$Y_b$	Base year for constant dollars
$Y_{co}$	First year of commercial operation
$Y_p$	Price year for cost information
$Y_t$	Year t
<hr/>	
Subscript	
n	Accounting lifetime
N	System operating lifetime
o	Cost year $Y_{co}$ expressed in $Y_b$ dollars
pv	Present value (year $Y_{co}$ value)
t	Time

$$FCR = \frac{CRF_{K,N}}{1 - T} [1 - (T \cdot DPF_{K,n}) - a] + b \quad (A-4)$$

$$CRF_{K,N} = K/[1 - (1 + K)^{-N}] \quad (A-5)$$

The present value of the capital expenditures and of the operating and maintenance costs is computed using typical discounting formulas. In calculating the present value of the operating and maintenance costs, we assume that these costs are uniform streams over the system lifetime.

$$CI_{pv} = (1 + g_c)^P \sum_t CI_t \left( \frac{1 + g_c}{1 + K} \right)^j \quad (A-6)$$

$$O\&M_{pv} = (1 + g_o)^P \cdot O\&M_o \left( \frac{1 + g_o}{K - g_o} \right) \left[ 1 - \left( \frac{1 + g_o}{1 + K} \right)^N \right] \text{ if } K \neq g_o \quad (A-7)$$

$$(1 + g_o)^P \cdot O\&M_o \cdot N \quad \text{if } K = g_o$$

$$p = Y_{co} - Y_p \quad (A-8)$$

$$j = Y_t - Y_{co} + 1 \quad (A-9)$$

$$d = Y_{co} - Y_b \quad (A-10)$$

Note that  $CI_{pv}$  and  $O\&M_{pv}$  are in year  $Y_{co}$  dollars. Adjustment to  $Y_b$  dollars is made when calculating AC.

$O\&M_o$  is the cost in year  $Y_{co}$  expressed in  $Y_p$  dollars.  $CI_t$  is the capital investment during year  $Y_t$  expressed in  $Y_p$  dollars.

For nonuniform operating and maintenance costs,  $O\&M_{pv}$  is calculated from:

$$O\&M_{pv} = (1 + g_o)^P \cdot \sum_{j=1}^N O\&M_t \left( \frac{1 + g_o}{1 + k} \right)^j \quad (A-11)$$

Based on the present value estimates for the capital expenditures, the recurrent costs, and operating and maintenance costs, the annual levelized system cost is calculated. This annualized system cost is equal to a cost stream of equal annual payments that has a present value equal to that of all the system costs (i.e., capital expenditures and operating, maintenance, and fuel costs).

For storage subsystem analysis, where several options for storage are considered, and where no annual system output can be associated with the subsystem (but only a storage capacity), present worth for capital costs, operation and maintenance costs, and fuel costs (gas, oil, or electricity) may be used in the trade-off.



For accounting purposes, the capital investment must be depreciated over a number of years. For the equipment under consideration the accounting life-time is 15 years. According to the tax law of 1981, the accelerated cost recovery system (ACRS) may be used. For investments after 1985, the depreciation factor for statutory accelerated depreciation is:

$$SDF_{K,N} = \frac{1}{n(1+K)} \left\{ 1 + \frac{2}{CRF_{K,(n-1)}} - \frac{2(1+K)}{nK^2} \left[ 1 - \frac{1+nK}{(1+K)^n} \right] \right\}. \quad (A-12)$$

The accelerated depreciation schedule for a public utility (15-year accounting life) is shown in Table A-2.

**Annual Output Value**

The basic equation for the levelized cost requires an estimate of the system output.

The output value should also be expressed as a levelized annual value using the same discount and inflation factors given in Table A-3. To calculate the levelized value of the output the following expression is used.

$$V = V_0 \left( \frac{1+g}{K-g} \right) \left[ 1 - \left( \frac{1+g}{1+K} \right)^N \right] \cdot CRF_{K,N}. \quad (A-13)$$

**Table A-2. Accelerated Depreciation Schedule for Public Utility Placed into Service after 31 December 1985 (in percent)**

If the year since installation is:	Applicable percentage
0	7
1	12
2	12
3	11
4	10
5	9
6	8
7	7
8	6
9	5
10	4
11	3
12	3
13	2
14	1

**Table A-3. Financial Parameters for Preliminary Economic Analyses**

Symbol	Description	Value
N	System operating lifetime (years)	30
n	Accounting lifetime (years)	15
K	Cost of capital (rate of return on capital, discount rate)	$0.10^a$
$CRF_{K,N}$	Capital recovery factor (10%, 30 years)	0.10608
$g$	Rate of general inflation	0.06
$g_c$	Escalation rate for capital costs	0.06
$g_o$	Escalation rate for operating and maintenance costs	0.06
$g_f$	Escalation rate for fuel costs	0.08
$Y_b$	Base year for constant dollars	1981
$Y_{co}$	First year of commercial operation	1990
$Y_p$	Price year for cost information	1981
	Raw land cost	$\$1.25/m^2$
	1990 costs in 1981 dollars for:	
	Natural gas	$\$6.30/GJ$
	Residual oil (No. 6)	$\$7.49/GJ$
	Distillate oil	$\$8.91/GJ$
	Liquid gas	$\$6.83/GJ$
	Coal	$\$2.28/GJ$
	Electricity	$\$12.89/GJ$
FCR	Annualized fixed charge rate	0.19216
b	Annual insurance + "other tax" fraction	0.02
a	Investment tax credit fraction	0.10
T	Effective corporate income tax rate	0.50

<sup>a</sup>Typical for utility applications. Cost for industrial applications may be higher.

For the given values of the discount factor and the inflation rate, the above expression for the levelized annual output value reduces to:

$$V = 1.88584 V_0 .$$

The financial parameters to be used are given in Table A-3.

### Capital Investment Estimation

Cost estimation for capital equipment shall use the methodology and factors given in Refs. 2 and 3.

### Cost Comparisons

For energy storage cost estimates, the capital investment in Eq. A-6 can be approximated by:

$$CI_t = F_1[F_2(A) + F_3(B)] , \quad (A-14)$$

where

A = energy and power related capital costs of system

B = storage medium cost

$F_1$  = nondirect costs factors

$F_2$  = installation cost factor for A

$F_3$  = installation cost factor for B.

The magnitude of the factors  $F_1$ ,  $F_2$ , and  $F_3$  vary widely for various groups that have made cost estimates. Table A-4 shows the values for these factors.

For SERI work, the factor per Ref. 3 shall be used. Deviations from these factors must be justified.

**Table A-4. F-Factors**

Source	$F_1$	$F_2^b$	$F_3^c$	$(F_1) \times (F_2)$
Ref. 3	1.95	1.80	1.0	3.51
Industry practice <sup>a</sup>				
Maximum	2.5	2.0	2.0	5.0
Minimum	--	--	1.0	3.0
JPL	1.2	1.0	1.0	1.2
SNLL	1.155	--	--	TBD
SNLA	1.25	--	--	TBD
Solar Thermal Cost Goals Committee	1.25	TBD	TBD	TBD
Copeland (6/81-2/82)	1.44	1.8	1.0	2.59

<sup>a</sup>According to Stearns-Roger Services, Inc.

<sup>b</sup>The installation cost factor is based on the primary equipment cost. It gives an estimate for the labor cost to install the equipment.

<sup>c</sup> $F_3$  is the labor cost factor to install the storage medium.

## REFERENCES

1. Doane, J. W., R. P. O'Toole, R. G. Chamberlain, P. B. Bos, and P. D. Maycock, The Cost of Energy from Utility-Owned Solar Electric Systems--A Required Revenue Methodology for ERDA/EPRI Evaluations, ERDA/JPL-1012-76-3, Pasadena, CA: Jet Propulsion Laboratory, June 1976.
2. Peters, M. S., and K. D. Timmerhaus, Plant Design and Economics for Chemical Engineers, 3rd Edition, New York: McGraw-Hill Book Company, 1980.
3. Cost and Performance of Thermal Storage Concepts in Solar Thermal Systems, Final Report Phases 1 and 2, SERI/TR-XP-0-9001-1-A and -B. November and December 1981. Prepared by Stearns-Roger Services Inc., Denver, CO. Available from NTIS.

APPENDIX B

CRITICAL REVIEW  
OF THE STATE OF THE ART  
OF PARTICLE-GAS HEAT EXCHANGERS

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## OBJECTIVES OF THIS ACTIVITY

COLLECT AND REVIEW EXISTING INFORMATION ON SAND TO AIR DIRECT CONTACT HEAT EXCHANGERS AND RELATED EQUIPMENT OPERATING AT HIGH TEMPERATURE AND PRESSURE.

DETERMINE THE OPTIONS FOR EACH COMPONENT OF THE SAND TO AIR DCHX SUBSYSTEM TO BE INCLUDED IN A CONCEPTUAL DESIGN AND COST ESTIMATE.

## APPROACH

CHOOSE A BASELINE SET OF COMPONENTS WHICH BEST SATISFY BASIC PERFORMANCE CRITERIA AND FOR WHICH SUFFICIENT INFORMATION EXISTS TO DEVELOP AN OPTIMIZED DESIGN FROM WHICH COST MAY BE ESTIMATED.

IF POSSIBLE, IDENTIFY AN OPTION FOR EACH COMPONENT OF THE BASELINE WHICH HOLDS THE POTENTIAL FOR IMPROVED PERFORMANCE.

## OUTLINE

## I. COMPONENTS

## A. HEAT EXCHANGER

## 1. OPTIONS

- a. FLUIDIZED BED
  - i. SINGLE-STAGE
  - ii. MULTI-STAGE
- b. FALLING BED
  - i. FREE
  - ii. HINDERED
- c. MOVING BED
- d. CASCADING BED
- e. STAGED CYCLONES

## 2. HEAT TRANSFER

- a. CONVECTION AND CONDUCTION ONLY
- b. INCLUDING RADIATION

## 3. FLUID MECHANICS

## B. FEEDER

- 1. LOCK HOPPER
- 2. PISTON
- 3. POUCKET
- 4. SCREW
- 5. INERTIAL PLUG
- 6. PAN

## C. SEPARATOR

- 1. AIR QUALITY REQUIREMENTS
- 2. OPTIONS
  - a. CYCLONE
  - b. ELECTROCYCLONE
  - c. FILTER
  - d. PACKED BED

## D. COMPRESSOR

## E. INSULATION

## II. INDUSTRY

## A. INVENTORS AND MANUFACTURERS

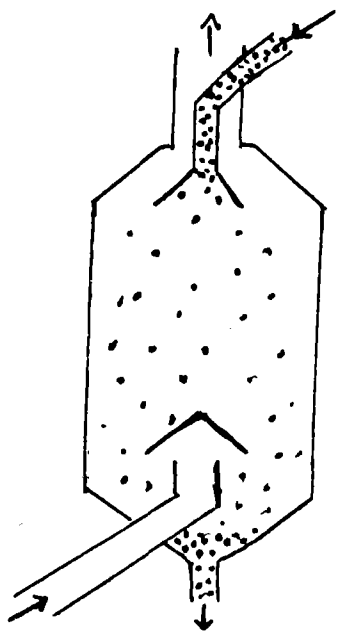
## B. APPLICATIONS

- 1. WASTE HEAT RECOVERY
- 2. CAT CRACKING
- 3. MHD
- 4. PRESSURIZED FLUIDIZED BED

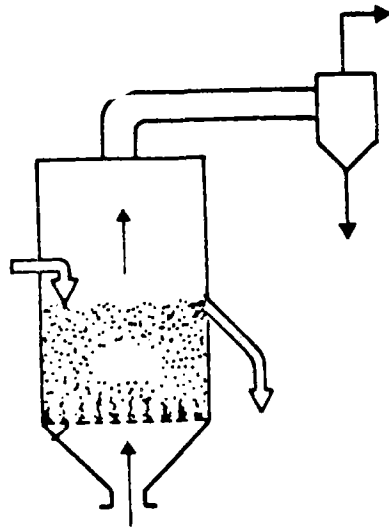




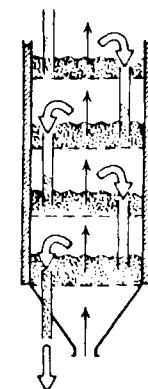
FREE FALLING BED



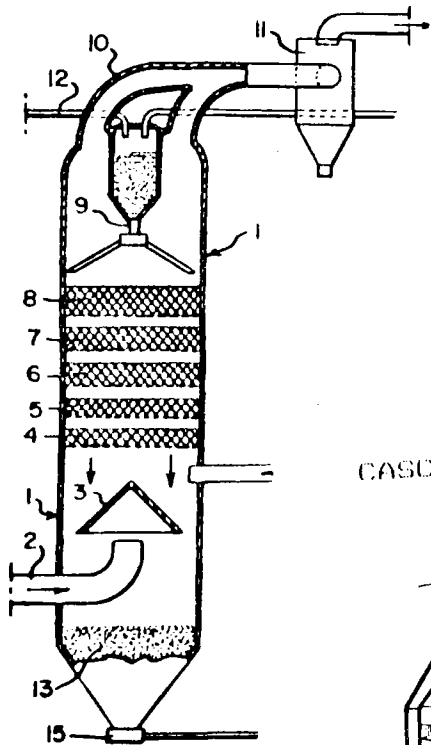
SINGLE-STAGE FLUIDIZED BED



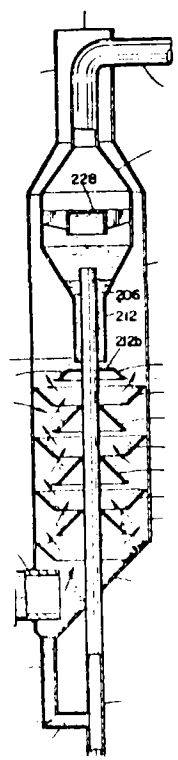
MULTI-STAGE FLUIDIZED BED



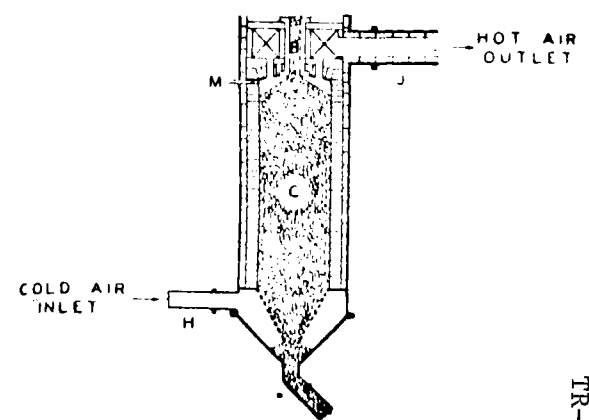
HINDERED FALLING BED



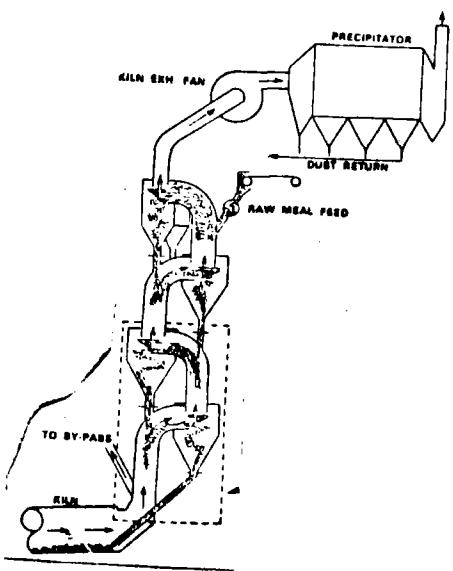
CASCADING BED



MOVING BED



STAGED CYCLONES



## INFORMATION ON PARTICLE/GAS HEAT EXCHANGERS

	HEAT TRANSFER (AMBIENT)	HEAT TRANSFER (HIGH T)	HEAT TRANSFER (HIGH P)	FLUID MECHANICS (AMBIENT)	FLUID MECHANICS (HIGH T)	FLUID MECHANICS (HIGH P)
FREE FALLING BED	2	1		2		
HINDERED FALLING BED	2			2		
MULTISTAGE FLUIDIZED BED	2	2	2	2	2	2
MOVING BED	1	1		2		

2 = DIRECTLY RELATED INFORMATION

1 = INFORMATION FROM ANOTHER SYSTEM THAT CAN BE APPLIED.

FLUIDIZED BED  
FLUID MECHANICS  
AT AMBIENT TEMPERATURE AND PRESSURE

REFERENCES: ERGUN (1952), ERGUN AND ORNING (1949)

SUMMARY: THE PRESSURE DROP ACROSS A FIXED AND EXPANDED BED IS GIVEN BY

$$\frac{\Delta P}{L} = 150 \frac{(1-\epsilon)^2}{\epsilon^3} \frac{\mu U_M}{D_p^2} + 1.75 \frac{(1-\epsilon)}{\epsilon^3} \frac{\rho U_M}{D_p}$$

WHEN THE PRESSURE DROP EQUALS THE BOUYANT WEIGHT OF THE PACKING PER UNIT VOLUME OF THE BED,

$$\frac{\Delta P}{L} = (1-\epsilon) (\rho_p - \rho_f) g,$$

THE BED BEGINS TO EXPAND. WHILE THE BED EXPANDS THE PRESSURE DROP REMAINS CONSTANT AND THE VOID FRACTION IS GIVEN BY SUBSTITUTING EQUATION 2 IN EQUATION 1.

THE EXPANSION IS HOMOGENEOUS UNTIL THE BED ATTAINS THE LOOSEST STABLE CONFIGURATION OF THE SOLIDS (FOR SPHERES THIS IS A CUBICAL PACKING WITH  $\epsilon = 0.47$ ). AN ADDITIONAL INCREASE IN FLOW RATE CAUSES BUBBLES OF GAS TO PASS THROUGH THE BED. THE BED IS NOW FLUIDIZED.

FLUIDIZED BED  
FLUID MECHANICS  
EFFECT OF GREATER THAN AMBIENT TEMPERATURE

REFERENCE: BOTTERILL, TEOMAN, AND YUREGIR (1982 A AND B)

EXPERIMENTAL  
CONDITIONS:

PRESSURE: AMBIENT

GAS: AIR

GAS INLET

TEMP.: 20°C TO 960°C

PARTICLE

MATERIALS: SAND, COAL ASH, ALUMINA, GLASS BALLOTINE

PARTICLE MEAN DIAMTERS (MM): SAND - 0.38, 0.46, 0.53, 0.66, 0.78, 0.89, 1.28, 2.32; COAL ASH - 0.82 WITH A WIDE DISTRIBUTION; ALUMINA - 0.37, 0.98, 1.12; GLASS BALLOTINE - 1.04

PARTICLE SHAPE FACTORS: SAND - 0.90, 0.80, 0.84, 0.92, 0.97, 0.95, 0.74, 0.64; COAL ASH - UNDETERMINED; ALUMINA - 0.88, 0.56, 0.54; GLASS BALLOTINE - 1.00

MEASUREMENTS: MEASURED THE MINIMUM FLUIDIZING GAS SPEED AND THE VOIDAGE AT MINIMUM FLUIDIZATION

RESULTS:  $E_{MF}$  VARIES WITH TEMPERATURE.

VARIATION OF  $U_{MF}$  WITH TEMPERATURE AGREES WELL WITH ERGUN EQUATION WHEN VARIATION OF  $E_{MF}$  IS TAKEN INTO ACCOUNT.

THERE IS A TRANSITION BETWEEN TYPE B&D BEHAVIOR WHEN  $Re_{MF} = 12.5$  AND  $Ar = 26000$

COMMENTS: NO EXPLANATION GIVEN FOR WHY  $E_{MF}$  VARIES WITH TEMPERATURE.

FLUIDIZED BED  
FLUID MECHANICS  
EFFECT OF GREATER THAN AMBIENT PRESSURE

REFERENCE: KAWABATA ET.AL. (1981)

EXPERIMENTAL CONDITIONS:

TEMPERATURE: AMBIENT

GAS: AIR

GAS PRESSURE: 0.1 MPA TO 0.8 MPA

PARTICLE

MATERIALS: SILICA SAND

PARTICLE MEAN

DIAMETERS (MM): 0.30, 0.43, 0.60

APPARATUS: TWO DIMENSIONAL COLUMN OF 10 x 300 MM

INSIDE CROSS-SECTION AND 450 MM HEIGHT

MEASUREMENTS:

MINIMUM FLUIDIZATION VELOCITY, BED EXPANSION, BED HEIGHT FLUCTUATIONS, AND BUBBLE SIZE DISTRIBUTION, RISING VELOCITY, AND FREQUENCY AS A FUNCTION OF PRESSURE WITH PARTICLE SIZE AS A PARAMETER.

RESULTS:

THE MINIMUM FLUIDIZATION VELOCITY DECREASES WITH PRESSURE AND THIS EFFECT IS GREATER FOR LARGER PARTICLES. THIS BEHAVIOR IS IN AGREEMENT WITH THE ERGUN EQUATION.

THE BED EXPANDS FASTER WITH EXCESS GAS SPEED AT HIGH PRESSURE THAN AT LOW AND THIS EFFECT IS GREATER FOR LARGER PARTICLES, BUT THE BED HEIGHT FLUCTUATIONS ARE UNCHANGED BY PRESSURE. THESE RESULTS ARE ATTRIBUTED TO AN INCREASE IN THE WIDTH OF BUBBLES WITH PRESSURE RESULTING IN DECREASED BUBBLE VELOCITY AND INCREASED HOLDUP AND THUS BED EXPANSION WITHOUT AN INCREASE IN BED HEIGHT FLUCTUATIONS.

COMMENT:

MEASUREMENT OF BUBBLE CHARACTERISTICS DIFFICULT AND MAY HAVE LARGE ERROR. RESULTS IN 3-D MAY BE DIFFERENT THAN IN 2-D.

HEAT TRANSFER: FLUIDIZED BEDS: RADIATION

REFERENCES: Chen and Chen (1981); Botterill et al (1982)

CHEN AND CHEN

Model for bed-to-wall heat transfer including radiation in a bubbling fluidized bed

\* A portion of the wall is in contact with either a bubble or a "packet" of the solid-gas "emulsion". The emulsion is at bed temperature when it first comes into contact with the wall ; it loses heat to the wall by conduction and radiation before it is swept away.

\* Heat transfer when a bubble is in contact with the wall is treated as radiation between parallel plates. (The wall and the bubble/emulsion interface are the plates.) When the emulsion is in contact with the wall, heat transfer is treated as a combination of conduction and radiative heat exchange between a wall and a scattering, absorbing, and emitting medium.

To apply this model, it is necessary to know:

- \* residence time of an emulsion packet at the wall
- \* fraction of time the wall is in contact with bubbles
- \* absorption and back-scattering coefficients of emulsion packets
- \* effective emissivity of the bubble-emulsion interface
- \* wall emissivity
- \* emulsion packet emissivity.

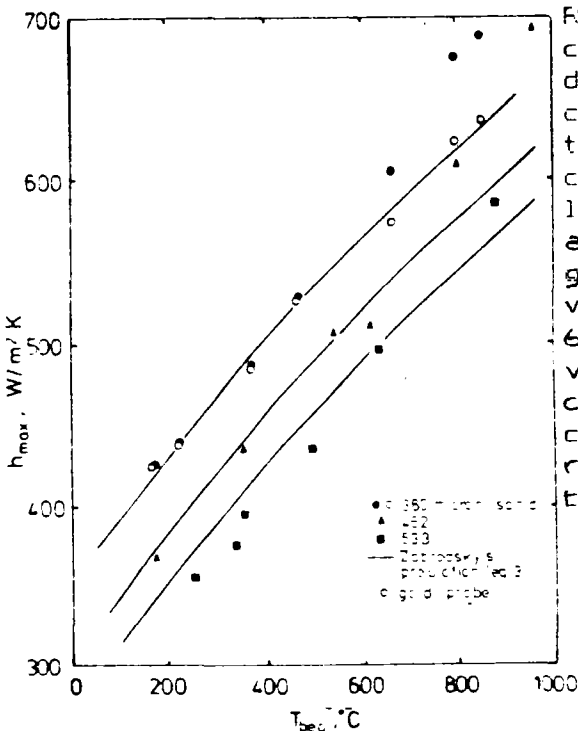
Many of these quantities are not readily available. Thus, it is difficult to use the model.

Using estimates of these values based in part on the properties of fixed beds, Chen and Chen achieved good agreement with the experimental results of an earlier investigator. It is not clear how sensitive the predictions are to the choice of values for the unknown quantities.

BOTTERILL ET AL.

Experiment of the behavior of fluidized beds at high temperatures.

Experimental Conditions: see FLUID MECHANICS: FLUIDIZED BEDS: HIGH TEMPERATURE



Results: Botterill et al. measured heat transfer coefficients from a fluidized bed to surfaces of different emissivities in order to determine the contribution of radiation. They found (see graph) that the measured maximum heat transfer coefficient was well predicted by the empirical correlation of Zabrotsky at low temperatures and when a gold probe was used. (Radiative transfer to a gold surface is small because of the low emissivity of gold.) However, for temperatures above 600 C and materials with reasonably high emissivities, they measured a larger heat transfer coefficient. In some cases, the heat transfer coefficient was as much as 14% higher. No correlation is provided for the radiative contribution.

HEAT TRANSFER IN MULTI-STAGE FLUIDIZED BEDS AT HIGH TEMPERATURES

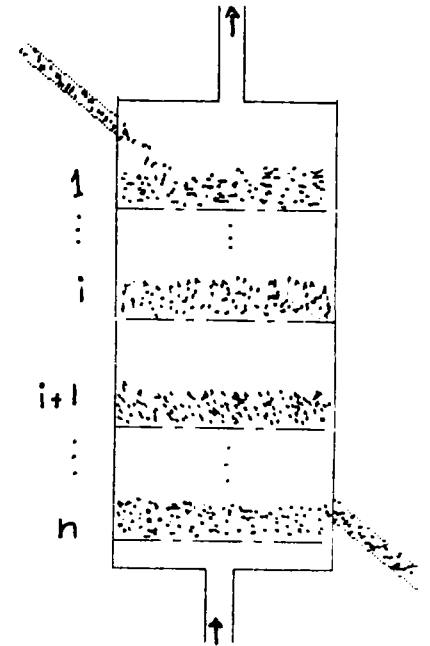
REFERENCES: Feyman and Laguerie (1980); Hood (1981)

IDEAL N-STAGE FLUIDIZED BED

- \* gas and particles leaving a given stage are at the same T
- \* wall losses and radiation are insignificant

$$\text{efficiency } \eta \equiv \frac{T_{g, \text{out}} - T_{p, \text{out}}}{T_{p, \text{in}} - T_{g, \text{in}}} = \frac{\gamma(\gamma^{n-1} - 1)}{\gamma^{n+1} - 1}$$

$$\text{where } \gamma = \frac{\dot{m}_g C_{p,g}}{\dot{m}_p C_{p,p}}$$



AT HIGH TEMPERATURE:

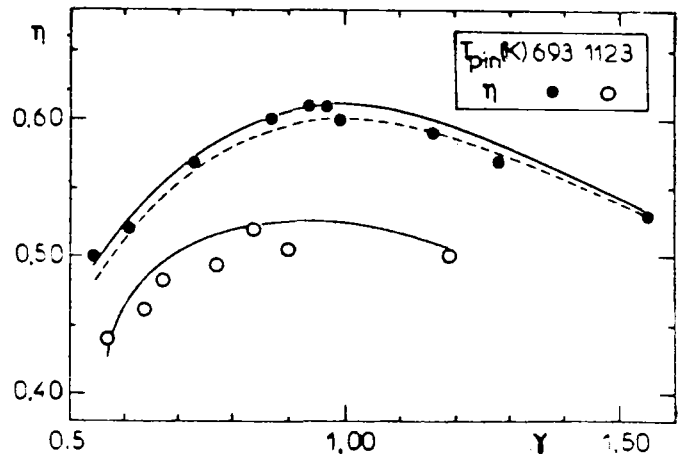
wall losses and radiative backmixing become important

model of Feyman and Laguerie includes:

- \* radiation between upper surface of bed and distributor plate above (black bodies)
- \* conduction through wall

model of Hood includes:

- \* wall in radiative balance
- \* convection between gas and wall
- \* screens (radiation shields)



HEAT TRANSFER: MULTISTAGE FLUIDIZED BEDS: RADIATIVE HEAT TRANSFER

REFERENCES: Peyman and Laguerie (1980); Hood (1981).

PEYMAN AND LAGUERIE MODEL

- \* Gas and particles in a given stage are in thermal equilibrium with each other and with the distributor plate below them.
- \* Radiative heat transfer occurs between the upper face of the fluidized bed and the lower face of the distributor plate above it, which act as black bodies. The wall acts as a refractory.
- \* Radiative heat transfer has reduced the efficiency of a multistage fluidized bed because it has a "backmixing" effect.

$$\dot{m}_p (C_{p,p,i-1} T_{i-1} - C_{p,p,i} T_i) = \dot{m}_g (C_{p,g,i} T_i - C_{p,g,i+1} T_{i+1}) + L_i (T_{wi} - T_s) + R_{i,i+1} (T_i^4 - T_{i+1}^4) - R_{i-1,i} (T_{i-1}^4 - T_i^4)$$

EXPERIMENT

- \* 4-stage heat exchanger
- \* sand cooled by air
- \* scale: diameters of stages: 145 mm, 185 mm  
height of beds: 75mm
- \* particles: sand with mean diameter 0.29mm
- \* temperature: inlet solids at 420 and 850 C
- \* pressure: ambient

HOOD MODEL

- \* modification and extension of the model of Peyman
- \* Convection occurs between the wall and the gas travelling between the fluidized bed and the next distributor plate
- \* The wall does not act as a refractory.
- \* Model can include screens (i.e. radiation shields) below the distributor plates.

EXPERIMENT

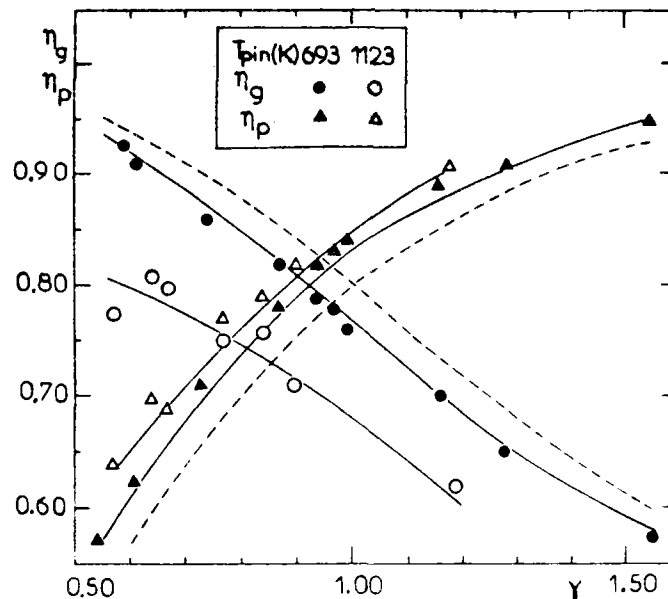
- \* apparatus of Peyman
- \* Only two stages were used when the screens were inserted.
- \* Experiment agrees with the predictions of Hood's model to within 4% for temperature.

Results of Peyman, where

$$\gamma = \dot{m}_g C_{p,g} / (\dot{m}_p C_{p,p})$$

$$\eta_g = (T_{g,out} - T_{g,in}) / (T_{p,in} - T_{g,in})$$

$$\eta_p = (T_{p,in} - T_{p,out}) / (T_{p,in} - T_{g,in})$$





## HEAT TRANSFER: FALLING BED

REFERENCES: Kato et al (1983); Sanderson and Howard (1977)

Sanderson and Howard measured the heat transfer coefficient between heated air and particles and compared their results to the predictions of a simple model of heat transfer from a gas to a falling droplet or particle. They used terminal velocity correlations for single rigid spheres falling through a gas.

## Experimental Conditions:

- \* column dimensions: diameter: 0.15 m; height: 1.5 m.
- \* particles: steel shot with mean diameter 364 microns
- \* pressure: atmospheric
- \* temperature: air inlet temperatures up to 154 C; LMTD up to 53 C
- \* Rig and measurements were simple, and thus more representative of industrial than laboratory conditions.

## Results:

A typical theoretical prediction for the heat transfer coefficient was  $6.3E2$  W/m<sup>2</sup> K. Experimental results agreed reasonably well with the predictions except for some tests in which a high air flow rate produced a flow maldistribution at the column inlet. Poor flow conditions reduced the heat transfer coefficient. In some tests, screens were inserted to increase the residence time of particles in the column. This also made the air flow more uniform. No correlation was provided for the effect of screens.

Kato et al. measured heat transfer rates for the drying of alumina particles in a hindered falling bed heat exchanger.

## Experimental Conditions:

- \* column dimensions: 3 columns used-- d=.105 m, h=.6 m; d=.077 m, h=.4 m; d=.052 m, h=.4 m.
- \* particles: alumina with diameter 832, 527, 480, 317 microns
- \* pressure: atmospheric
- \* temperature: gas inlet: 35 to 95 C; particle inlet: 14 to 35 C.

## Results:

A correlation for the Nusselt number was obtained in terms of the void fraction and the particle Reynolds number.

HINDERED FALLING BED  
FLUID MECHANICS



AT AMBIENT TEMPERATURE AND PRESSURE

TR-2663

REFERENCE: LARGE, GUIGON, AND BERGOUGNON (1981)

EXPERIMENTAL

CONDITIONS:

GAS: AIR

PACKING: 15 x 15 MM METAL PALL RINGS

PARTICLE

MATERIAL: SAND; PARTICLE MEAN DIAMETER (MM) 0.19

MEASUREMENTS: VISUALIZATION OF FLOW PATTERNS, PRESSURE DROP,  
SOLIDS HOLD-UP

RESULTS: THE DRY PRESSURE DROP OF THE PACKING IS A  
SIGNIFICANT PORTION OF THE TOTAL PRESSURE DROP.

AT LOW SUPERFICIAL GAS VELOCITIES SAND TRICKLED  
UNIFORMLY THROUGH THE COLUMN

AT HIGH SUPERFICIAL GAS VELOCITIES SAND MIGRATED  
VERTICALLY AND SAND AND GAS SEGREGATED RADially.

THE NET SOLIDS HOLD-UP INCREASED WITH GAS AND  
SOLIDS FLOW RATE UP TO THE UNSTABLE REGIME.

THE FRACTION OF SOLIDS SUSPENDED IN THE GAS  
WAS CONSTANT AT 0.6 WHEN THE SOLID AND GAS  
FLOW RATES VARIED.

COMMENT: THE HYDRODYNAMICS OF HINDERED FALLING BEDS  
DEPENDS ON BED DIAMETER.

THE ANALOGY BETWEEN SOLID PARTICLE/GAS FLOW  
AND LIQUID/GAS FLOW IS VERY LIMITED BECAUSE  
THE SOLID PARTICLES LACK SURFACE TENSION.

## HEAT TRANSFER: FALLING CLOUD

REFERENCE: Sanderson and Howard (1977)

Sanderson and Howard measured the heat transfer coefficient between heated air and particles and compared their results to the predictions of a simple model of heat transfer from a gas to a falling droplet or particle. They used terminal velocity correlations for single rigid spheres falling through a gas.

## Experimental Conditions:

- \* column dimensions: diameter: 0.15 m; height: 1.5 m.
- \* particles: steel shot with mean diameter 364 microns
- \* pressure: atmospheric
- \* temperature: air inlet temperatures up to 154 C; LMTD up to 53 C
- \* Rig and measurements were simple, and thus more representative of industrial than laboratory conditions.

## Results:

A typical theoretical prediction for the heat transfer coefficient was  $6.3E2 \text{ W/m}^2 \text{ K}$ . Experimental results agreed reasonably well with the predictions except for some tests in which a high air flow rate produced a flow maldistribution at the column inlet. Poor flow conditions reduced the heat transfer coefficient. In some tests, screens were inserted to increase the residence time of particles in the column. This also made the air flow more uniform. No correlation was provided for the effect of screens.

## FEEDERS



TR-2663

REFERENCES: GUZDAR AND HARVEY (1982), HAWRYCH (1981)

APPLICATIONS: FEEDING COAL AND BIOMASS TO HIGH PRESSURE GASIFIERS

### TYPES:

LOCK HOPPERS - LARGE BINS WITH VALVES TO SHUT OFF SO THAT THEY CAN BE PRESSURIZED WITH A GAS AFTER FILLING.

PISTONS - SMALL LOCK HOPPERS WITH A PISTON REPLACING COMPRESSED GAS.

### POCKETS (TWO TYPES):

ROTARY - SMALL LOCK HOPPERS ON A SHAFT WITH VALVES REPLACED BY SEAL BETWEEN BLADES AND HOUSING.

LINEAR - SMALL LOCK HOPPERS WITH HIGH PRESSURE AIR DISPLACED BY WATER.

### SCREWS (TWO TYPES):

EXTRUDERS - A COMPACTED PLUG OF FEED MATERIAL IS FORMED AT LOW SPEED.

COMPRESSORS - A LOOSE PLUG OF FEED MATERIAL IS FORMED AT HIGH SPEED.

### INERTIAL PLUGS (TWO TYPES):

GRAVITATIONAL - A MOVING BED OF FEED MATERIAL HIGH ENOUGH TO WITHSTAND  $\Delta P$

CENTRIFUGAL - A LOOSE PLUG OF FEED MATERIAL IS FORMED BY CENTRIFUGAL FORCE.

RAM - A COMPACTED PLUG OF FEED MATERIAL IS FORMED AND PUSHED INTO THE HIGH PRESSURE REGION.

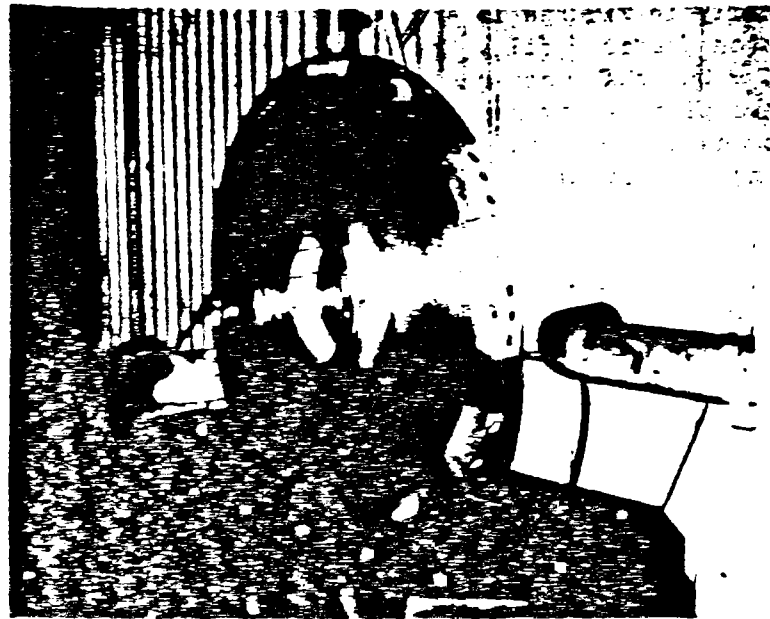


FIGURE 13. ROTOR

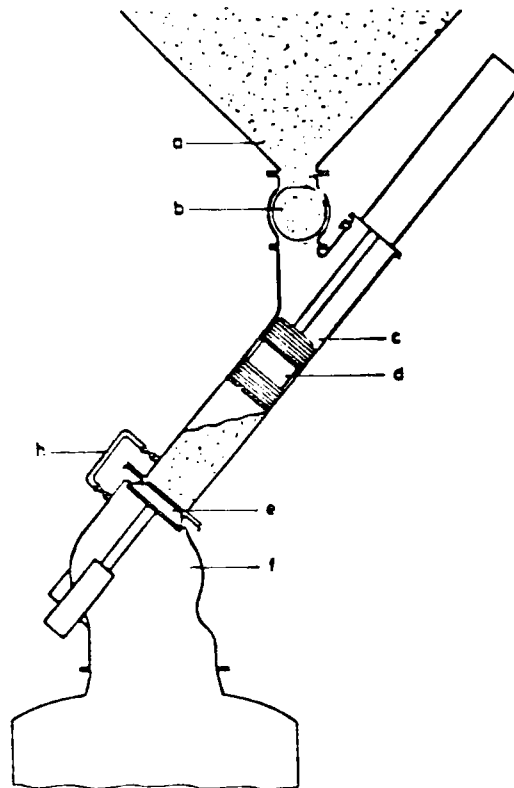


FIGURE 14. SCHLEPPER PISTON FEEDER

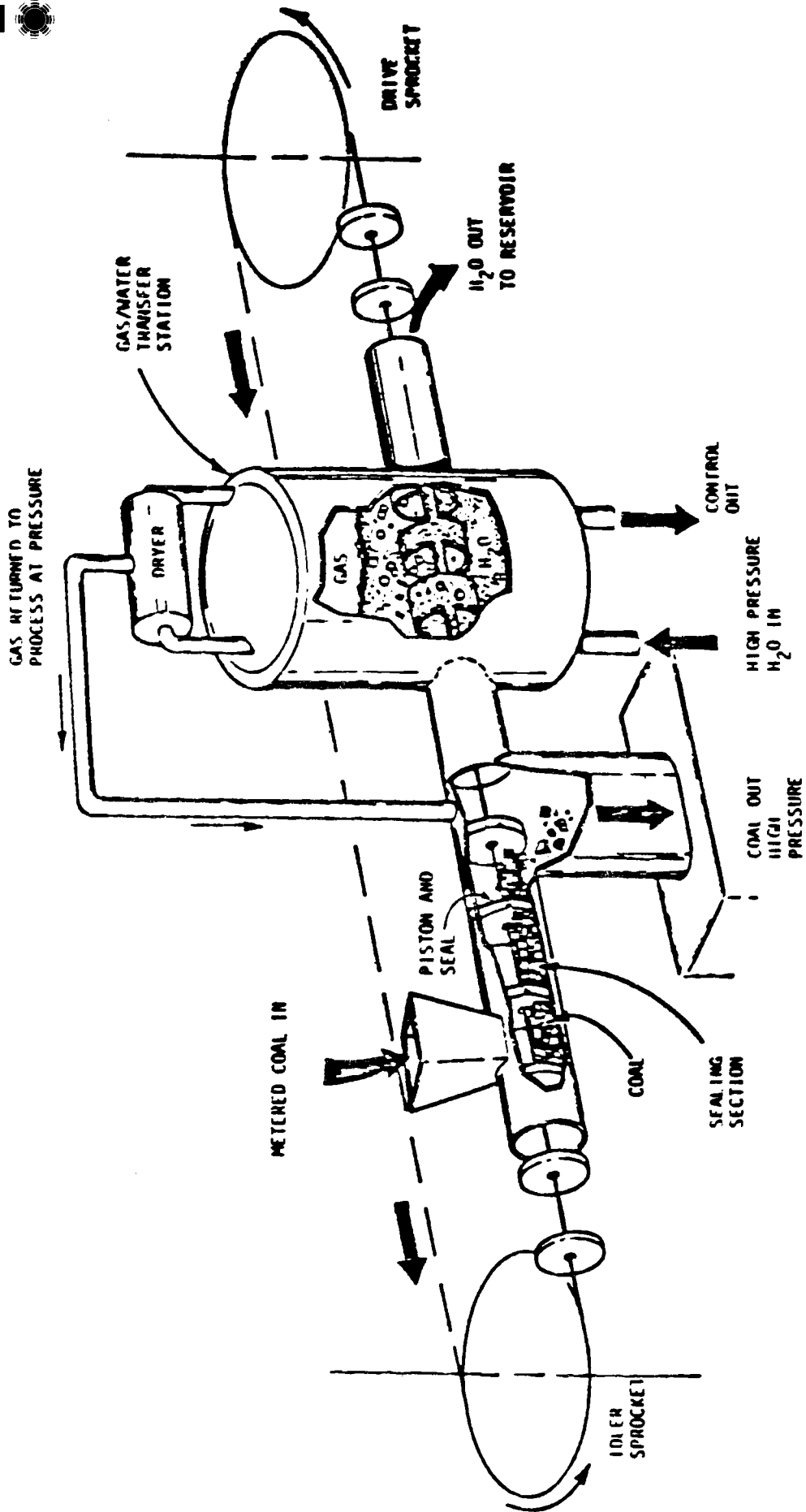


FIGURE 20. CUTAWAY VIEW

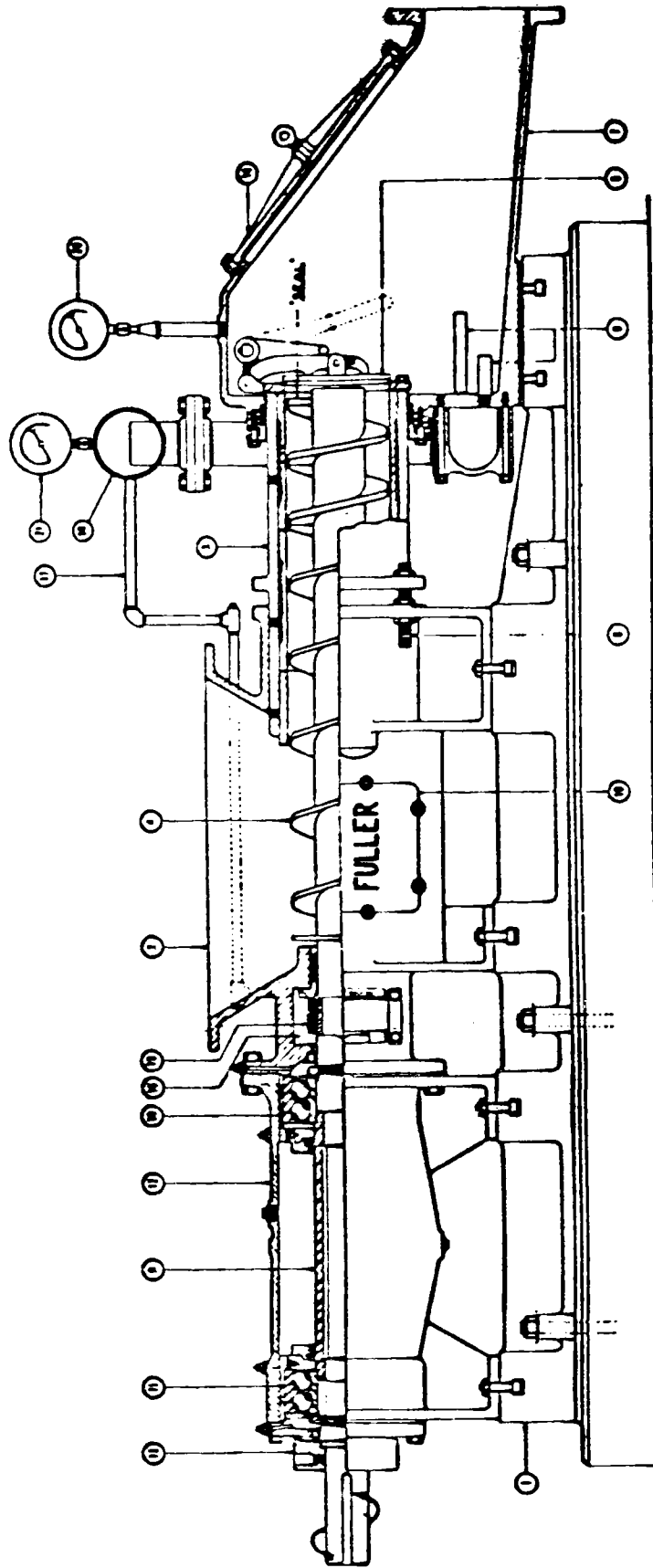


Figure 6. Fuller-Kinyon Pump

with hydrogen (not shown) the low end of the specific power range is reached by about 10 tons/hr. For high mass flow or light gas, performance for biomass should approach that for coal. Figure 12 shows a sketch of the Lockheed Kinetic Extruder and Figure 13, a photograph of the rotor.

Piston Feeder

A piston feeder is conceptually the same as a mini-lock hopper with a displacer piston to conserve the high pressure gas. Many types of piston feeders have been developed only three of which are described here briefly.

A Schlepper type piston feeder (14) is being developed by Lurgi to provide semicontinuous feed to its gasifier and to minimize gas compression costs. Figure 14 shows a schematic of this feeder. The cylinder is filled with coal from a bunker with the piston on its upper end position and the bottom outlet closed. It appears that a limited charge must be metered in order to provide smooth piston passage past the fill port. The piston then moves down to seal the cylinder compartment and hold the coal drops into the reactor. The piston is forced down to the lower cylinder end displacing almost all coal and gas from the cylinder. Bottom valve closure and piston retraction complete the feed cycle. A demonstration feeder is currently being built by Lurgi and is expected to be tested shortly (14).

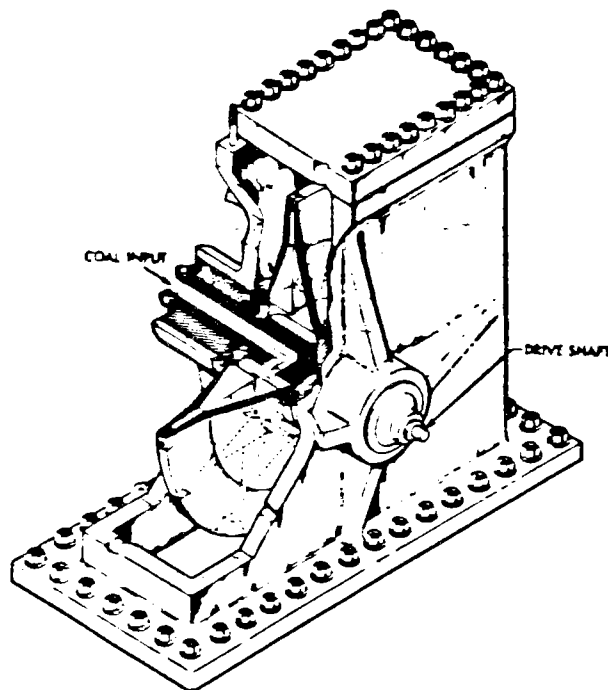


FIGURE 12. LOCKHEED KINETIC EXTRUDER



# Sand/Air Heat Exchanger Feeder Ratings

E = Excellent    G = Good    F = Fair    P = Poor    U = Unacceptable

Requirement Type	Controlled And Metered Feed Rate	Pressure Seal To 20 Atmospheres	Handle Particles of 1.0 to 0.1 mm. Diameter	Economic Operation	Low Capital Cost	Reliable And Safe Operation	Potential To Operate At 1000° C
Lock Hopper 11	Intermittent, Requires Pressurized storage Hopper P	Lurgi Pilot Plant Unit Operated To 1200 psi E	Can Handle Any Size Up To 4" small particles wear valves F	Pressurized Air Requirement Leads To High Operational Cost U	Factor of 2 Greater Than other Types U	Years of Operational Experience, Problems with Valves and Holdup F	Hopper Adaptable To High Temperature, Valves may not be F
Piston 22	Multiple Pistons Smooth Feed Rate Compared To Hopper F	Ingersoll-Rand Unit Operated To 500 psi E	Any size, up to 4" but small particles may cause wear G	Mechanical Action Leads To Low Specific Power E	A few percent less than screw at 300 psi G	Under Development. Can be Designed To Be Fail Safe G	Piston Heads and Cylinder adaptable to high temp. G
Pocket Rotary	Quasicontinuous Controllable G	Limited to 120 psi by Blade Leakage U	Small particles will wear blades F	requires pressurized air P	Fairly simple Construction F	Years of operation experience, blade wear a problem F	Rotor can be adapted G
Linear	Quasicontinuous controllable over wide range G	Foster-Miller unit operated to 1000 psi E	small particles will wear plug F	pressurized air replaced by water E	15% more than screw or piston F	500 hours of Testing. Fail Safe G	Use of water unsuitable at high temp. U
Screw	Continuous, Controllable over wide range E	Fuller-Kinyon Pump Operated to 75 psi U	Can be designed to handle small particles G	High speed rotation leads to medium operating expense F	30% more than Centrifugal Inertial Plug G	Internal "Flapper" Valve Can Provide Fail Safe Design F	screw expensive to adapt, Flapper valve may give trouble F
Inertial Gravitation	Continuous controllable E	Limited By Height of Column G	very small particles without wear E	mechanical, Listening is Efficient E	Simplicity Leads To Low Cost E	Years of Low DP Experience Not Fail Safe F	Cylinder easily adaptable G
Centrifugal	Continuous, Controllable over a range E	lockheed unit Tested To 400 psi E	very small particles with little wear E	Low specific power below 500 psi G	Simplicity Leads To Low Cost E	100 Hours of Testing, Not Fail Safe P	Rotor and Feed Pipe adaptable G



## AIR-SOLIDS SEPARATORS: AIR QUALITY REQUIREMENTS FOR THE TURBINE

REFERENCE: Boericke et al. 1977

Evaluation of the problem of turbine blade erosion by particles, directed towards power generation from pressurized fluidized bed combustion. Gases from pressurized fluidized bed combustors (PFBC) have similar temperature (790 to 950 C) and pressure (approx. 16 atm.) to the air leaving the heat exchanger in our application. PFBC turbine blade environment is somewhat harsher because the combustor gases are corrosive. Boericke et al. based their recommendations for allowable particulate concentration on several tests, the conditions of which are summarized below:

TEST	PRESSURE	TEMPERATURE	LENGTH OF TEST
coal-fired locomotive	4.8 atm.	?	2000 hrs
GE erosion rig	1 atm.	480-870 C	600 hrs
PFB cascade	5.6 atm.	840 C	2x1000 hrs
Cat-cracker	3 atm.	650 C	used in industry

## RESULTS

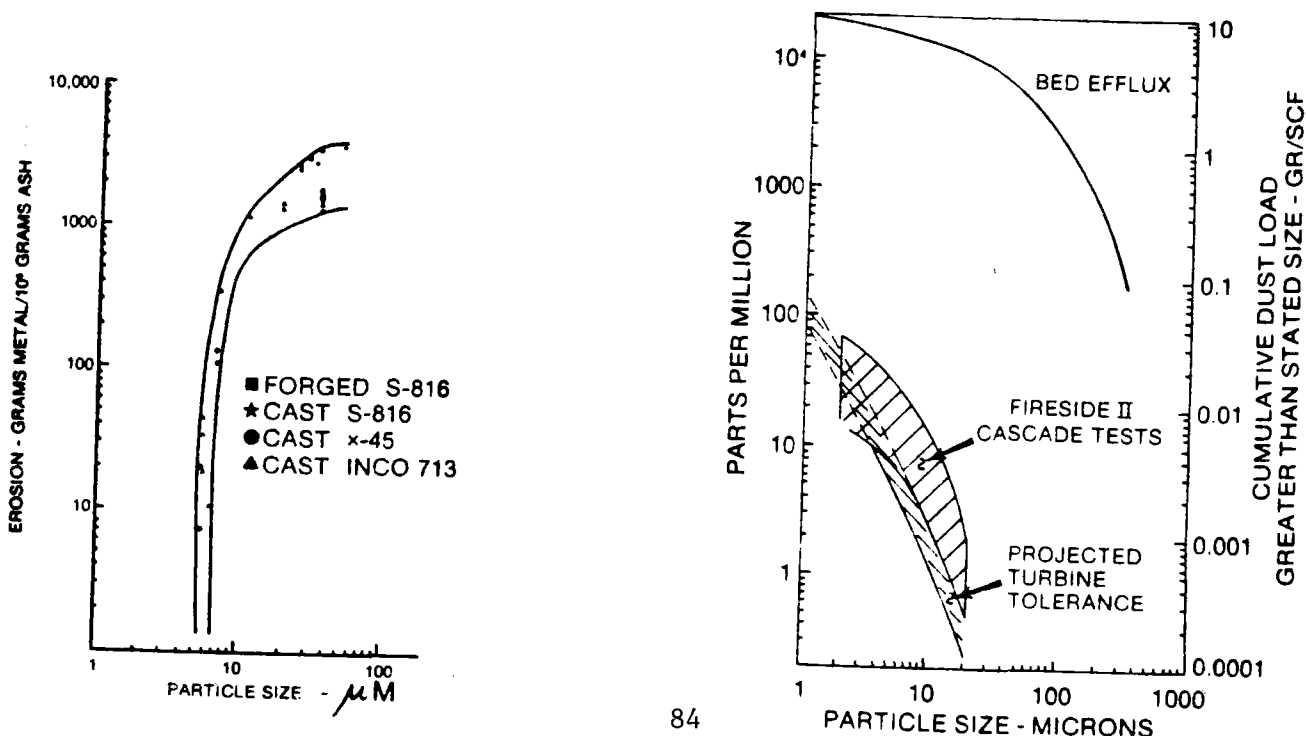
\* Erosion increases rapidly with particle size. Particles smaller than 8 microns do not cause measurable erosion.

\* Cat-cracker experience, which involves erosion by a highly abrasive catalyst similar to the particulate matter of our heat exchanger, indicates somewhat higher allowable particle concentrations than the combustion tests. However, materials available for turbine blades at those temperatures are more erosion-resistant than high-temperature materials.

In applying the results of these tests to the particular turbine of interest, Boericke noted that:

\* Increasing the pressure increases the particle flowrate for a given concentration.

\* Erosion rate is proportional to  $V^n$ , where  $V$  is the relative velocity of the particles and the blade, and  $n$  is a constant between 2 and 5.  $n \approx 2.3$  for some materials of interest.



SEPARATORS

REFERENCES: Boericke et al.(1981); Brooks et al.(1981); Casal and Martinez-Benet (1983); Fraas et al.(1979); Keairns et al.(1980); Mathers et al. (1980); Parker et al.(1981); Rennhack (1982); Strauss (1975); Westinghouse

CYCLONES:

- \* have been used in series to clean gases from pressurized fluidized bed combustors.
- \* last cyclone must be high-efficiency (i.e.small).
- \* most data on collection efficiency must be extrapolated to high temperature and high pressure.

ELECTROCYCLONES:

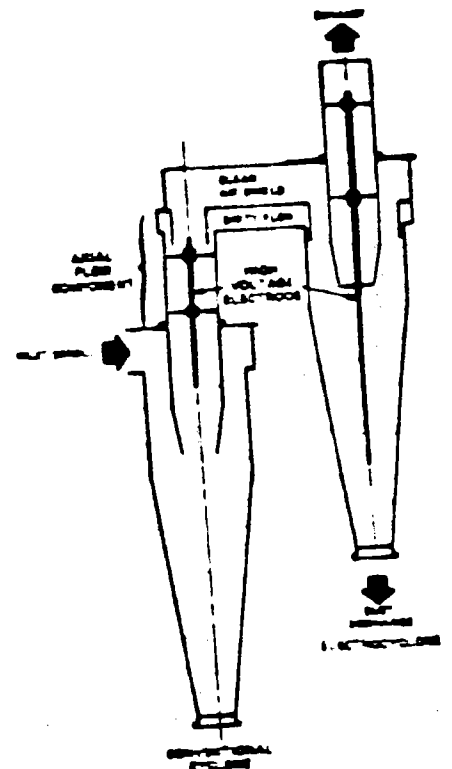
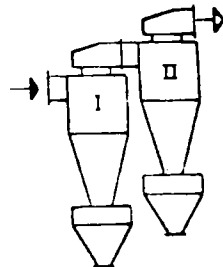
- \* not yet tested at full scale.
- \* dust is charged, then separation in cyclone is improved by applying electric field.
- \* high-efficiency electrocyclones can be larger than equivalent conventional cyclone.

FILTERS:

- \* at present not available for our temperatures.
- \* mineral-fiber filters are being developed.

PACKED BEDS:

- \* dirty gases pass through packed or moving bed of granular material.
- \* have been used at 500 C.
- \* temperature range can probably be extended.

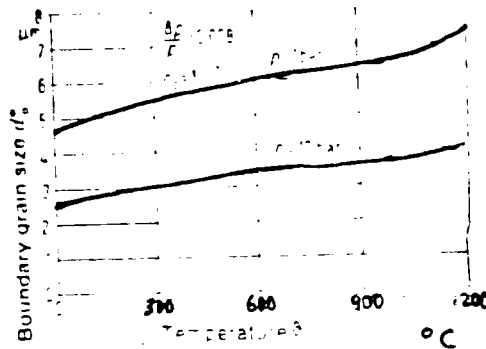


**AIR-SOLIDS SEPARATORS: CYCLONES: EFFECT OF TEMPERATURE AND PRESSURE**

REFERENCES: Parker et al. (1981); Rennhack (1982)

Information on cyclone efficiency must be extrapolated to our extreme temperature and pressure conditions. There is contradictory evidence on the effect of increasing temperature and pressure.

Rennhack predicts that cyclone collection efficiency will decrease with an increase in temperature or pressure. His prediction is based on the effect of temperature and pressure on gas properties and thus on the drag force acting on particles. Collection efficiency in cyclones decreases when the drag force increases, because drag acts against the centrifugal force that drives the particles outward and separates them from the air. The graph below shows how the minimum separable particle diameter varies with temperature and pressure.

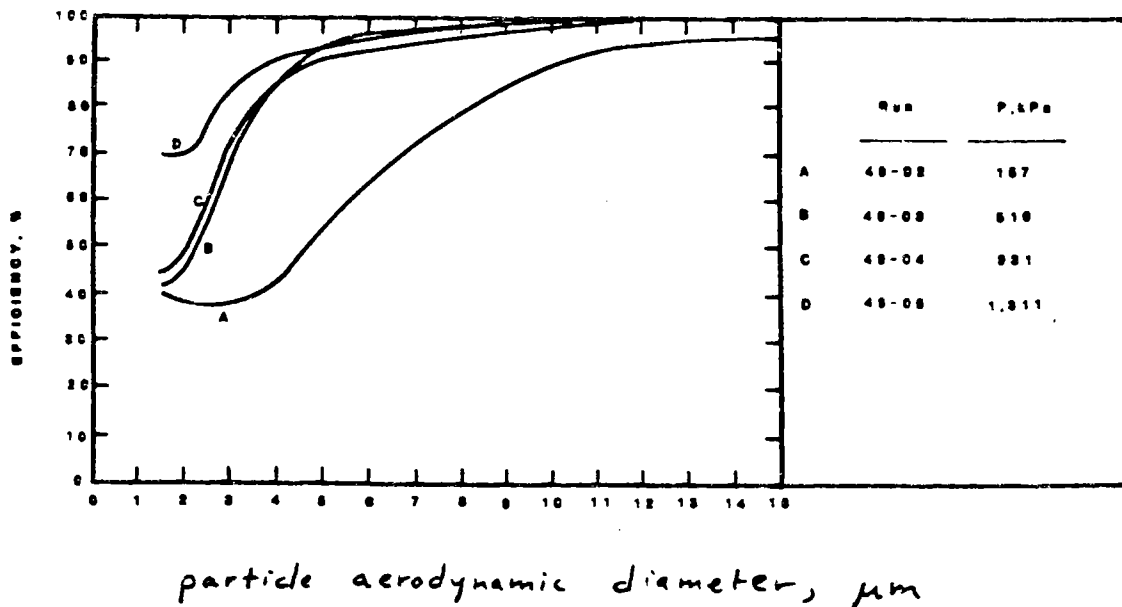


Parker et al. performed experiments and compared their results to the theoretical predictions of Leith and Licht.

Experimental conditions:

- \* 2-in cyclone
- \* inlet temperatures from ambient to 693 °C
- \* pressures from atmospheric to 2530 kPa (25 atm)

Results: Collection efficiency decreased with increasing temperature and increased with increasing pressure. (See graph below.) The pressure dependence was contrary to theory, which predicted that pressure would have little effect. Parker et al. present an empirical correlation but no theoretical explanation for their results.



AIR-SOLIDS SEPARATORS: ELECTROCYCLONES

REFERENCE: Boericke et al. (1981)

Collection efficiency of conventional cyclones decreases as size increases. Thus, high-efficiency cyclones required for the final stage of clean-up for pressurized fluidized bed combustor gases are small (approx. 10 in. diameter). High-efficiency electrocyclones can be much larger, since their efficiency depends on voltage rather than size. Boericke et al. describe how the electrocyclone works and report on the results of an analytical model and experiments on an 18-inch electrocyclone. GE is now involved in the design and testing of larger models.

In the drawing, an electrocyclone is shown following a conventional cyclone. Dust particles are charged as they leave the first cyclone. Inside the electrocyclone, they are pushed to the wall by an applied electrical force as well as by the centrifugal force acting in all cyclones.

Force balance:

$$3\pi\mu d_p U_w = \frac{1}{3}\pi d_p^3 \rho_p \frac{V_t^2}{D} + q E_a$$

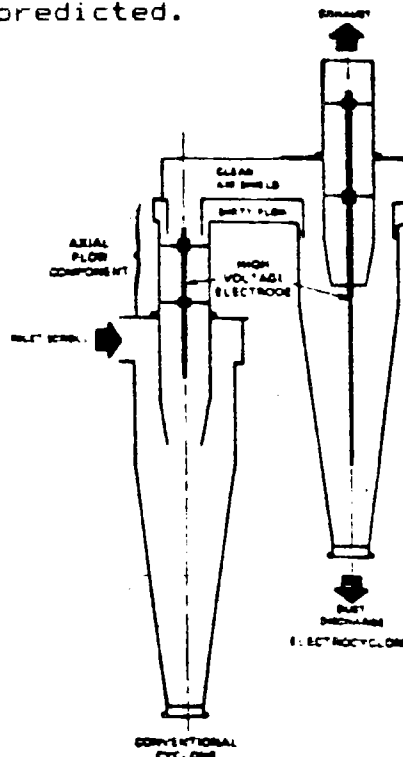
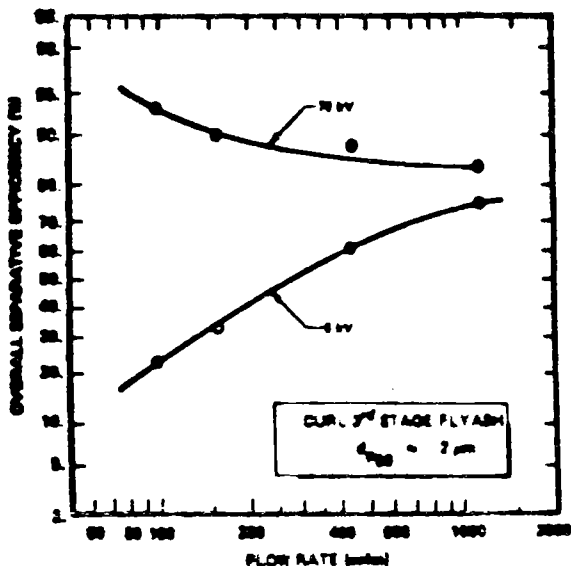
drag                      centrifugal                      electrostatic

Analytical model:

Electrocyclone is represented by a simplified two-dimensional model divided into five zones. Particle migration from zone to zone is expressed in a set of coupled differential equations. An analytical solution has been found, and is presented in another paper.

Experiment:

- \* 18-in. electrocyclone operating at ambient temperature and pressure
- \* Results agreed very well with the predictions of the model for low flowrates, where the electrostatic force is dominant. For higher flowrates, the measured efficiency was lower than predicted.



## INSULATION

## REQUIREMENTS:

- \* withstand 1000 C
- \* abrasion resistant

## DESIGN:

- \* internal insulation, probably with an innermost abrasion-resistant layer.
- \* pressure vessel shell
- \* external insulation.

## MANUFACTURERS:

- \* Babcock and Wilcox
- \* Carborundum
- \* Johns-Manville

## COMMENTS:

- \* Our temperature requirements are not unusual.
- \* Since abrasion depends on particle velocity, size, and impact rate, as well as on particle and insulation hardness, manufacturers were reluctant to predict erosion rate. However, they did not think that our application would involve exceptional erosion problems.
- \* High-density insulation is more appropriate for abrasion resistance, but is a poorer insulator and more subject to thermal shock than low-density insulation. It may be necessary to control warm-up to guard against thermal shock.
- \* High-density insulation is available for our temperatures with a hardness rating of 9 (where diamond =10).



THERMOELECTRON CORP.  
Waltham, MA 02254. 617-890-8700  
Dr. Bill Cole

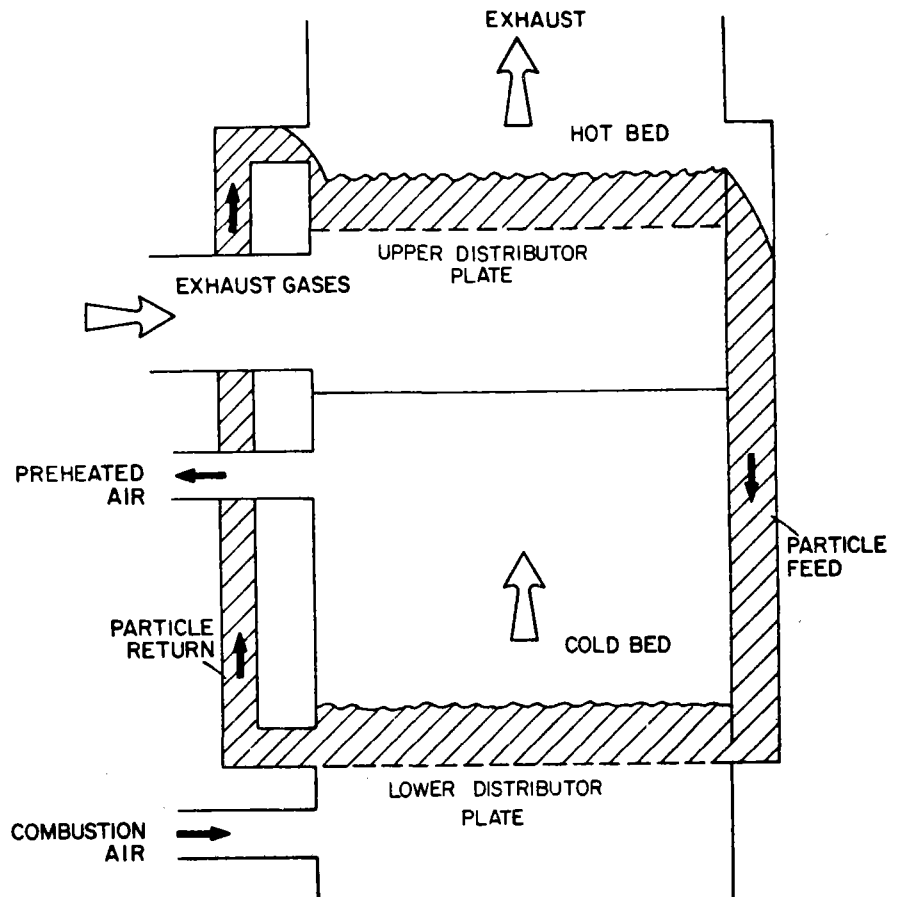
ThermoElectron is working on a particle-air heat exchanger for recovering waste heat from flue gases and preheating clean air for combustion. This work is sponsored by DOE Idaho Operations Office. The results will be in the public domain once reports have been approved by DOE. Until then, there is little performance information available.

#### Experimental Conditions:

- \* scale: apparatus has cross-sectional area 0.46 m.
- \* particles: alumina
- \* temperature: hot gases enter at 1090 C; air is preheated to 540 C. (The preheat temperature is the highest desired for industrial combustors. The heat exchanger can be modified to produce hotter air.)
- \* pressure: atmospheric

#### Design:

- \* Exhaust gases enter the upper chamber and fluidize a bed of alumina particles, transferring heat to them.
- \* The particles travel to the lower chamber, where they are fluidized by cold combustion air. The air is heated and leaves the chamber.
- \* The particles are carried pneumatically back to the upper chamber. This leg acts as a heat exchanger too, since heat is transferred to the air that carries them upward.



**ECONOTHERM**

15 Cedar Lane (P.O. Box 309)  
 Englewood, NJ 07631. 201-567-9767  
 Mr. J. Paul Vandenhoeck

REFERENCE: Vandenhoeck

Econotherm has designed gas-particle-air heat exchangers that are in use for waste heat recovery in the aluminum and foundry industries.

Operating conditions:

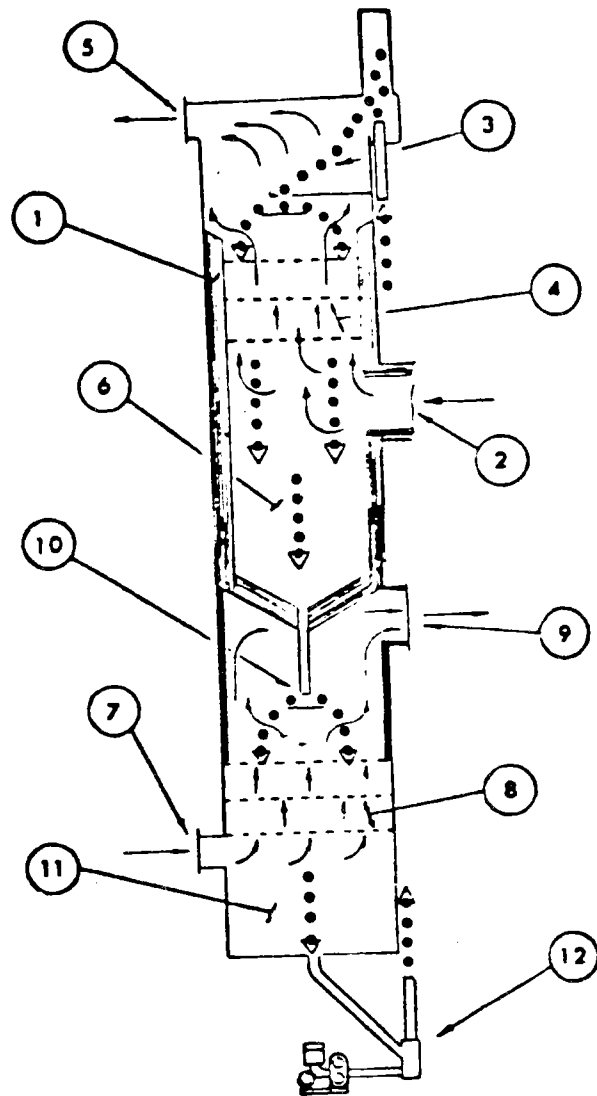
- \* scale: full-scale
- \* particles: sand or ceramic pellets
- \* temperature: inlet gas temperatures up to 1100 C
- \* pressure: atmospheric

Design:

- \* two chambers
- \* Particles are heated by hot flue gases in the upper chamber.
- \* Particles heat clean air in the lower chamber.
- \* Particles form a seal between the two chambers. From the bottom of the second chamber, they are carried pneumatically back to the top of the heat exchanger.
- \* Heat transfer occurs in shallow fluidized beds and, apparently, in a free-falling section.

Comments:

- \* The heat exchanger is refractory-lined. Vandenhoeck reports that abrasion was not noticeable in a foundry waste-heat heat exchanger of this type even after two years' operation.
- \* Sand is satisfactory for relatively low-temperature applications, but it sinters at high temperatures.





THERMAL SYSTEMS  
 Woburn, MA. 617-933-7880  
 Dr. Andy Syska

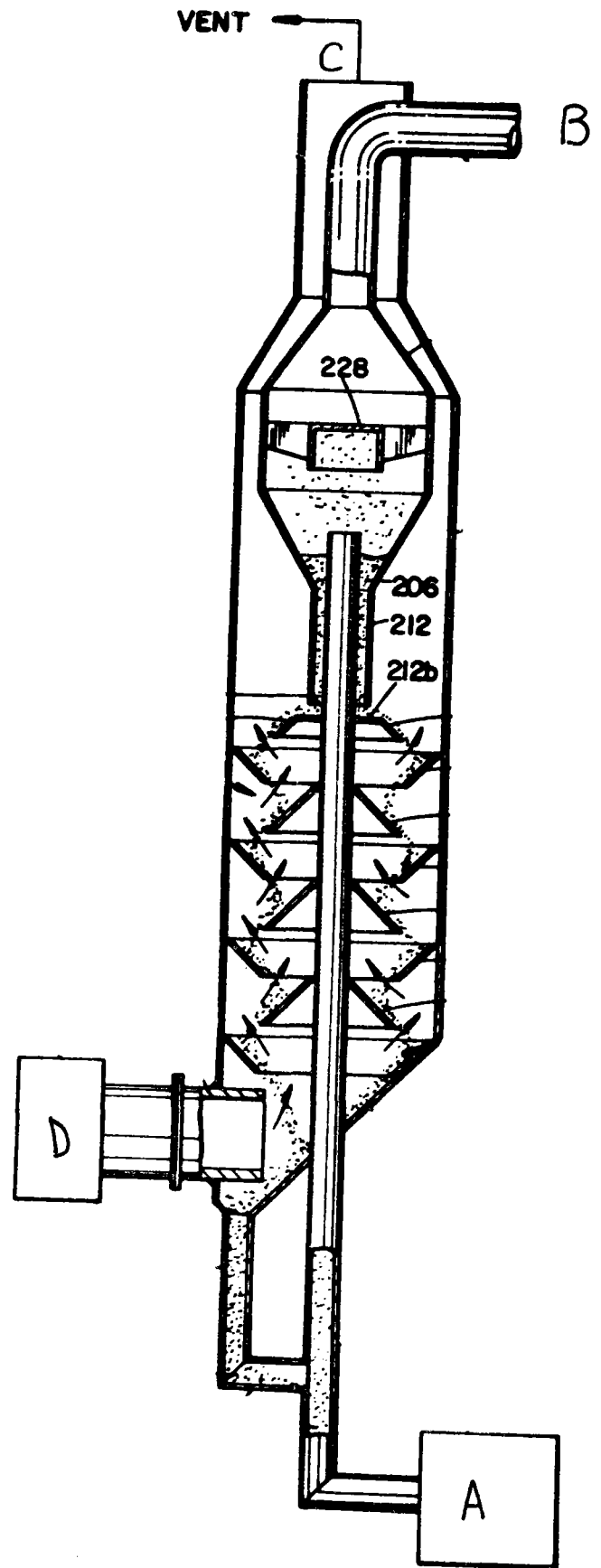
REFERENCE: Massey et al. (1979)

At Thermal Systems, Dr. Syska has done extensive experimental work on particle-air heat exchangers for waste heat recovery. To date, this work was done under contract to other companies and is proprietary. However, sometime in 1984, some of Thermal Systems' concepts will be developed by ThermoElectron with funding from DOE. The results of those investigations will be in the public domain.

- Tests performed at Thermal Systems:
- \* scale: working prototypes on industrial scale
  - \* particles: from 200 to 1200 microns
  - \* temperature: air preheated up to 1090 C.
  - \* pressure: atmospheric.

The reference to Massey et al. (a patent) gives information about a heat exchanger invented at Thermal Systems a few years ago. According to Dr. Syska, this design would no longer be recommended.

- \* Hot dirty gas enters the device at A and pneumatically conveys the particles upward as it transfers heat to them.
- \* The gas and particles enter a larger chamber, in which the particles settle. The gas moves upward and out of the system at B.
- \* The particles form a seal between the chamber and a larger chamber that surrounds it. They fall into the larger chamber and then fall through a system of baffles, exchanging heat with a stream of clean air.
- \* The clean air enters the heat exchanger at D and leaves, preheated, at C. The particles travel in a closed loop.
- \* Note that the particles are heated in cocurrent heat exchange; they are cooled in countercurrent heat exchange.



**TUNZINI-NESSI ENTERPRISES**  
 1 Place Honore de Balzac  
 95108 Argenteuil-Cedex, France  
 3-411-5454

**REFERENCES:** Meunier (1978 a and b);  
 Meunier et al. (1983)

Tunzini-Nessi is working with researchers at the Universite de Technologie de Compiègne on the development of the packed bed heat exchanger. Applications include flue gas waste heat recovery, regenerating foundry sand, and obtaining useful heat by burning mine tailings.

**Experimental conditions:**

- \* scale: 0.3-m-diameter column at the university; demonstration plant in progress.

- \* temperature: 500 C at the university; 1200 C in the demonstration plant

- \* pressure: ambient

**Design:**

- \* countercurrent heat exchanger

- \* layers of packing increase particle residence time and improve the uniformity of both particle and gas flow.

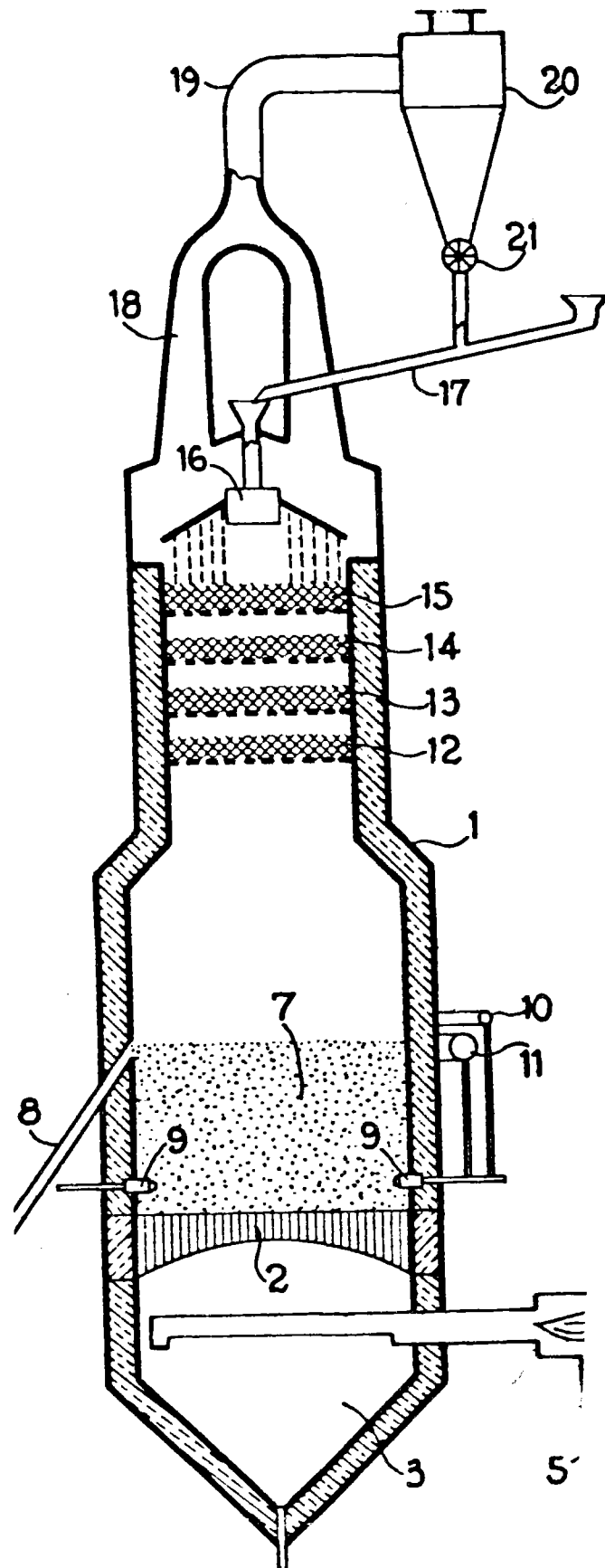
- \* fluidized bed is used for the hottest contacting at the bottom, since the packing and packing supports can not resist very high temperatures (1500 C).

**Note:**

The device shown is for heating particles with hot flue gases. A device for heating gases with hot particles would have a slightly different design:

- \* The fluidized bed would be omitted or placed at the top of the column.

- \* The diameter of the colmun would be larger at the top than the bottom beacuse of the change in density of the gas.



THE FALLING CLOUD HEAT EXCHANGER  
(STONE PLATT FLUIDFIRE LTD.)

REFERENCES: SAGOO 1981 A AND B, SAGOO 1979, EAVES 1978

APPLICATION: HEAT RECOVERY FROM HOT CONTAMINATED GASES  
FLOWING UP A CHIMNEY

OPERATING  
CONDITIONS:

GAS: AIR

GAS INLET TEMPERATURE: (U. OF ASTON) 100, 160  
215°C (PILOT PLANT) 200, 300°C

GAS PRESSURE: AMBIENT

PARTICLE MATERIAL: ALUMINA, STEEL

PARTICLE DIAMETER: 0.40 MM, 0.38 MM

TERMINAL VELOCITY: 2.62 M/S, 5.27 M/S

COLUMN DIMENSIONS: (U. OF ASTON) 0.3 M  
DIAMETER X 1.9 M HIGH (PILOT PLANT) 1.1 M  
DIAMETER X 4.3 M HIGH

TEST RESULTS: MEASURED HEAT RECOVERY RATE, HEAT TRANSFER  
COEFFICIENT, AND THERMAL EFFICIENCY FOR BENCH  
SCALE MODEL (U. OF ASTON) AND PILOT PLANT.  
PUBLISHED RESULTS FROM THE BENCH SCALE MODEL  
ARE ONLY QUALITATIVE. RESULTS FROM THE PILOT  
PLANT WERE LIMITED BY THE PLANT CAPACITY.

COMMENTS: REFERENCED REPORTS ARE OF VERY POOR TECHNICAL  
QUALITY, BUT SOME PRACTICAL LESSONS CAN BE  
LEARNED FROM THE RECORDED EXPERIENCE OF BUILDING  
AND OPERATING A PILOT PLANT.

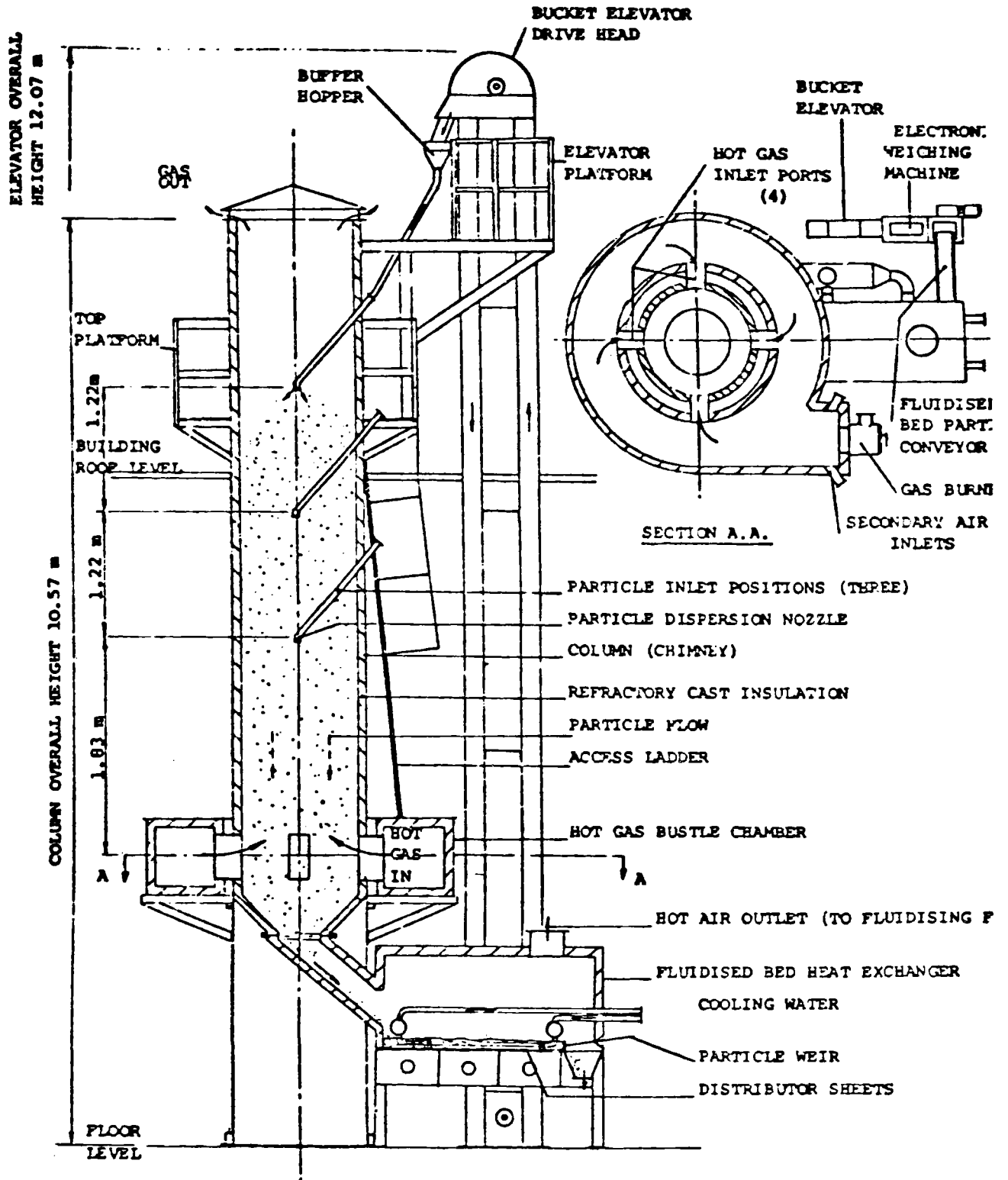


FIG 1: THE FALLING CLOUD HEAT EXCHANGER - COMMERCIAL PILOT PLANT

## SOURCES IN LITERATURE SEARCH

## ENGINEERING INDEX-- 1982-- topics such as:

- heat recovery
- heat exchangers
- heat transfer
- fluid mechanics

## CURRENT CONTENTS, Engineering Series, VOL.14 (1983)

## JOURNALS NOT COVERED BY CURRENT CONTENTS, such as:

- German Chemical Engineering
- International Chemical Engineering
- Applied Energy

## SURVEYS, such as

- Sandia Particle Library Listing (updated 4/19/83)
- Geldart's Survey of Gas Fluidization Research

## CONVERSATIONS with:

- Dr. M. Bergougnou (University of Western Ontario)
- Dr. T. Reed (SERI)
- Dr. J. Taborek (Science Applications, Inc.)
- Dr. W. Thielbahr (DOE Idaho Operations Office)

## COMPUTER SEARCHES IN COMPENDEX (equivalent to Engineering Index 1973-83) -- topics such as:

- moving bed/ heat transfer
- falling/ heat exchanger
- direct contact/ heat exchange/ particle/ gas

## CURRENT ENERGY PATENTS 1982 and 1983.

**APPENDIX C. SAMPLE CALCULATIONS FOR THERMAL ANALYSIS OF  
SHELL-AND-TUBE HEAT EXCHANGER**

**Shell-Side Heat Transfer Coefficient**

Given:

$$\begin{aligned} \rho_s &= \text{particle density} = 4000 \text{ kg/m}^3 \\ V_o &= \text{bed velocity} = 0.15 \text{ m/s} \\ \rho_b &= \text{bulk density} = 2400 \text{ kg/m}^3 \\ D_o &= \text{tube outside diameter} = 0.0272 \text{ m} \\ K_s &= \text{thermal conductivity of alumina} = 8 \text{ W/m K} \\ c_{ps} &= \text{specific heat of alumina} = 837.2 \text{ J/kg K} \\ d_m &= \text{mean size of particles} = 0.5 \times 10^{-3} \text{ m.} \end{aligned}$$

From Eq. 5-7 (Kurochkin 1966),

$$Nu_p = 0.0214 P_e^{0.21} \left( \frac{D_o}{d_m} \right)$$

with:

$$P_e = \frac{V_o C_{ps} \rho_b D_o}{K_p}$$

$$P_e = \frac{(0.15)(837.2)(2400)(0.0272 \text{ m})}{8} = 1025$$

$$Nu_p = 0.0214 (1025)^{0.21} \left( \frac{0.0272}{0.5 \times 10^{-3}} \right) = 5.0$$

$$H_p = \frac{Nu_p K_p}{D_o} = \frac{(5.0)(8)}{0.0272} = 1468 \text{ W/m}^2 \text{ K} \approx 250 \text{ Btu/h ft}^2 .$$

**Tube-Side Heat Transfer Coefficient (Smooth Tubes)**

Given:

$$\begin{aligned} Re_a &= \text{air Reynolds number} = 40,000 \text{ (varied)} \\ Pr_a &= \text{air Prandtl number} = 0.72 \\ F &= \text{heat transfer adjustment factor} = 1 \text{ (smooth tubes)} \\ D_H &= \text{hydraulic diameter} = 0.0222 \text{ m} = D_i \\ K_a &= \text{air thermal conductivity} = 0.0334 \text{ W/m K.} \end{aligned}$$

From Eq. 5-5,

$$Nu_a = 0.023 Re_a^{0.8} Pr_a^{0.4} F$$

$$Nu_a = (0.023)(40,000)^{0.8} (0.72)^{0.4} = 97$$

$$H_a = \frac{Nu_a K_a}{D_H}$$

$$H_a = \frac{(97)(0.0334)}{0.0222} = 146 \text{ W/m}^2 \text{ K} .$$

### Overall Heat Transfer Coefficient

Given:

$$T_{in,p} = \text{particle inlet temperature} = 1000^\circ\text{C}$$

$$T_{out,p} = \text{particle outlet temperature} = 581^\circ\text{C}$$

$$T_{in,a} = \text{air inlet temperature} = 150^\circ\text{C}$$

$$T_{out,a} = \text{air outlet temperature} = 970^\circ\text{C}$$

$$H_a = \text{tube-side heat transfer coefficient} = 146 \text{ W/m}^2 \text{ K}$$

$$H_p = \text{shell-side heat transfer coefficient} = 1413 \text{ W/m}^2 \text{ K}$$

$$R_p = \text{shell-side fouling resistance} = 0.0001 \text{ m}^2 \text{ K/W}$$

$$R_a = \text{air-side fouling resistance} = 0.0003 \text{ m}^2 \text{ K/W}$$

$$Y_w = \text{wall thickness} = 2.5 \times 10^{-3} \text{ m}$$

$$K_w = \text{wall thermal conductivity} = 11 \text{ W/m K}.$$

Compute  $\Delta T_{LM}$ :

$$\Delta T_{LM} = \frac{(T_p - T_a)_B - (T_p - T_a)_A}{\ln \left[ \frac{(T_p - T_a)_B}{(T_p - T_a)_A} \right]} = \frac{(581 - 150) - (1000 - 970)}{\ln \left[ \frac{(581 - 150)}{(1000 - 970)} \right]}$$

$$\Delta T_{LM} = 150.5^\circ\text{C} .$$

Calculate the average tube diameter:

$$D_w = \frac{D_o - D_i}{\ln \left( \frac{D_o}{D_i} \right)} = \frac{0.0272 - 0.0222}{\ln \left( \frac{0.0272}{0.0222} \right)} = 0.0246 .$$

Calculate U, the overall heat transfer coefficient:

$$U = \left[ 1 / \frac{1}{H_p} + R_p + \left( \frac{1}{H_a} + R_a \right) \frac{D_o}{D_i} + \frac{Y_w}{K_w} \frac{D_o}{D_w} \right]$$

$$U = 1 / \frac{1}{1413} + 0.0001 + \left( \frac{1}{146} + 0.0003 \right) \frac{0.0272}{0.0222} + \frac{0.0025}{11} = \frac{0.0272}{0.0246} = 103 \text{ W/m}^2 \text{ K} .$$

### Required Heat Transfer Area

Given:

$$U = 103 \text{ W/m}^2 \text{ K}$$

$$\Delta T_{LM} = 150^\circ \text{C}$$

$$Q = 100 \times 10^6 \text{ W} .$$

$$Q = UA\Delta T_{LM} .$$

Solving for the area,

$$A = \frac{Q}{U\Delta T_{LM}}$$

$$A = \frac{100 \times 10^6}{(103)(150.5)} = 6450 \text{ m}^2 .$$



APPENDIX D. SAMPLE CALCULATIONS FOR PRESSURE DROP IN  
SHELL-AND-TUBE HEAT EXCHANGER

Pressure Drop in Tubes

Given:

$$Re = 40,000$$

$$D_H = 0.0222 \text{ m}$$

$$\rho_a = 0.833 \text{ kg/m}^3$$

$$\mu = 0.000024 \rho_a \cdot s$$

$$C_{pa} = 1018 \text{ J/kg K} .$$

Compute air velocity:

$$Re = \frac{\rho_a V_a D_H}{\mu} \rightarrow V_a = \frac{Re \mu}{\rho_a D_H}$$

$$V_a = \frac{(40,000)(0.000024)}{(0.833)(0.0222)} = 51.9 \text{ m/s} .$$

Compute friction factor:

$$f = \frac{0.046}{Re^{0.2}} = \frac{0.046}{(40,000)^{0.2}} = 5.53 \times 10^{-3} .$$

Compute mass flow rate per tube of air:

$$\dot{m}_t = \rho_a A_t V_a = \frac{(0.833) \pi (0.0222^2) (51.9)}{4} = 0.0167 \text{ kg/s} .$$

Compute total mass flow rate of air:

$$Q = \dot{m} C_{pa} \Delta T_a \rightarrow \dot{m} = \frac{Q}{C_{pa} \Delta T_a}$$

$$\dot{m} = \frac{100 \times 10^6}{(1018)(970 - 150)} = 119.8 \text{ kg/s} .$$

Compute number of tubes required:

$$NT = \frac{\dot{m}}{\dot{m}_t} = \frac{119.8}{0.0167} = 7173 \text{ tubes} .$$

Compute tube length:

$$A = NT \times A_t = NT \times \pi D_o L$$

$$L = \frac{A}{NT \pi D_o} = \frac{6450}{(7173)(\pi)(0.0272)}$$

$$L = 10.5 \text{ m} .$$

Compute pressure drop:

$$\Delta P = \frac{2f V_a^2 L \rho_a}{D_H}$$

$$\Delta P = \frac{2(5.53 \times 10^{-3})(51.9)^2(10.5)(0.833)}{0.0222}$$

$$\Delta P = 11,737 \text{ Pa} .$$

## DISTRIBUTION LIST

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